
EFFICIENT ADAPTIVELY SECURE ZERO- KNOWLEDGE FROM GARBLED CIRCUITS

Chaya Ganesh

Aarhus

Yashvanth Kondi

Northeastern

Arpita Patra

Indian Inst. of

Pratik Sarkar

Science

OUR RESULTS

- We start from [Jawurek-Kerschbaum-Orlandi13] ZK protocol:
improve rounds and upgrade to **adaptive security**
(without erasures) at essentially **zero overhead**
 - This gives us the first **practical adaptively secure ZK protocol**
-

ADAPTIVE ZERO-KNOWLEDGE FROM GARBLED CIRCUITS

x f_x

P

w

V

ADAPTIVE ZERO-KNOWLEDGE FROM GARBLED CIRCUITS

$$x \quad f_x(w) = 1 \quad \text{if } x \in L$$

P

w

V

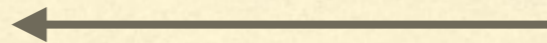
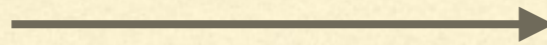
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accept/reject

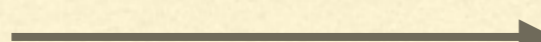
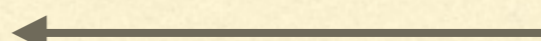
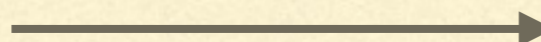
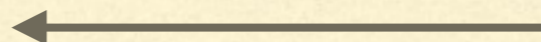
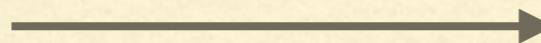
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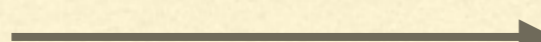
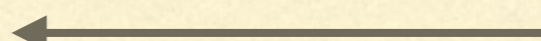
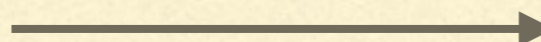
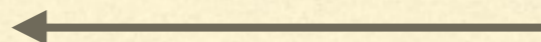


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Sim_P



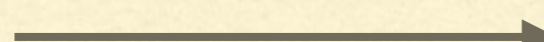
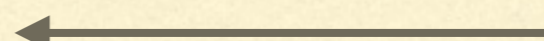
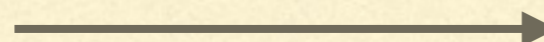
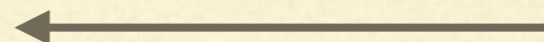
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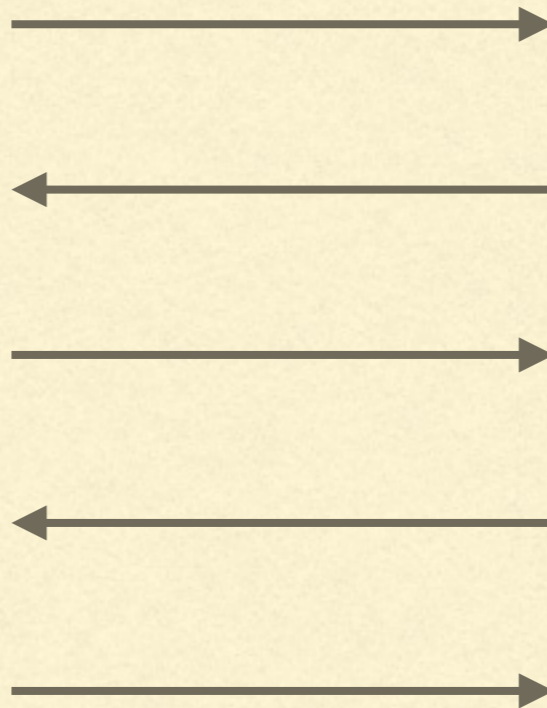
$$\{\langle \mathbf{P}(w), \mathbf{V} \rangle(x)\}_{x \in L} \approx_c \{\langle \text{Sim}_P \rangle(x)\}_{x \in L}$$

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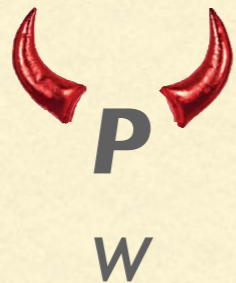
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Sim_v

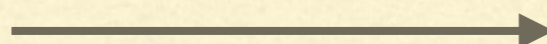
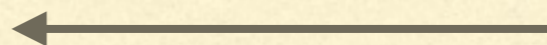
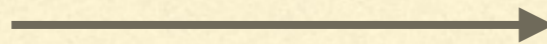
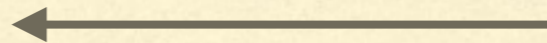
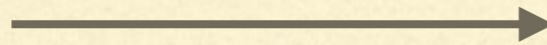


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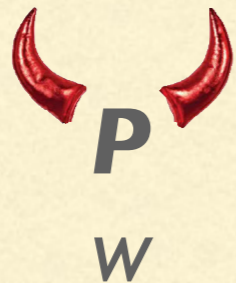
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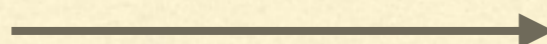
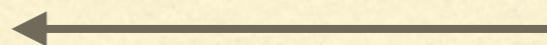
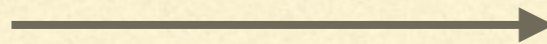
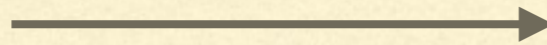
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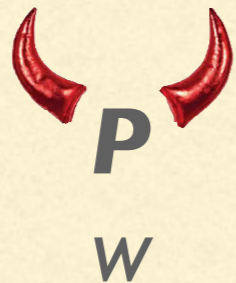
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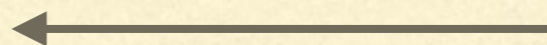
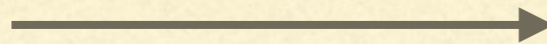
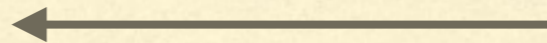
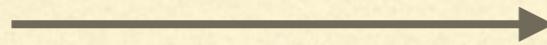
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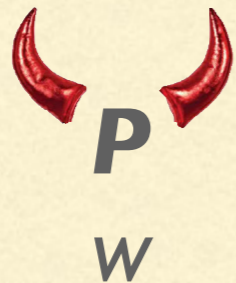
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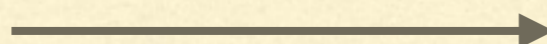
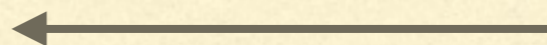
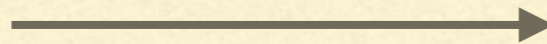
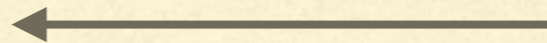
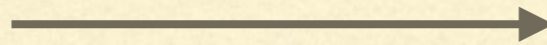
accept
w

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accept
 $f_x(w) = 1$

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- Previous definition models static corruptions
 - Adaptive corruptions closer to real world; systems ‘hacked’ dynamically
 - Adaptive ZK composed to build larger protocols resilient to dynamic corruptions
 - Adaptive security without erasures: Every simulated transcript has to be completely ‘explainable’ wrt any witness
-

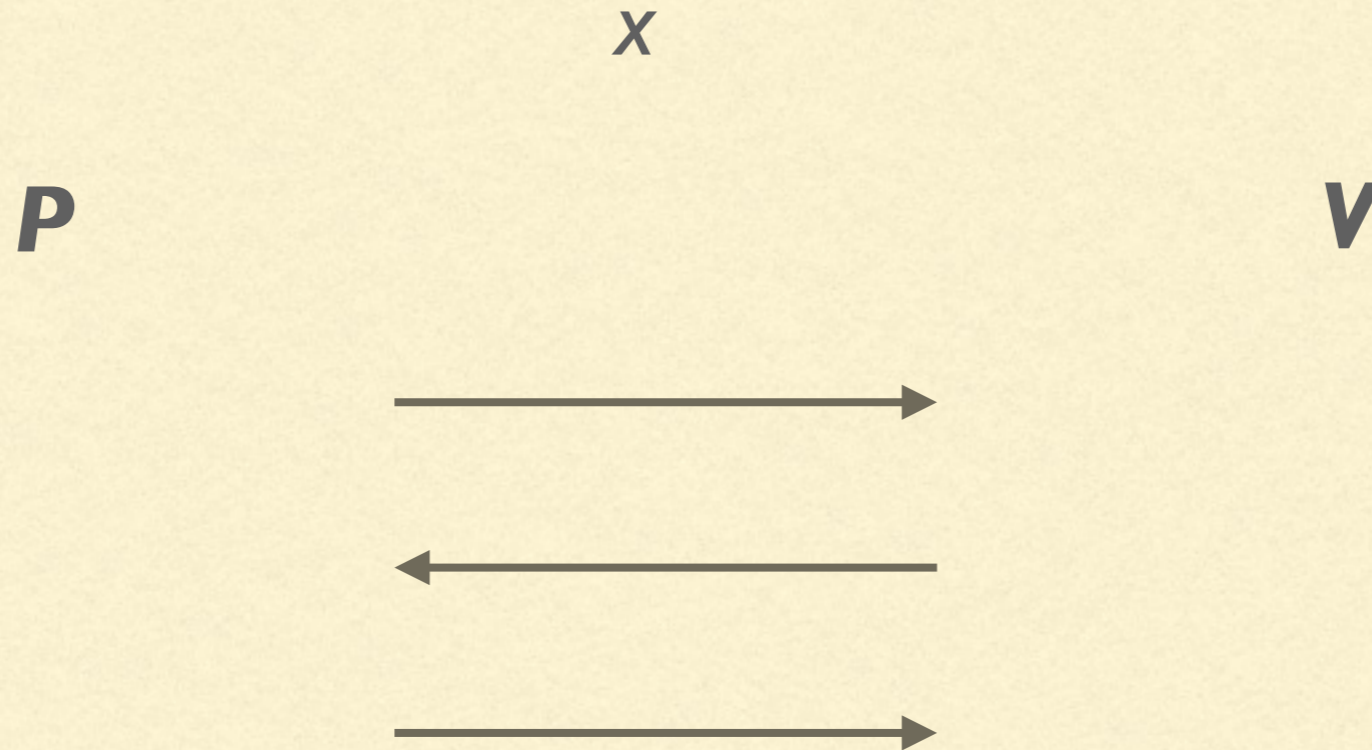
ADAPTIVE ZERO-KNOWLEDGE FROM GARBLED CIRCUITS

x

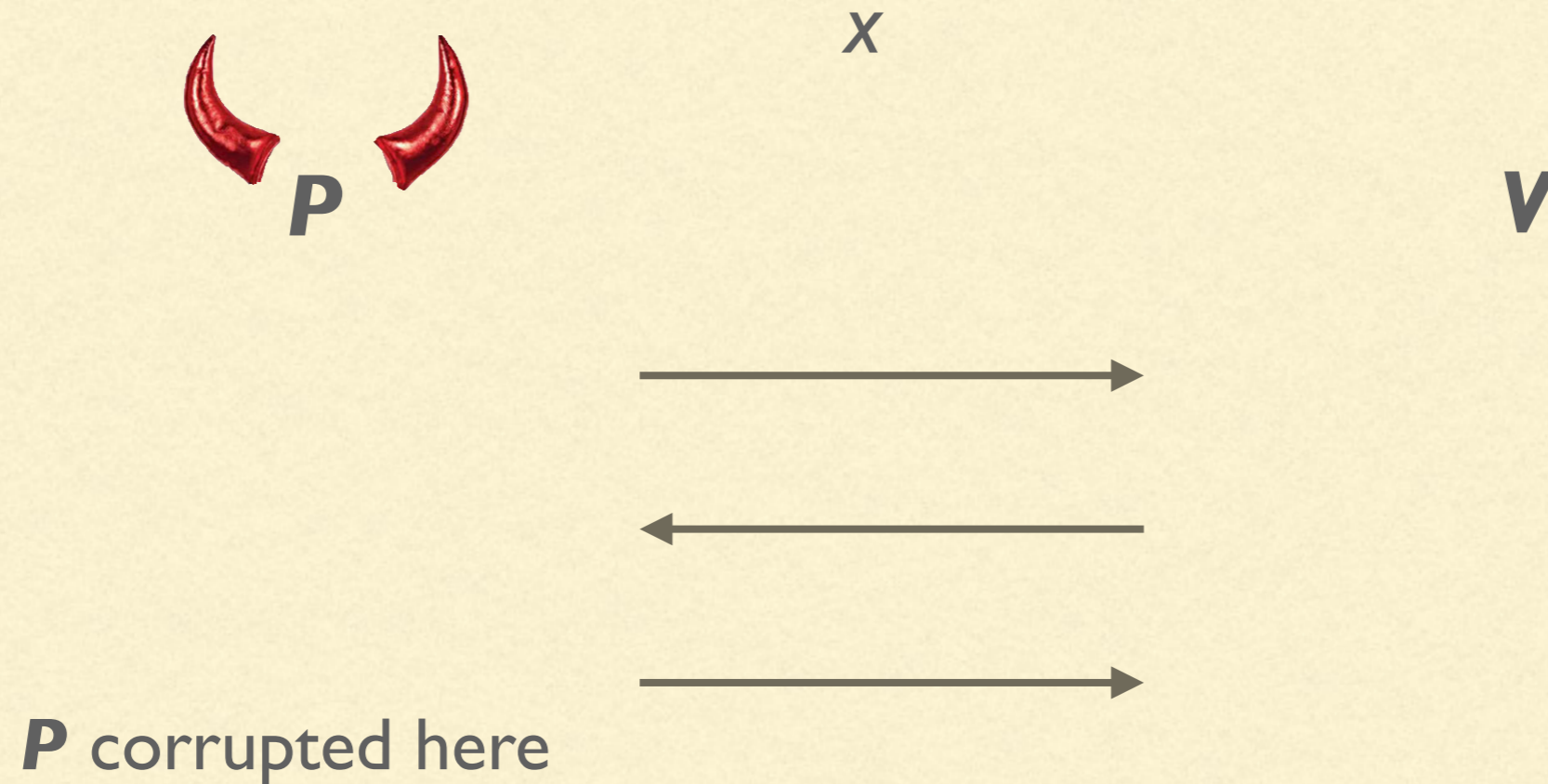
P

V

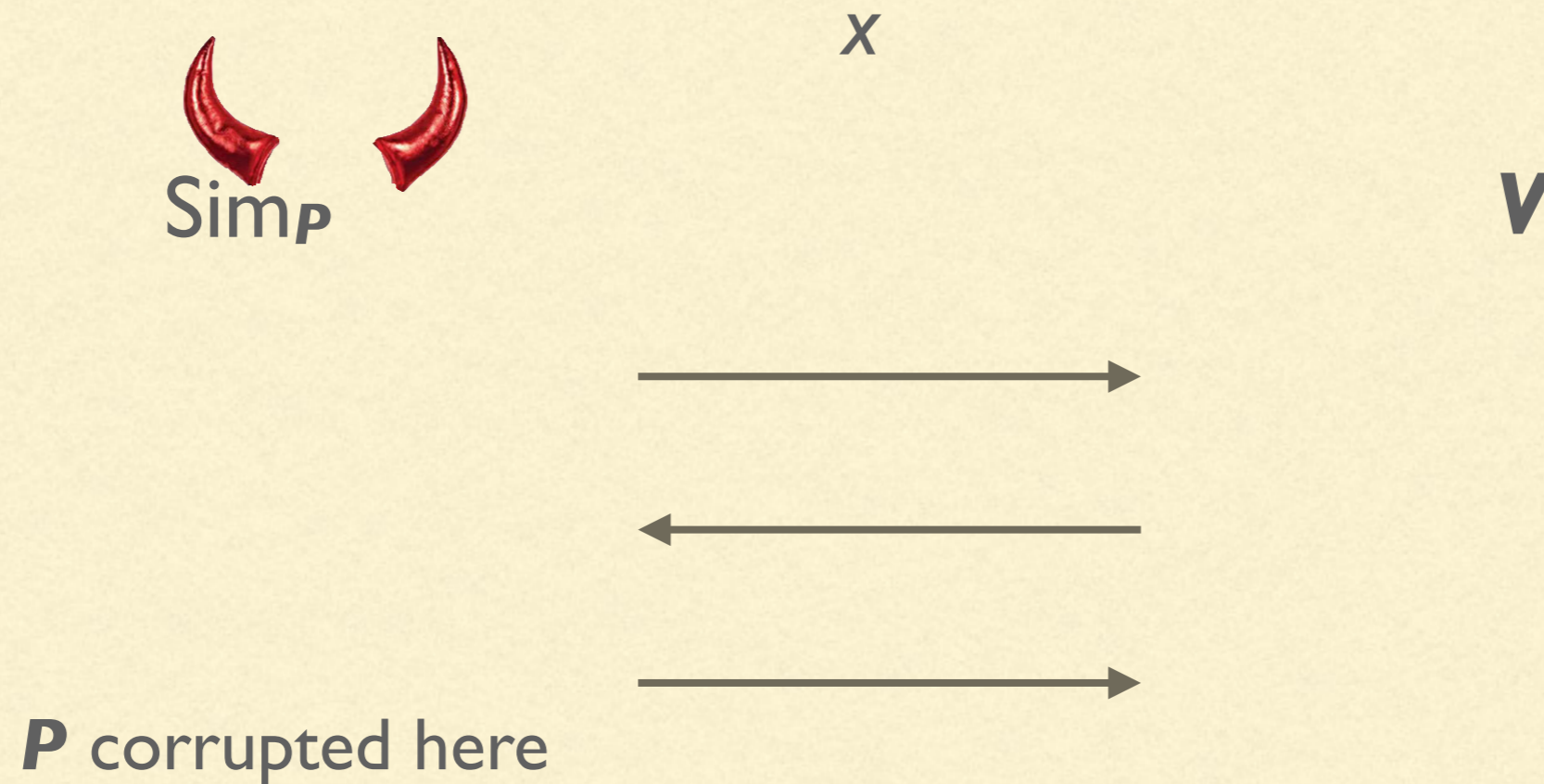
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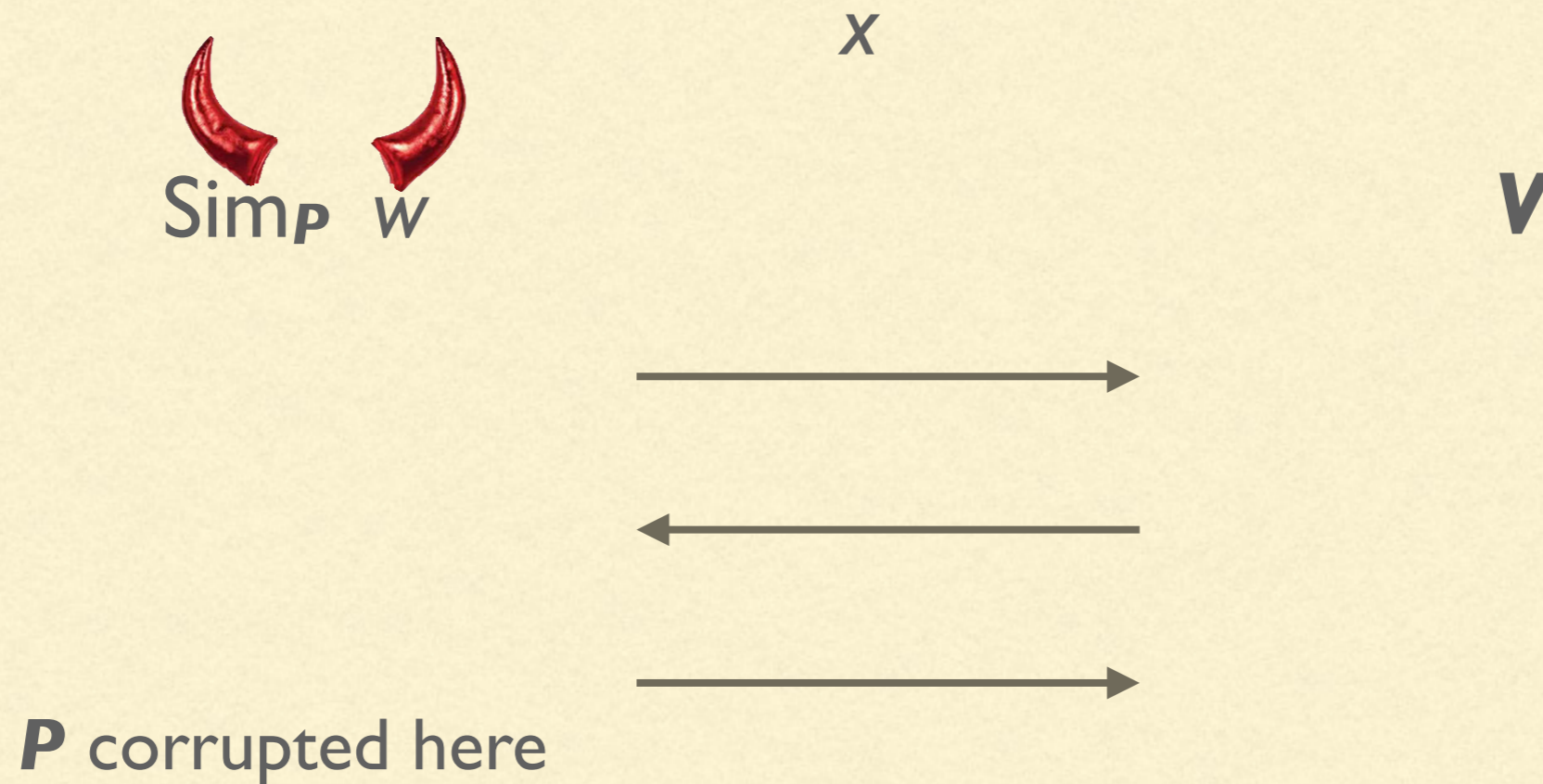
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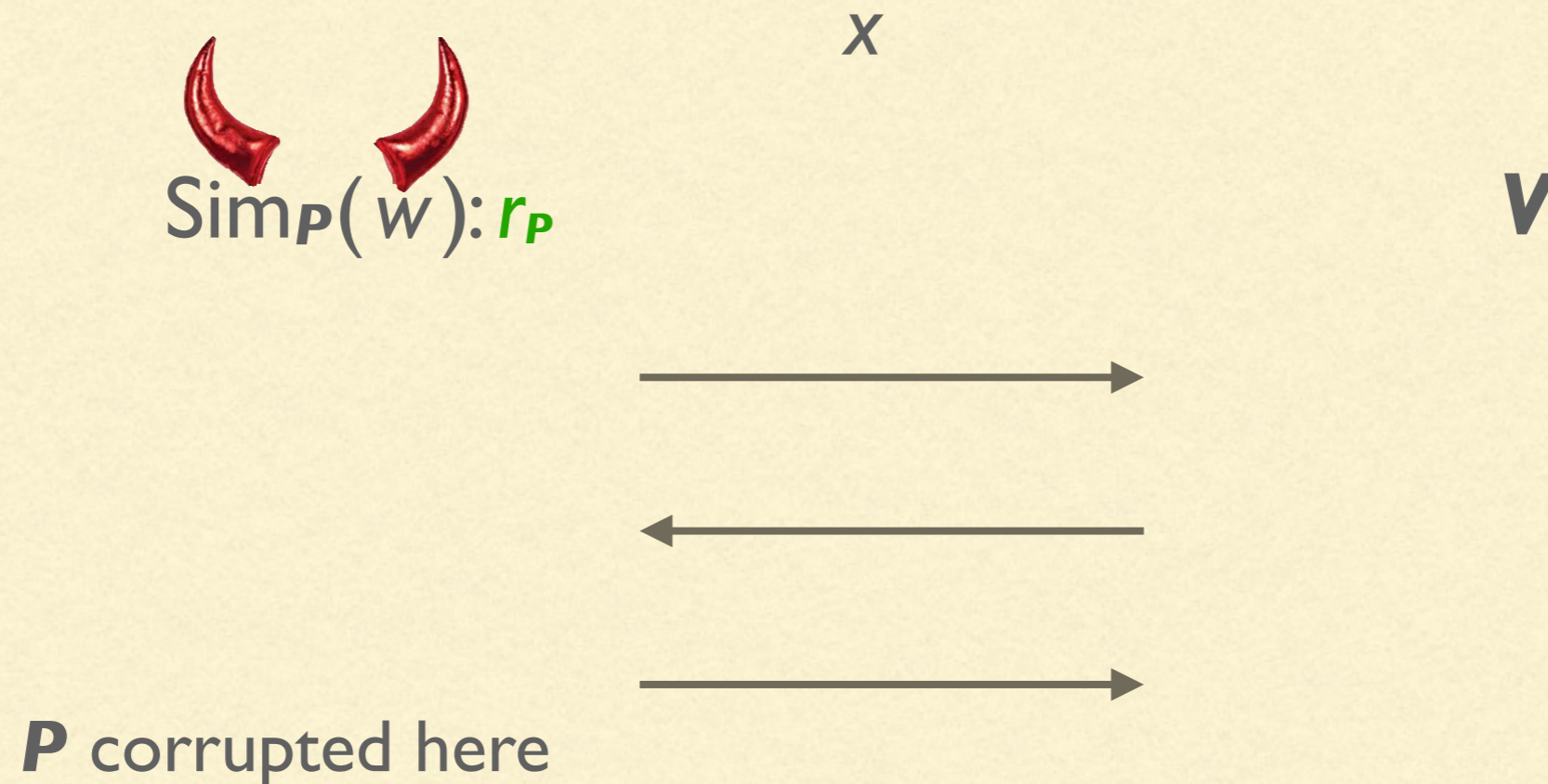
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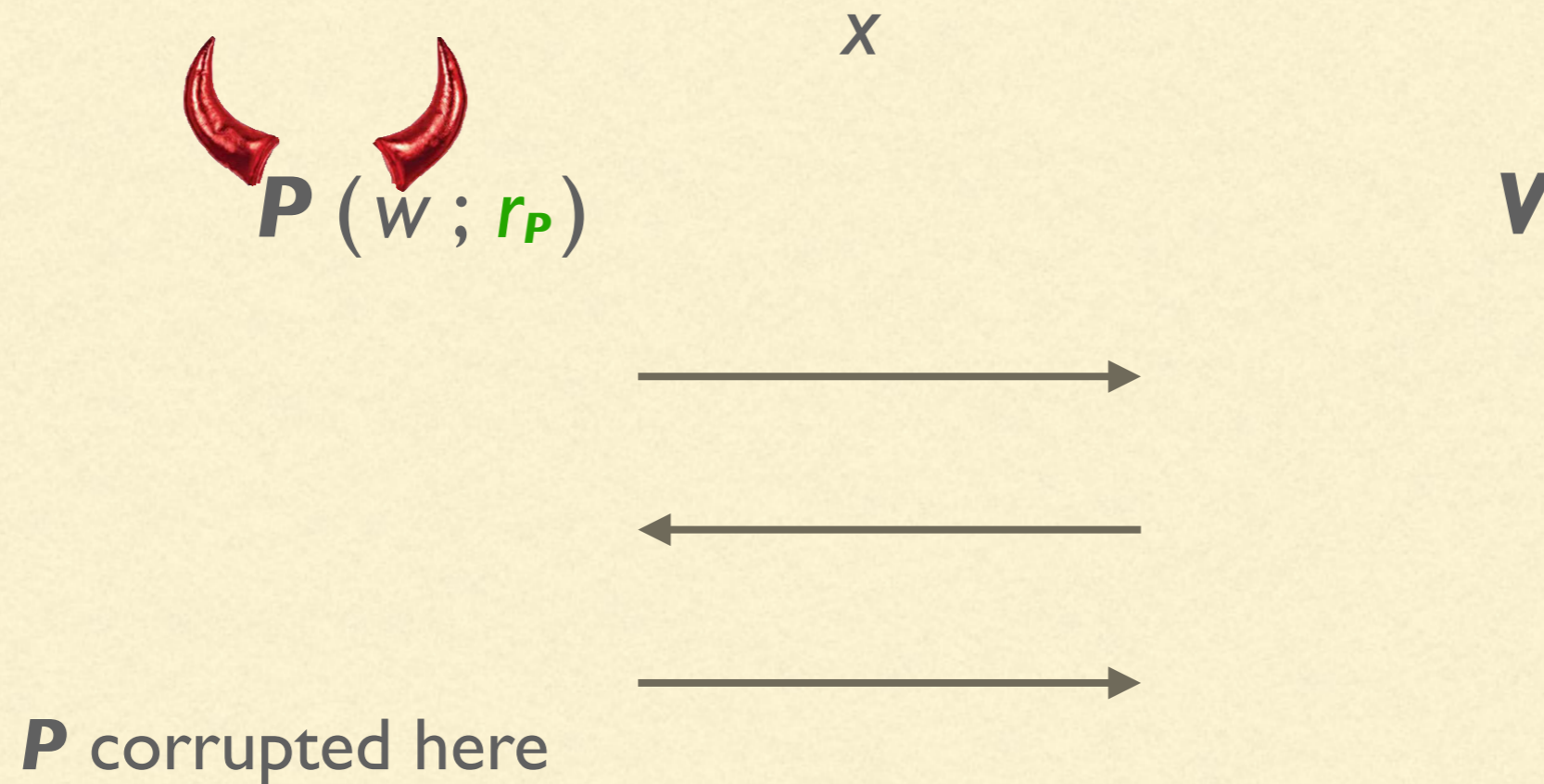
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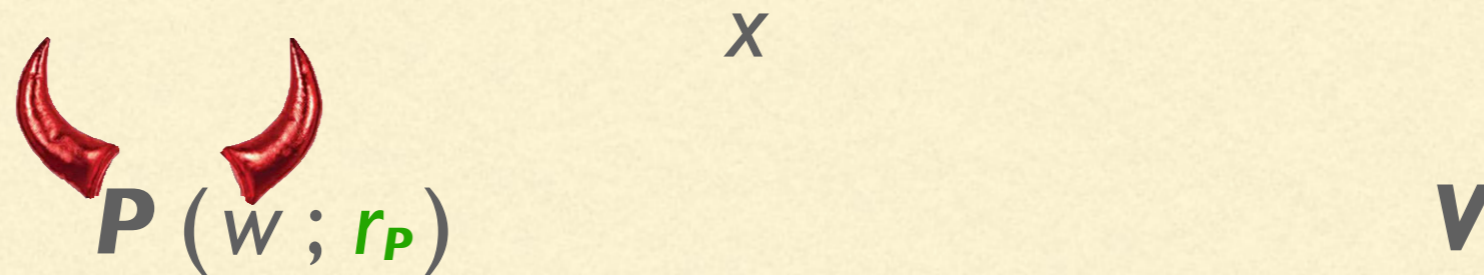
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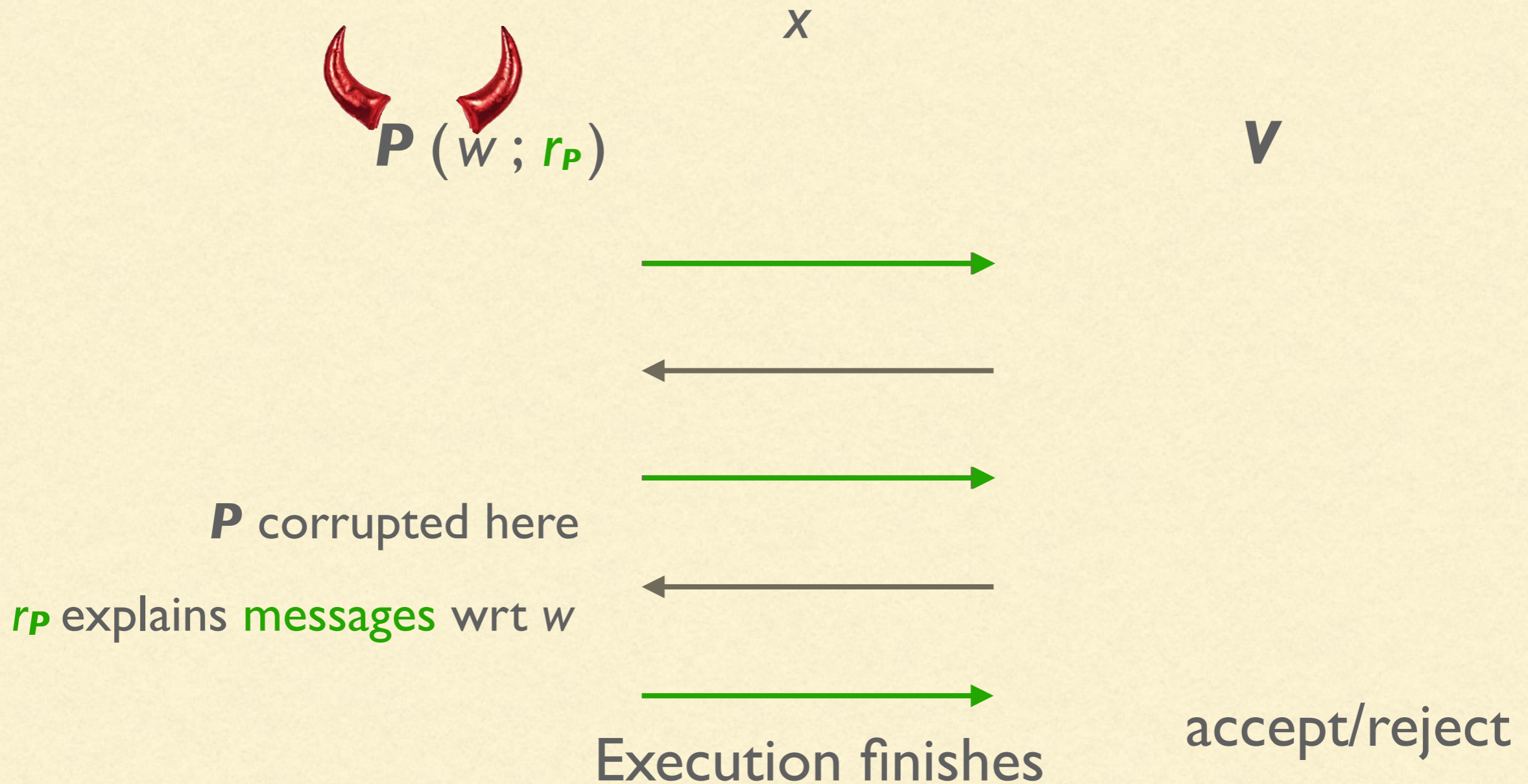
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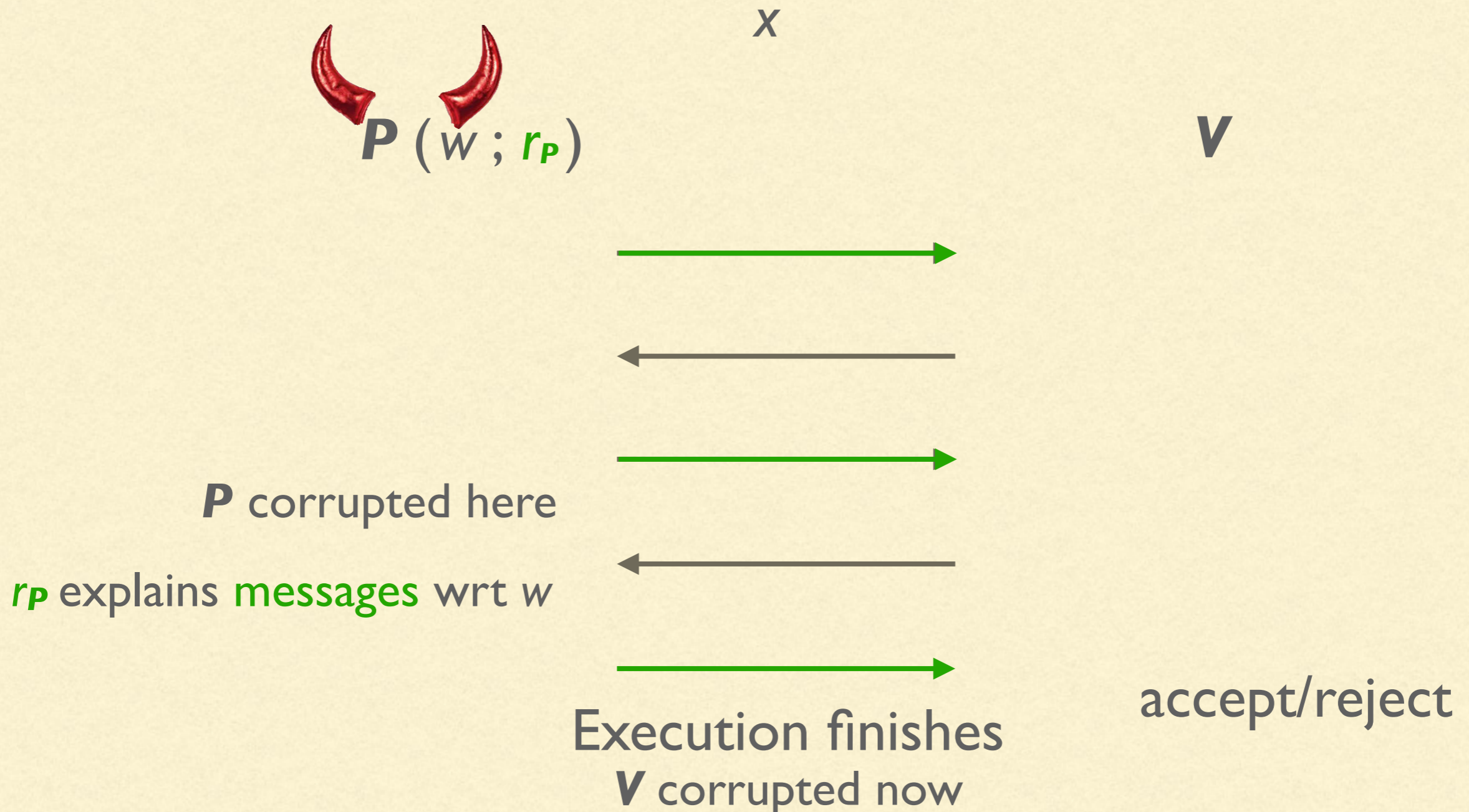
P corrupted here

r_P explains messages wrt w

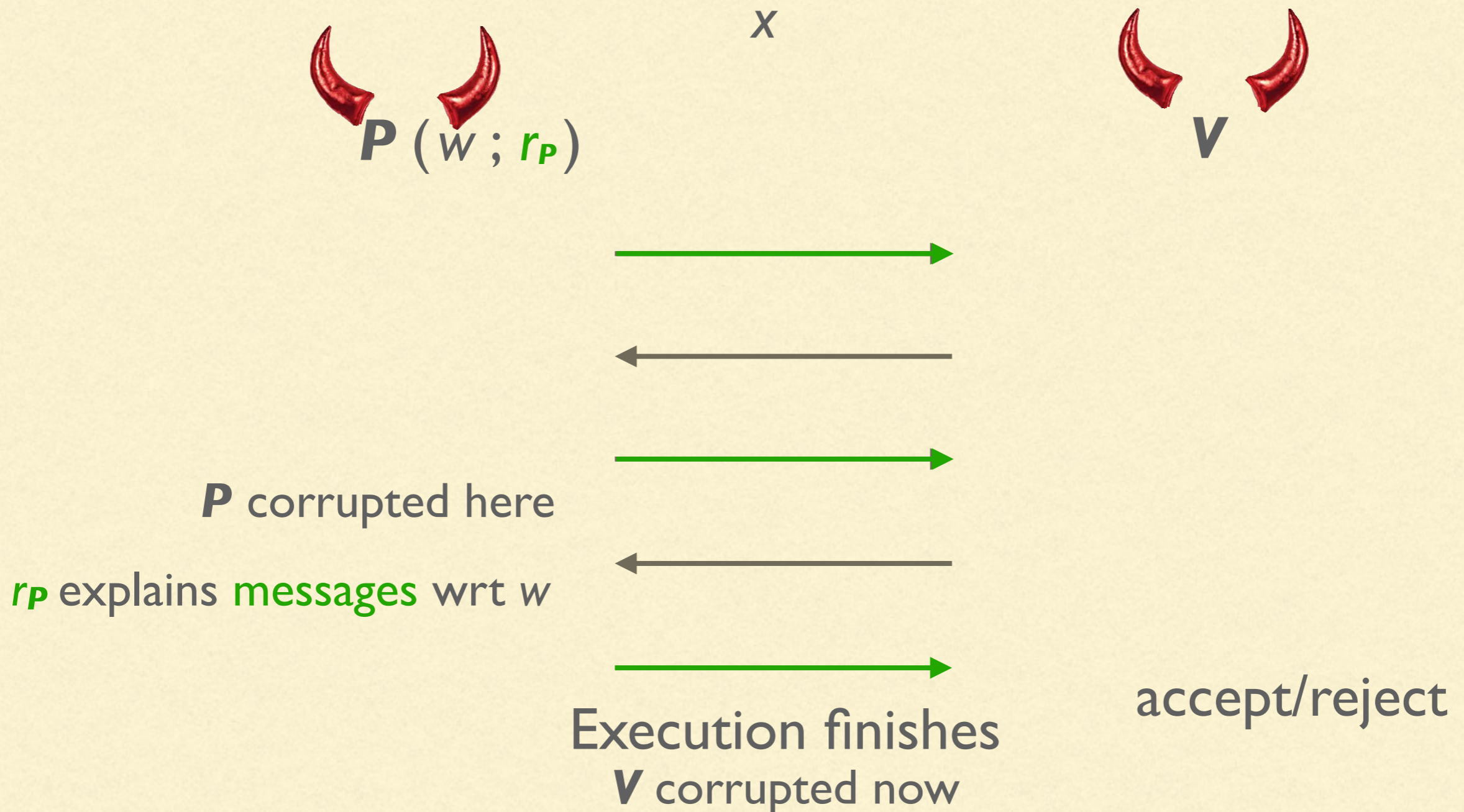
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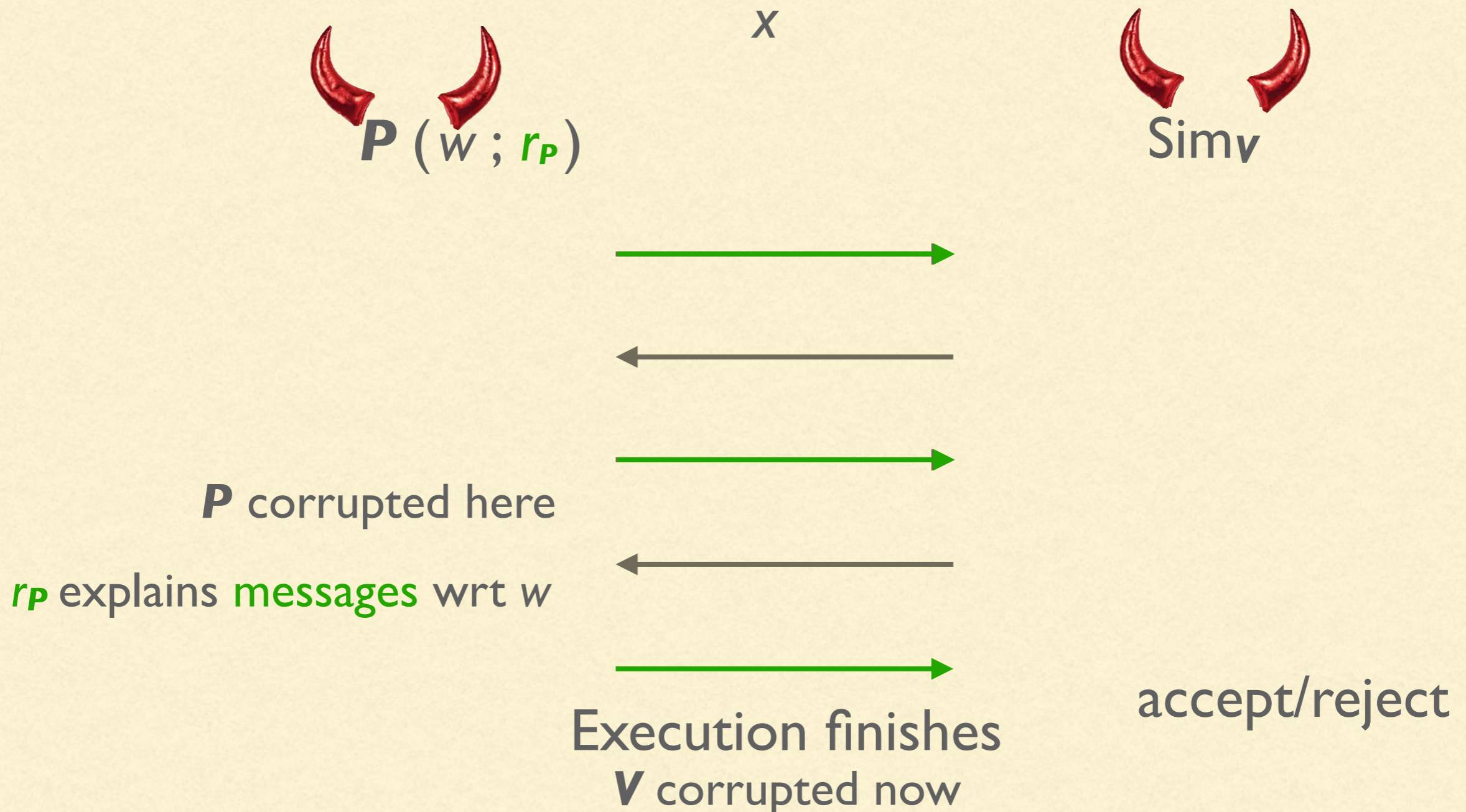
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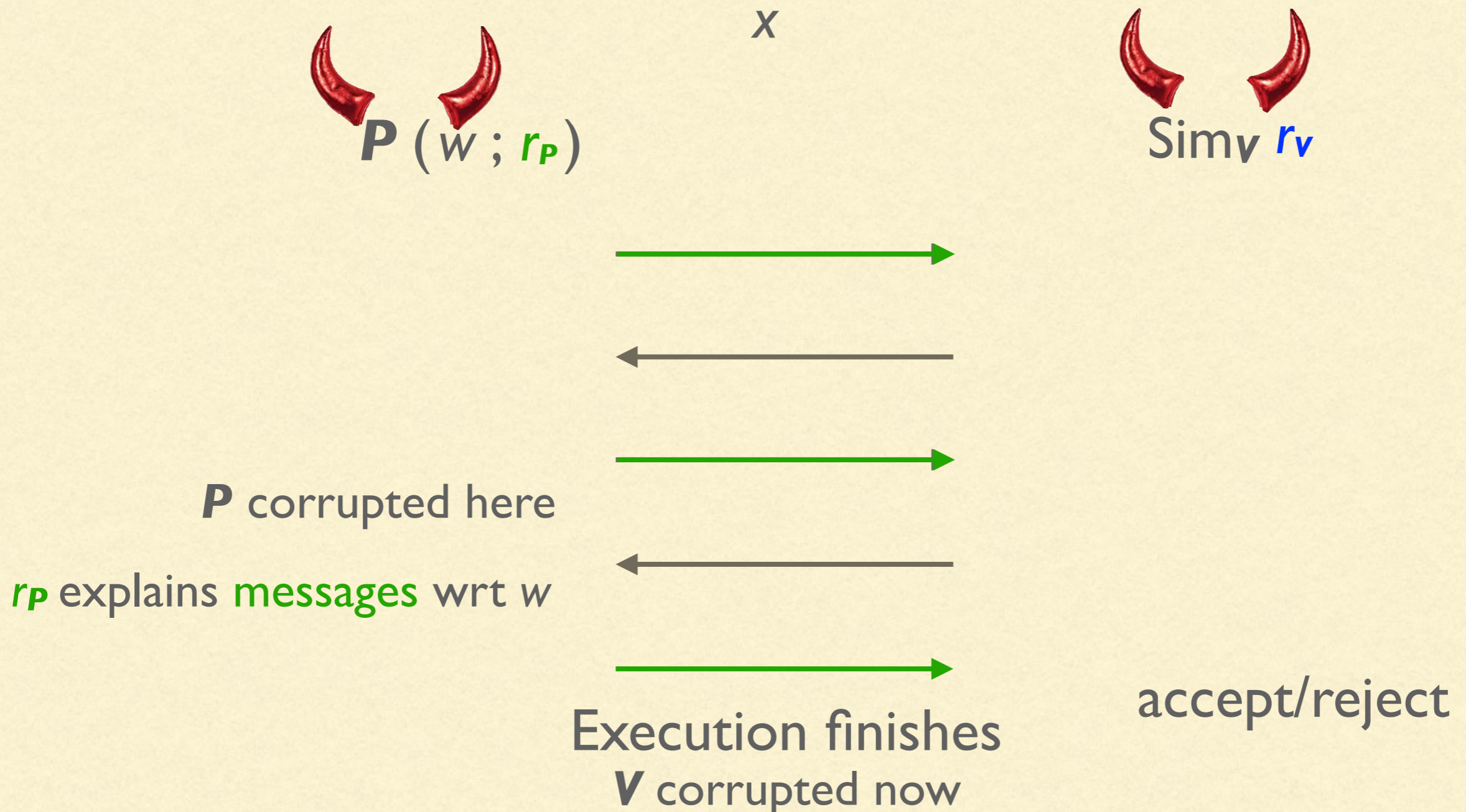
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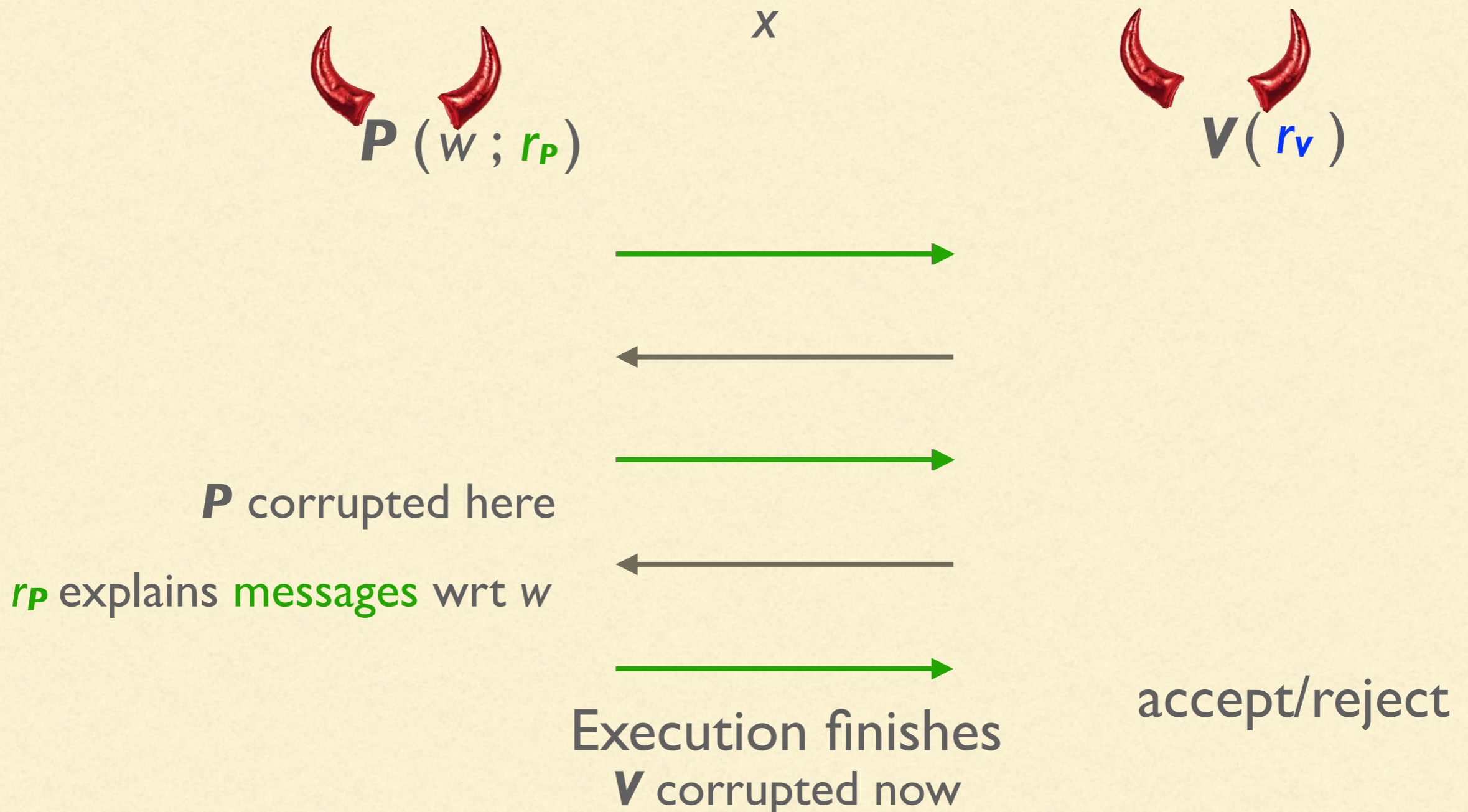
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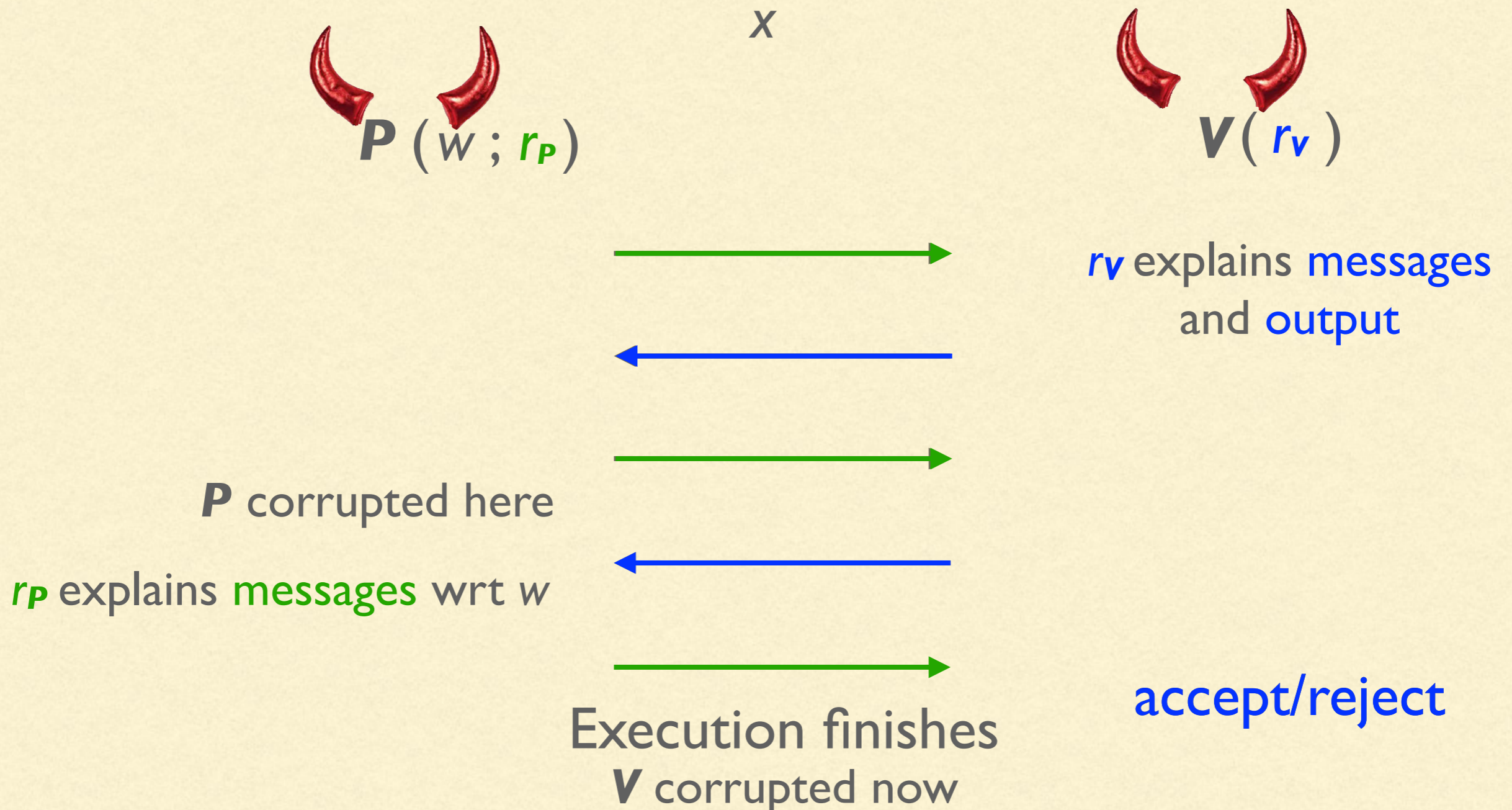
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ADAPTIVE ZERO-KNOWLEDGE: DESIDERATA

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- Most useful when **universally composable (UC)**
 - Asymptotic: **constant rounds, linear communication**
 - Towards **concrete efficiency**
 - Assumptions: standard public-key (**DDH, LWE, LPN, QR**)
-

RELATED WORK

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 - [Hazay-Venkatasubramaniam 16] Adaptive ZK from OWFs, Non-constant rounds, quasi-linear communication, standalone security
 - [Jawurek-Kerschbaum-Orlandi 13] ZK from GCs: Static security, **upgraded** to adaptive with greater efficiency **in this work**
-

TECHNICAL CONTRIBUTIONS

Improving
efficiency

Improving
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OT+I rounds, UC ZK, linear
comm, GRO model

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Adaptive UC ZK from Recv-
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Adaptive UC ZK from Recv-
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- Any OT can be transformed to Recv-Equiv OT [Canetti-Lindell-Ostrovsky-Sahai 02]
 - Two-round UC static ZK from garbled circuits with CRS
-

BUILDING BLOCK: GARBLED CIRCUITS

- Introduced by [Yao 86], formalization of [Bellare-Hoang-Rogaway 12]

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|^k

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$|k$

f

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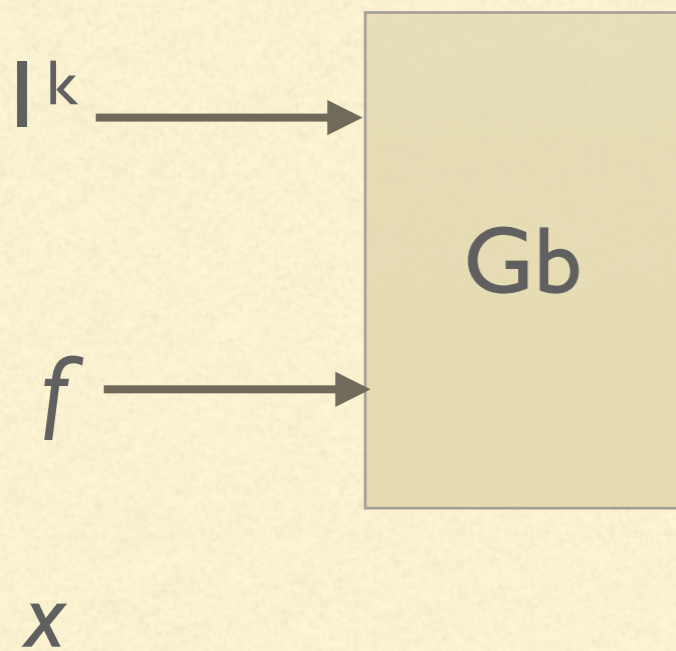
$|k$

f

x

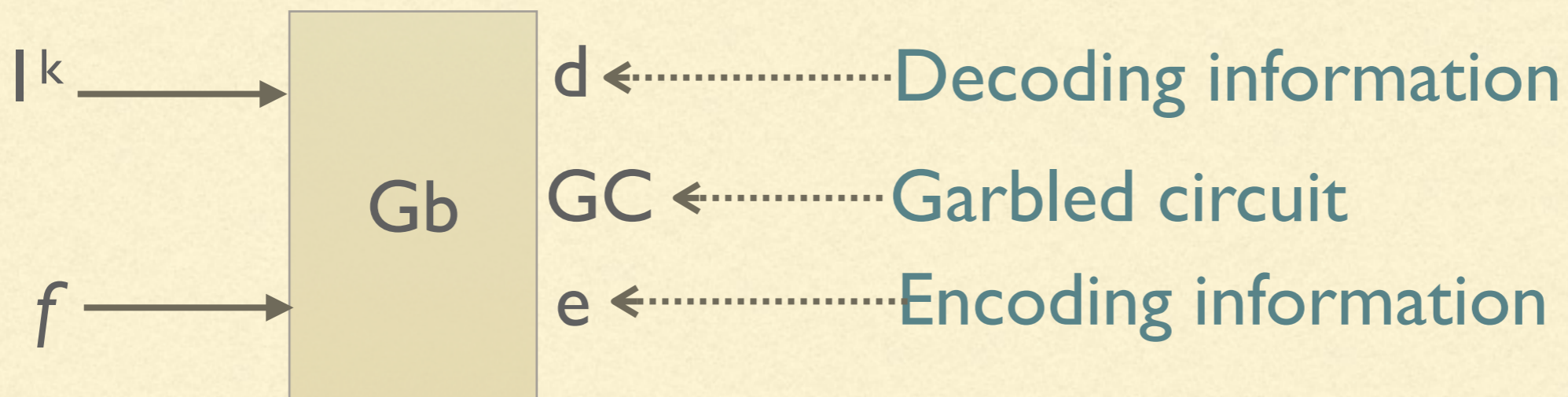
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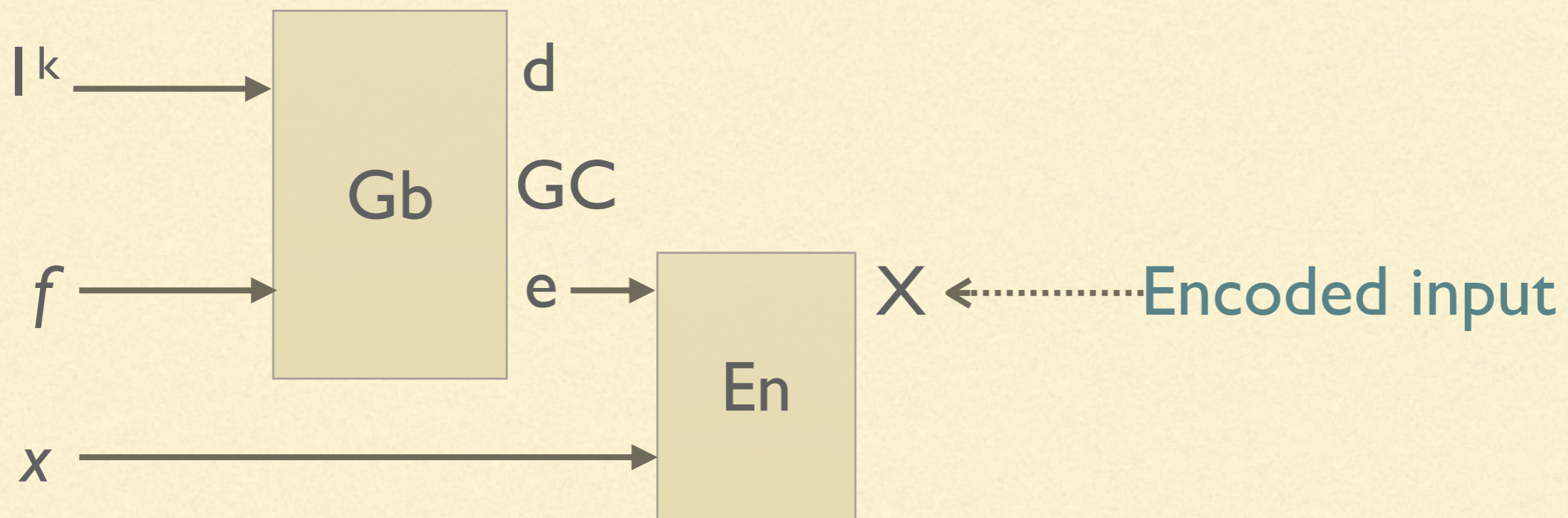
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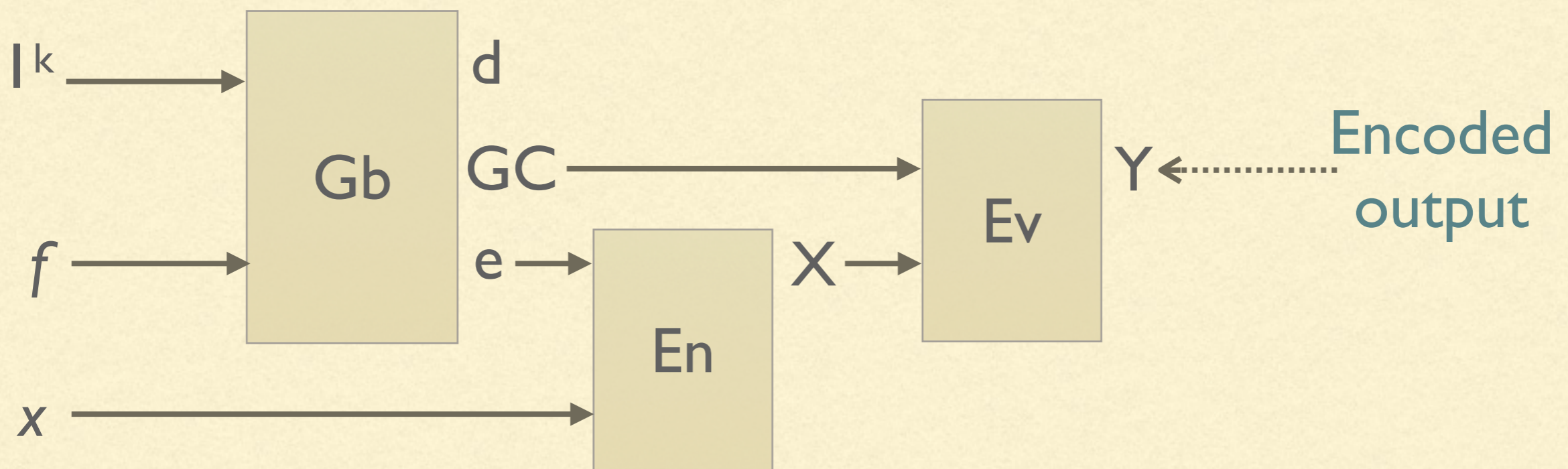
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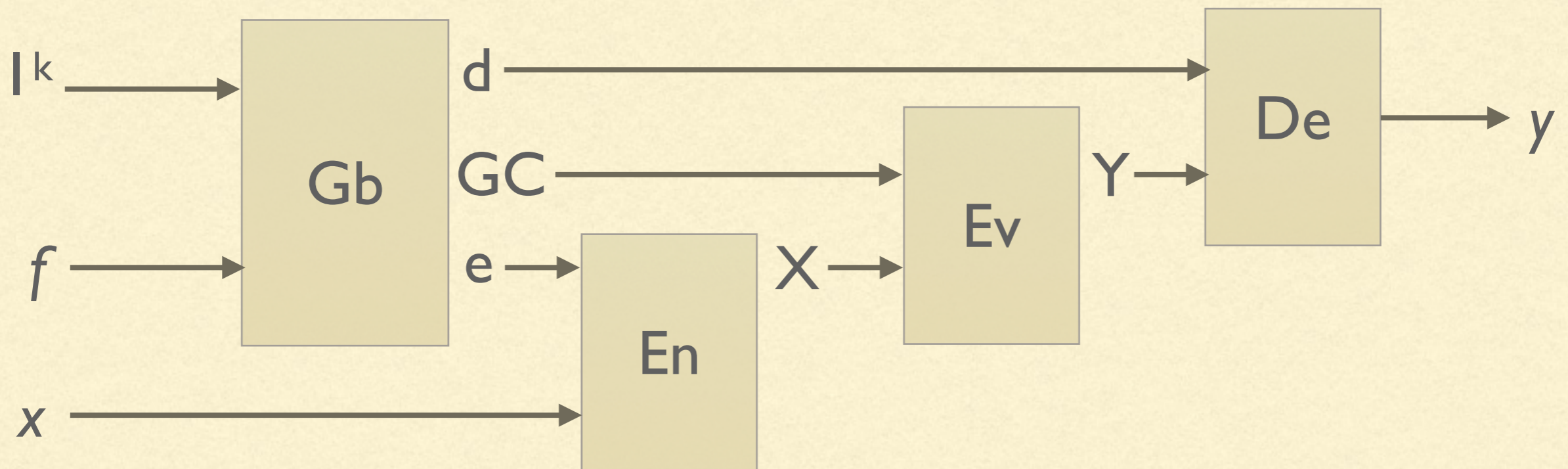
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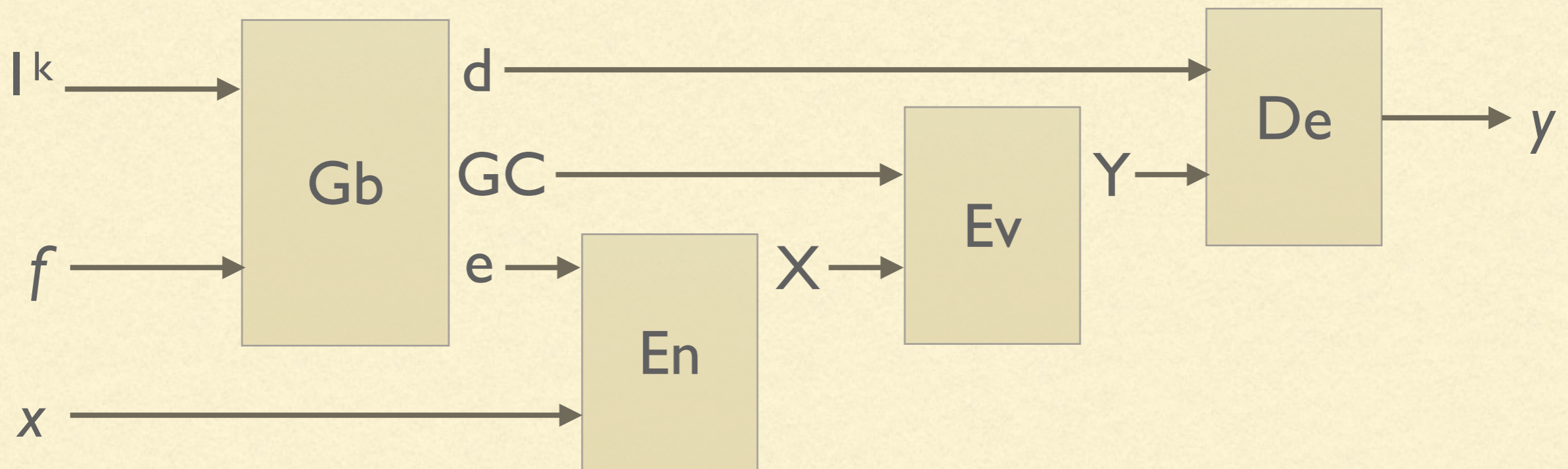
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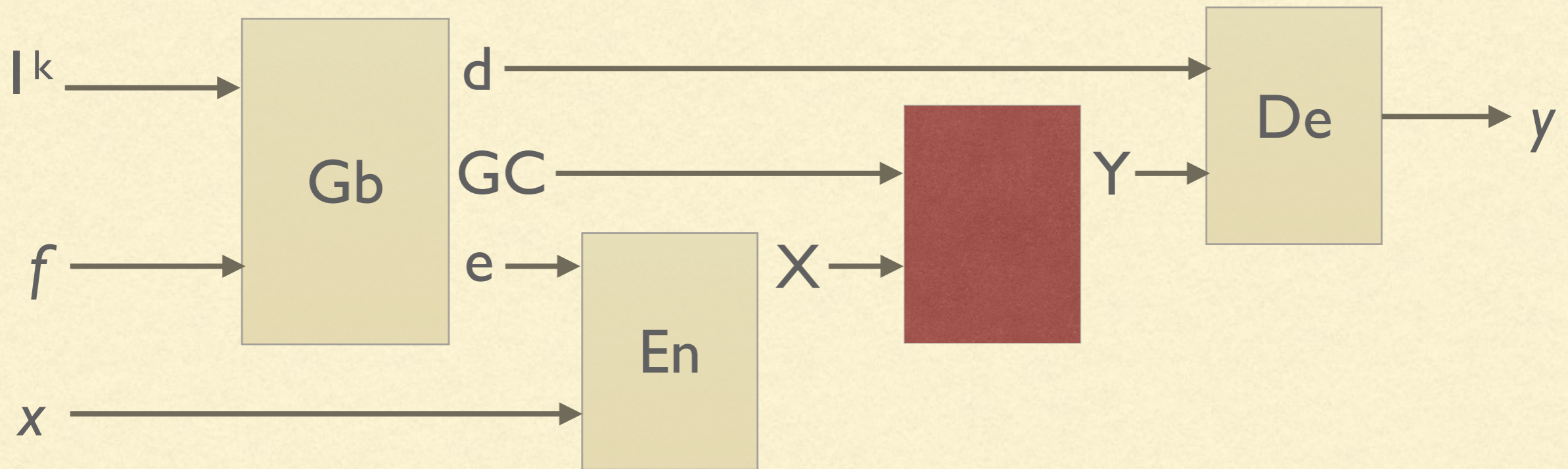
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- Correctness: $f(x) = y$

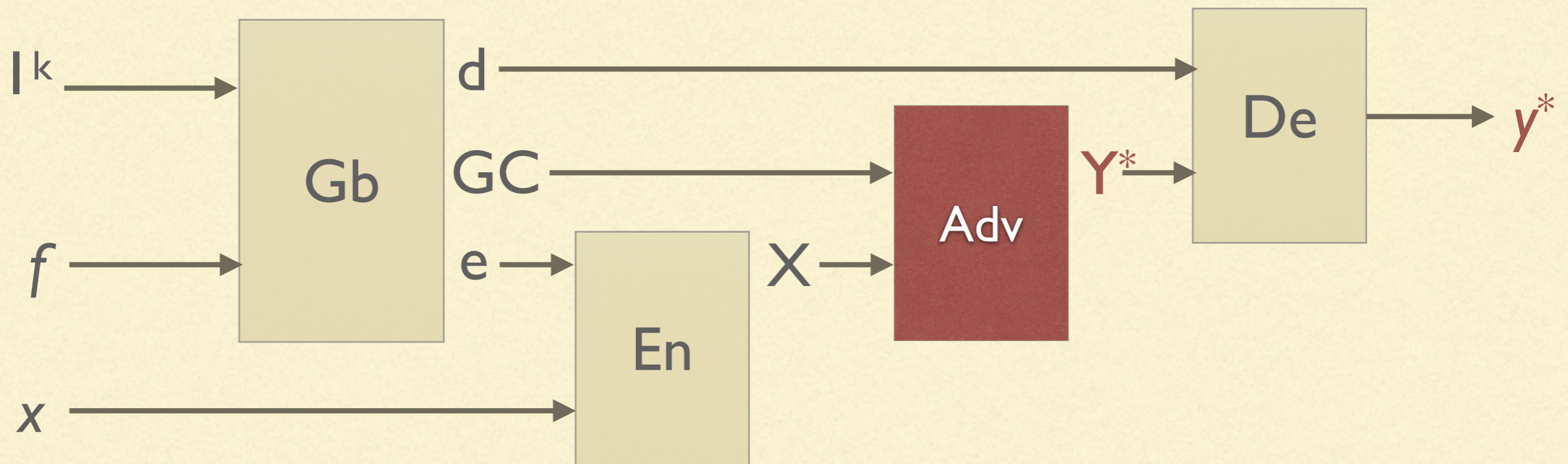
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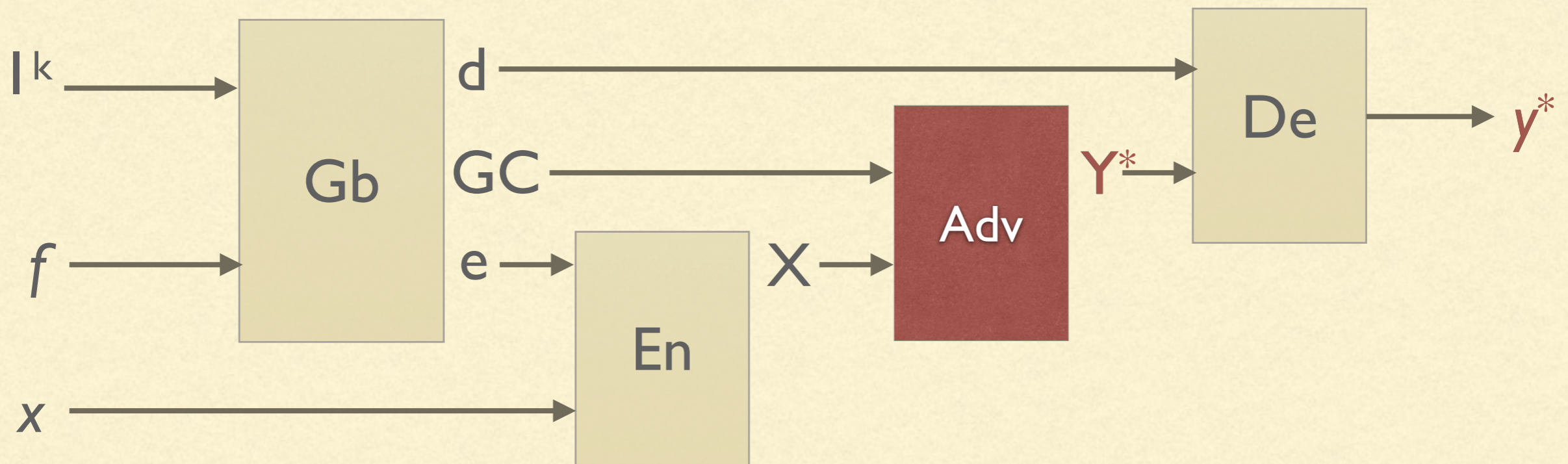
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- Authenticity: $Y^* = \text{Ev}(GC, X)$

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- Authenticity: $Y^* = \text{Ev}(GC, X)$... or **De** fails

BUILDING BLOCK: 1-2 OBLIVIOUS TRANSFER

S

R

BUILDING BLOCK: 1-2 OBLIVIOUS TRANSFER

S

R

m_0

m_1

BUILDING BLOCK: 1-2 OBLIVIOUS TRANSFER

S

m_0

m_1

R

b

BUILDING BLOCK: 1-2 OBLIVIOUS TRANSFER

S

m_0

m_1



OT

R

b

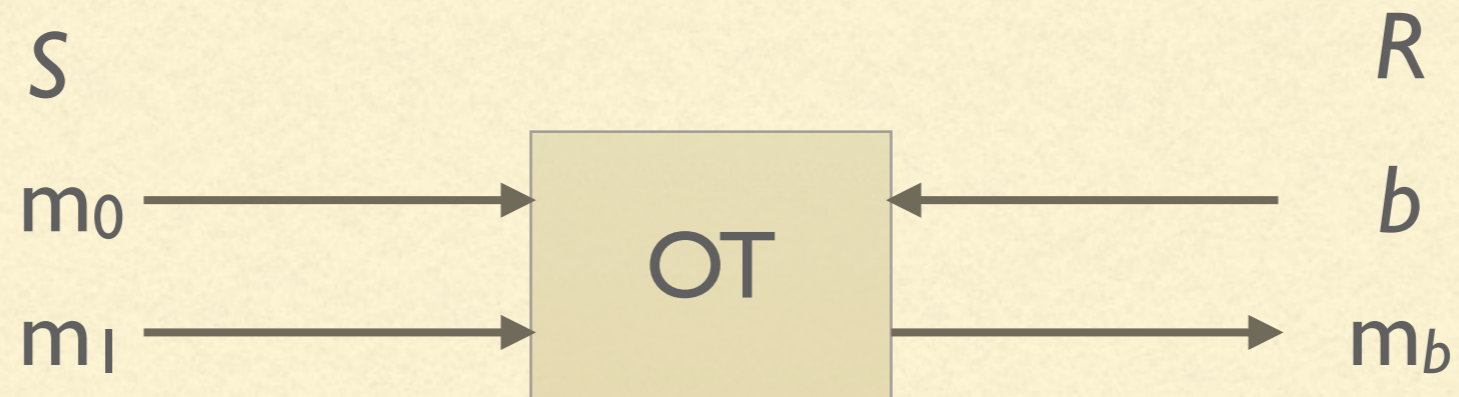
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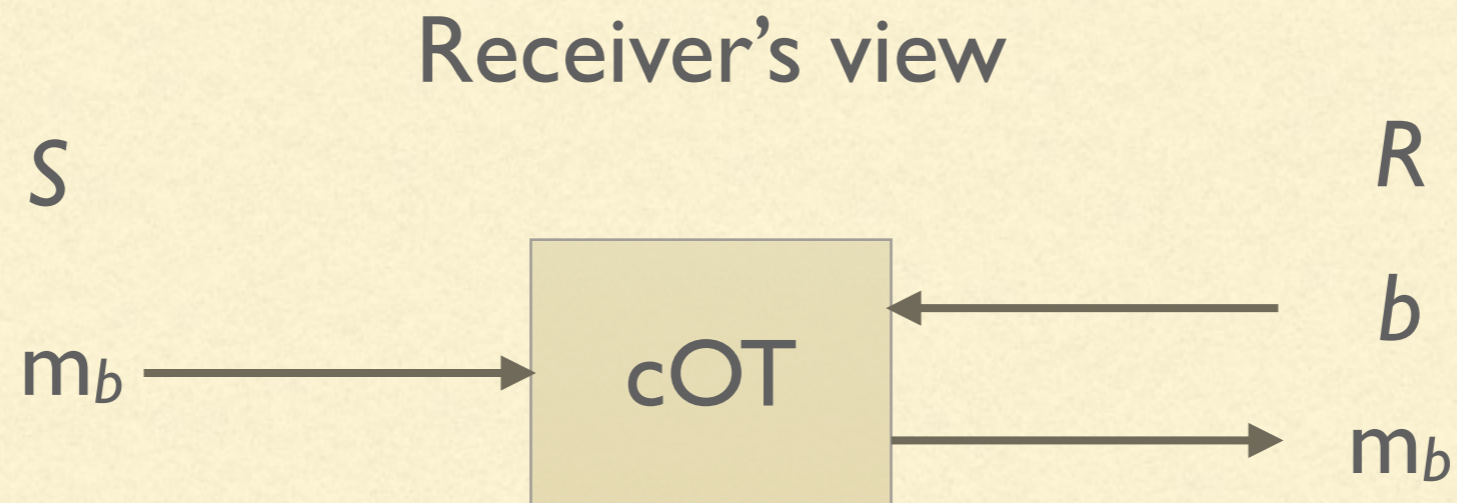


BUILDING BLOCK: 1-2 OBLIVIOUS TRANSFER



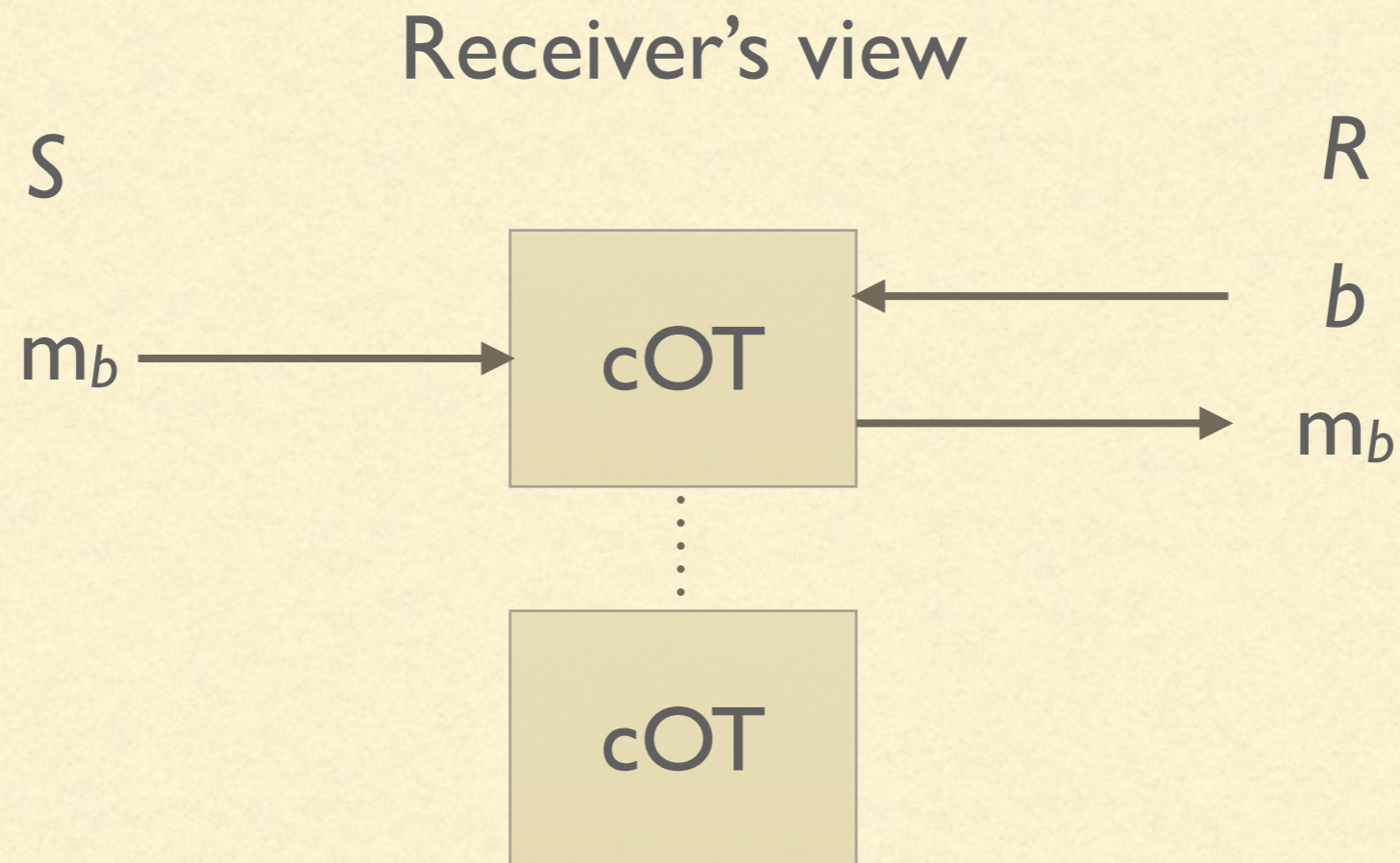
BUILDING BLOCK: COMMITTED OBLIVIOUS TRANSFER

- For this protocol: committed cOT



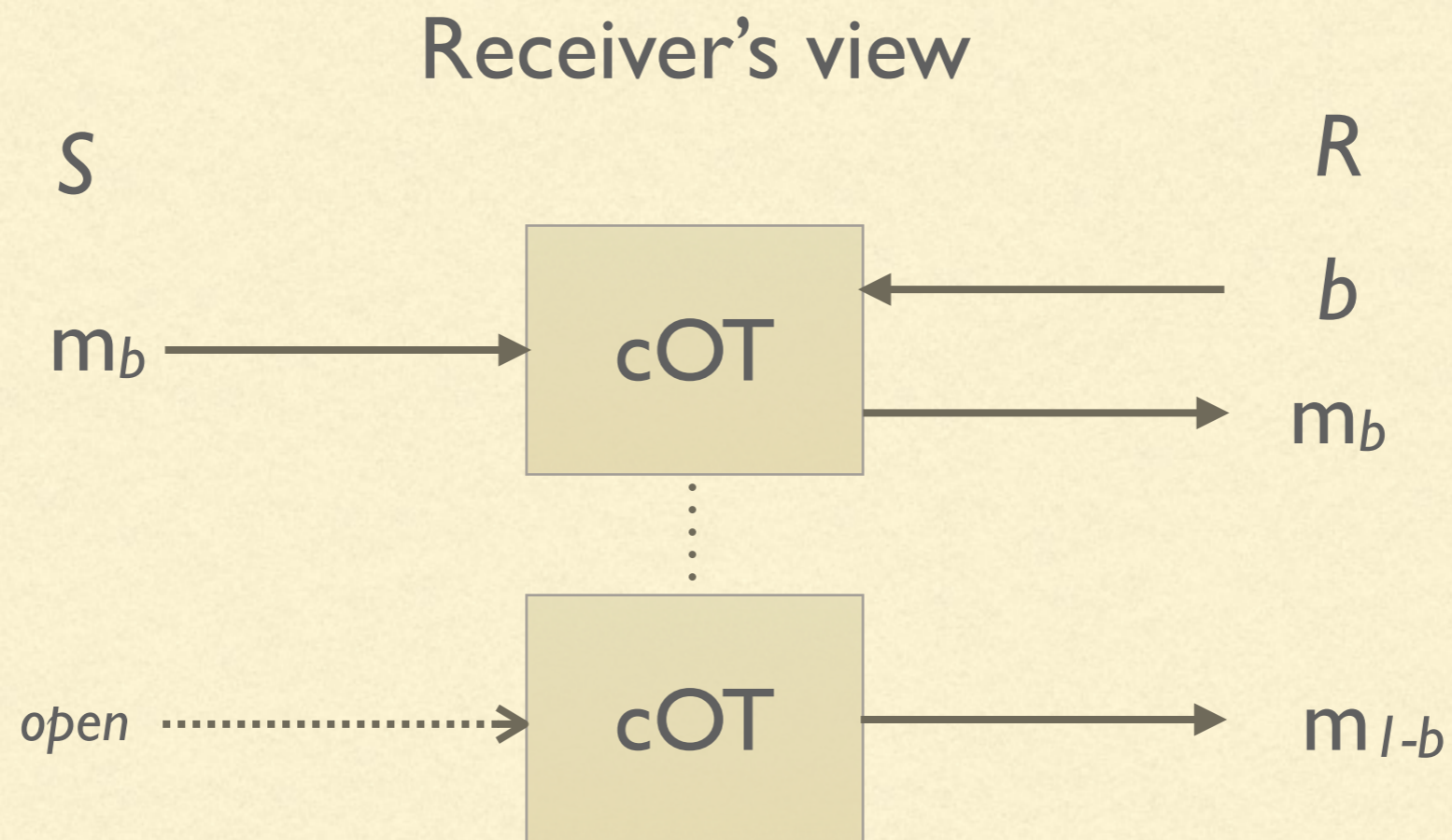
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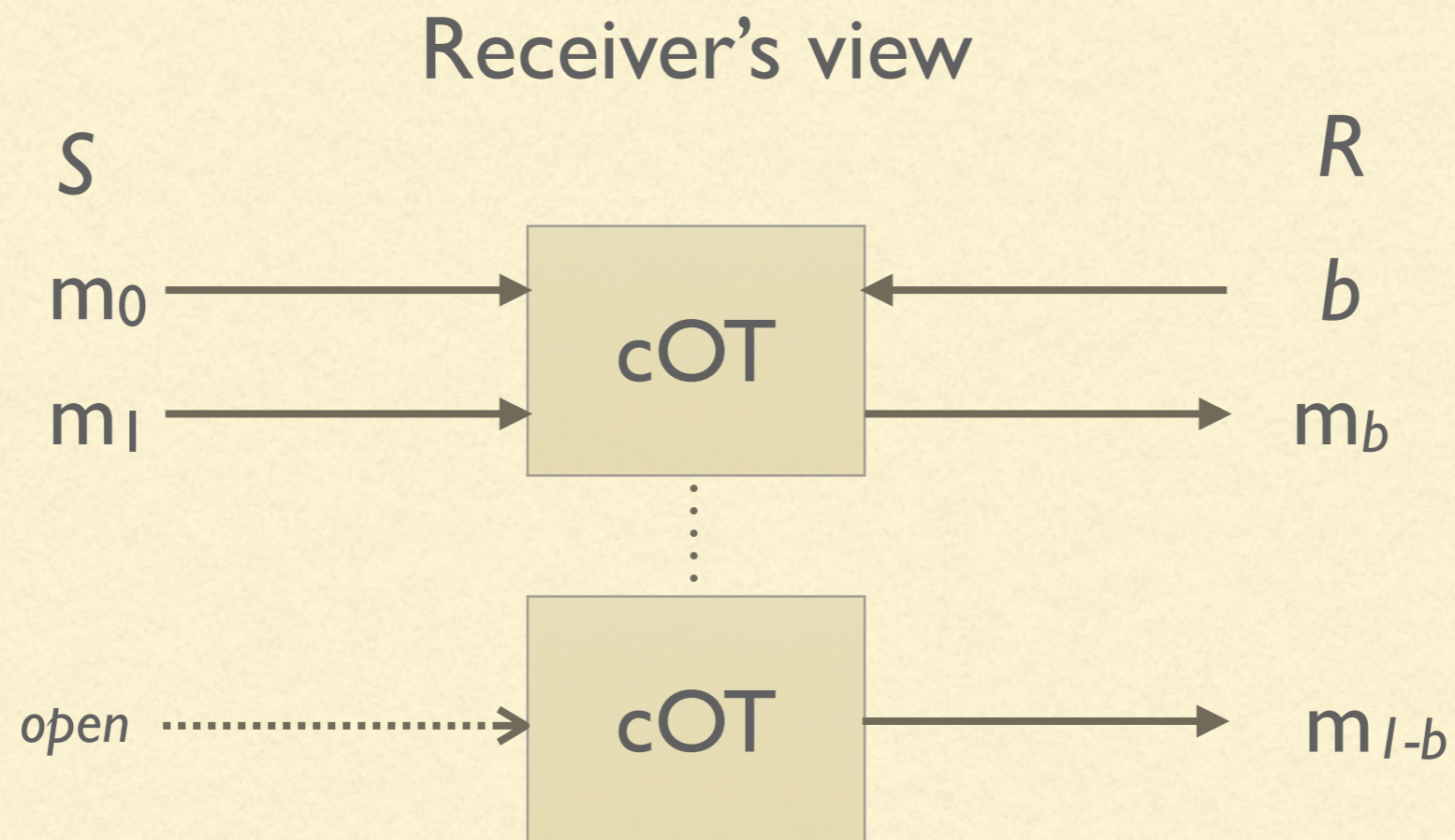
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BUILDING BLOCK: COMMITTED OBLIVIOUS TRANSFER

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ZERO-KNOWLEDGE FROM GARBLED CIRCUITS [JKO13]

- '***P***' wishes to prove knowledge of witness '*w*' for NP statement ' $x \in L$ ' to '***V***'

P

V

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$G_b(f_x, I^k)$

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X^0

X^1

$\swarrow \searrow$

e

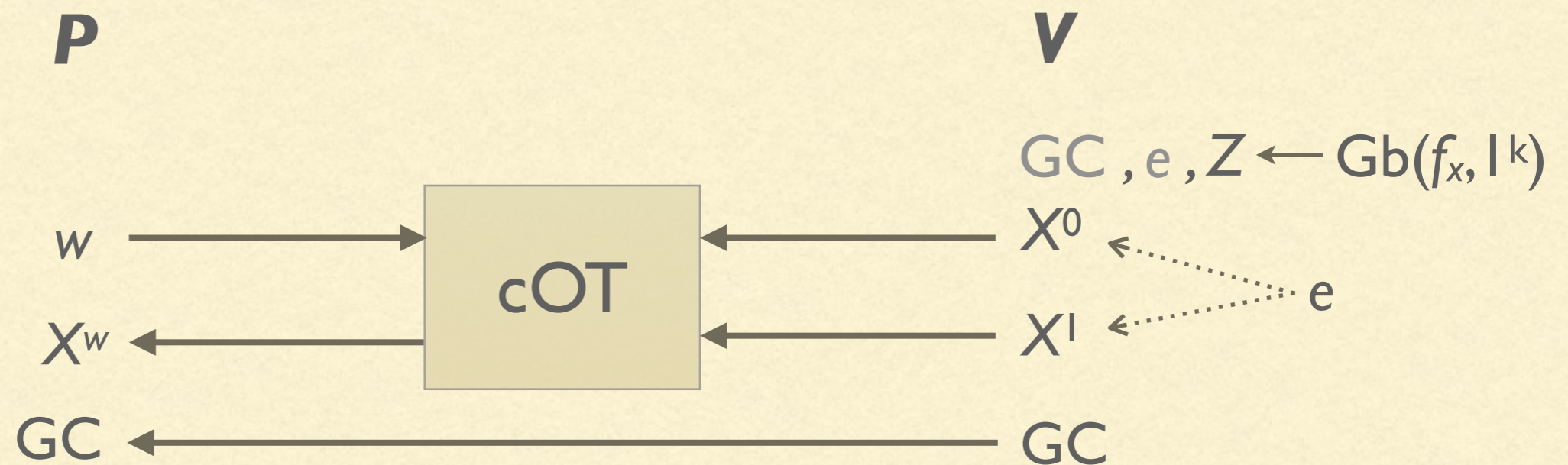
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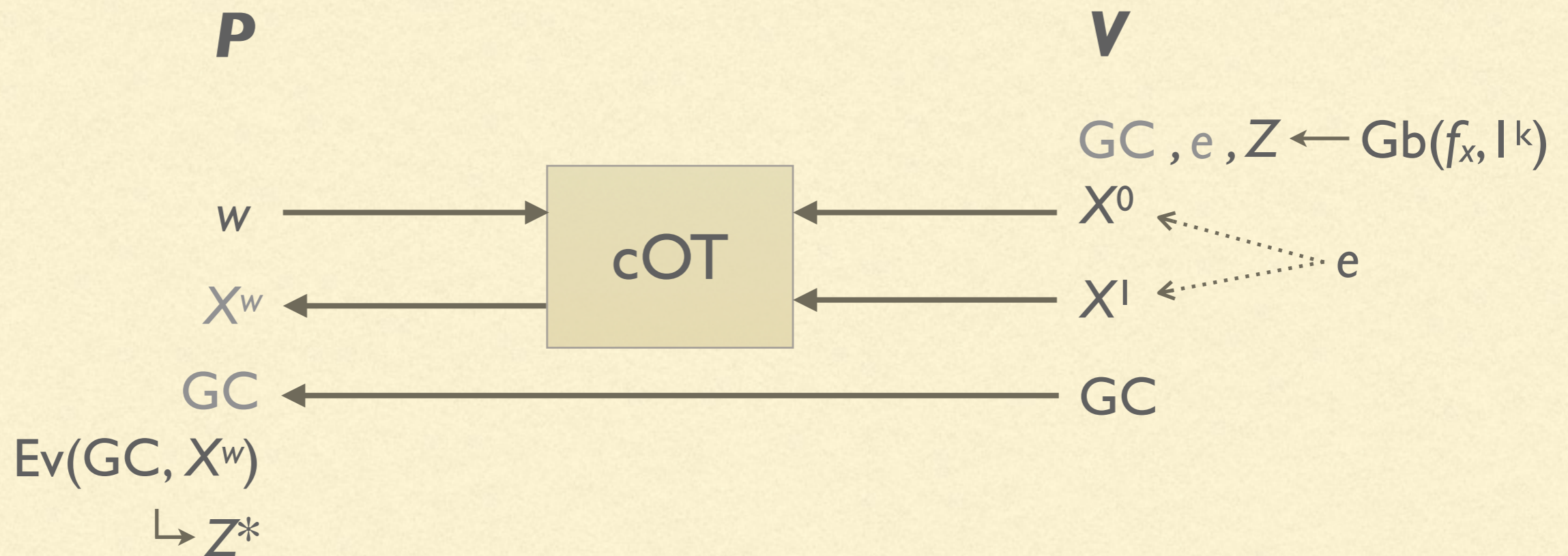
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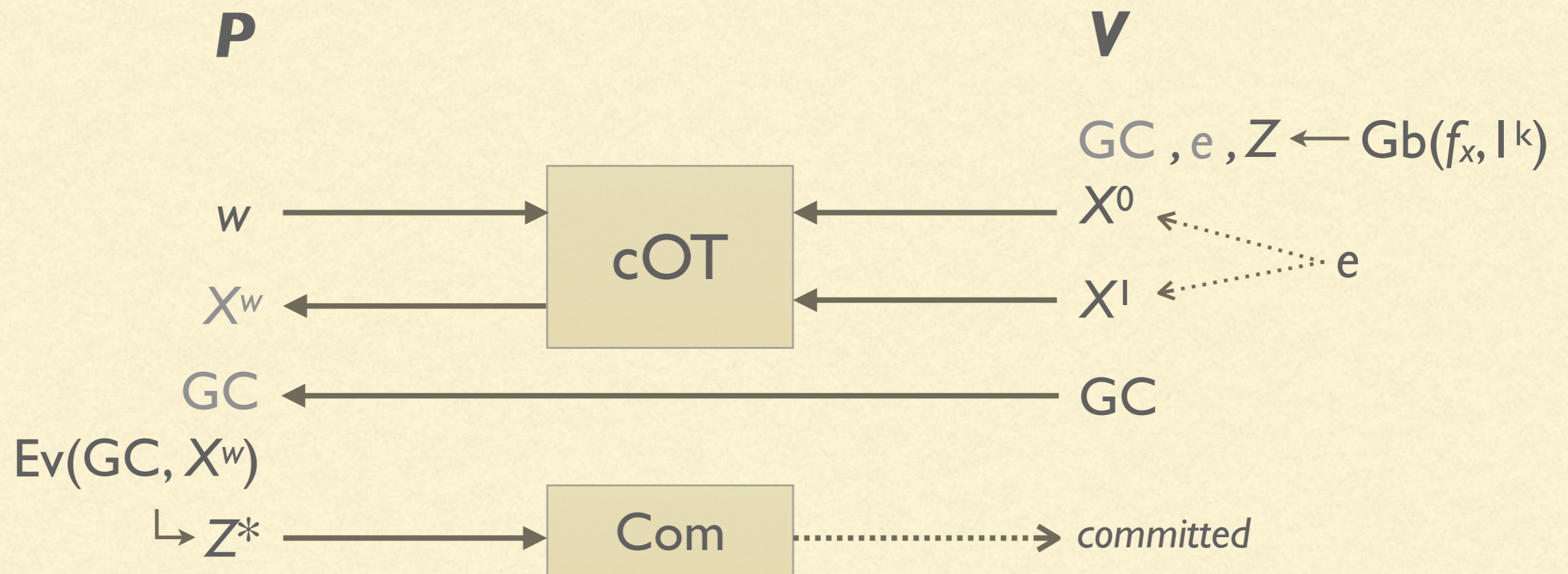
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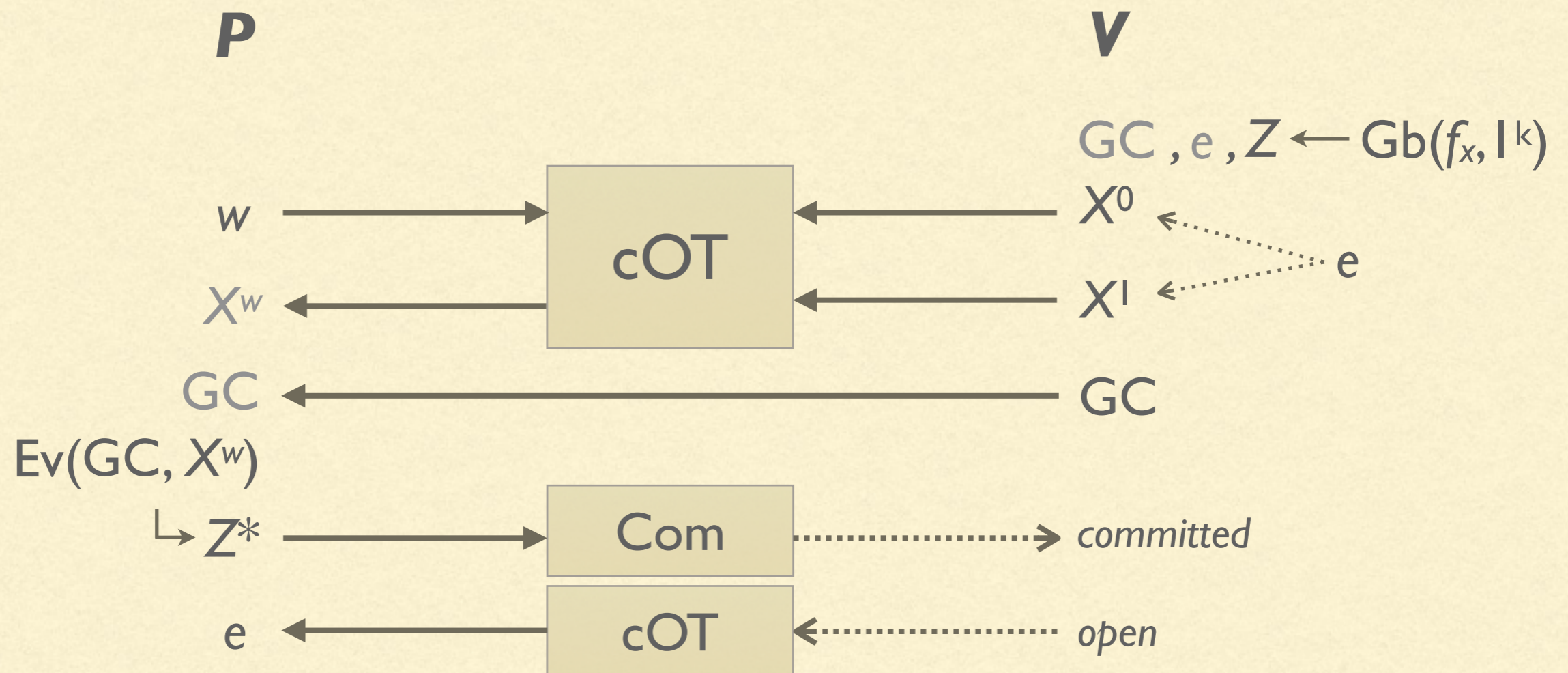
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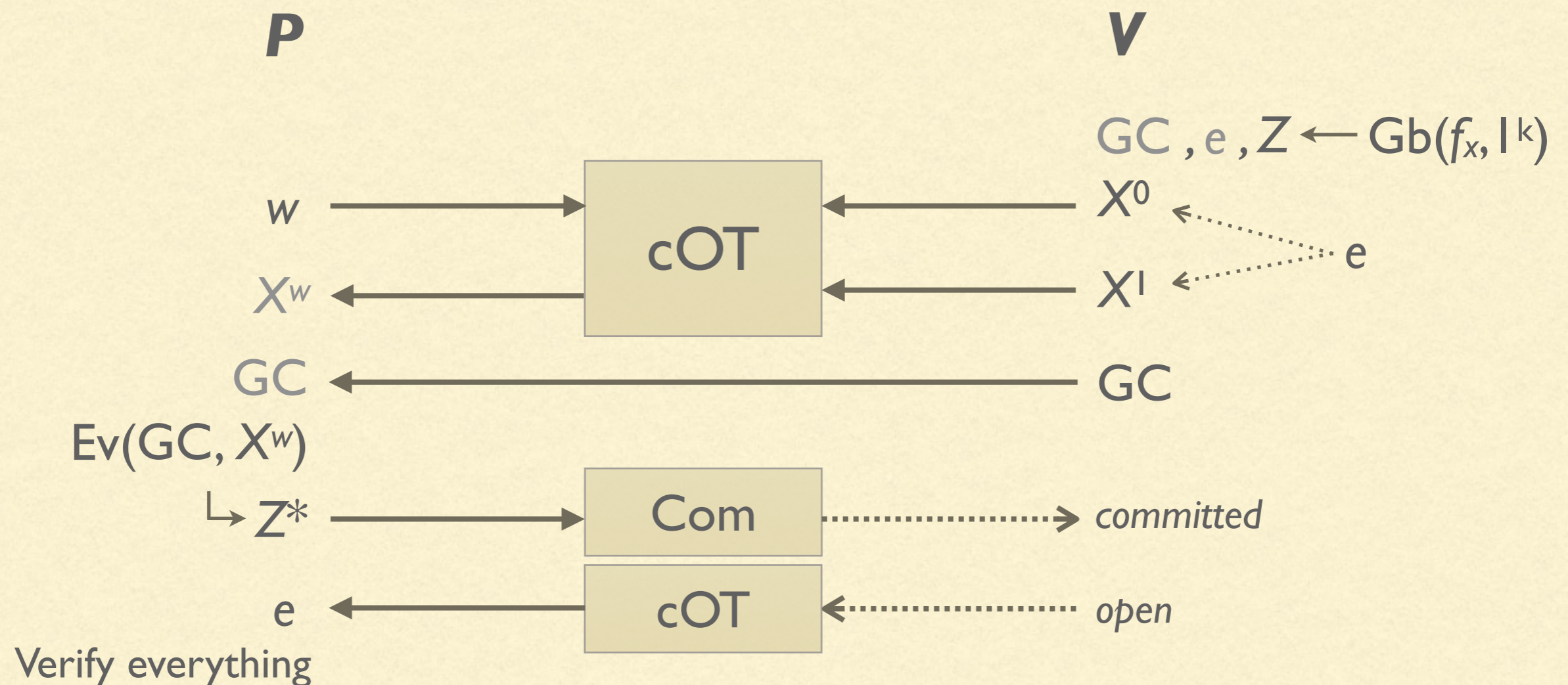
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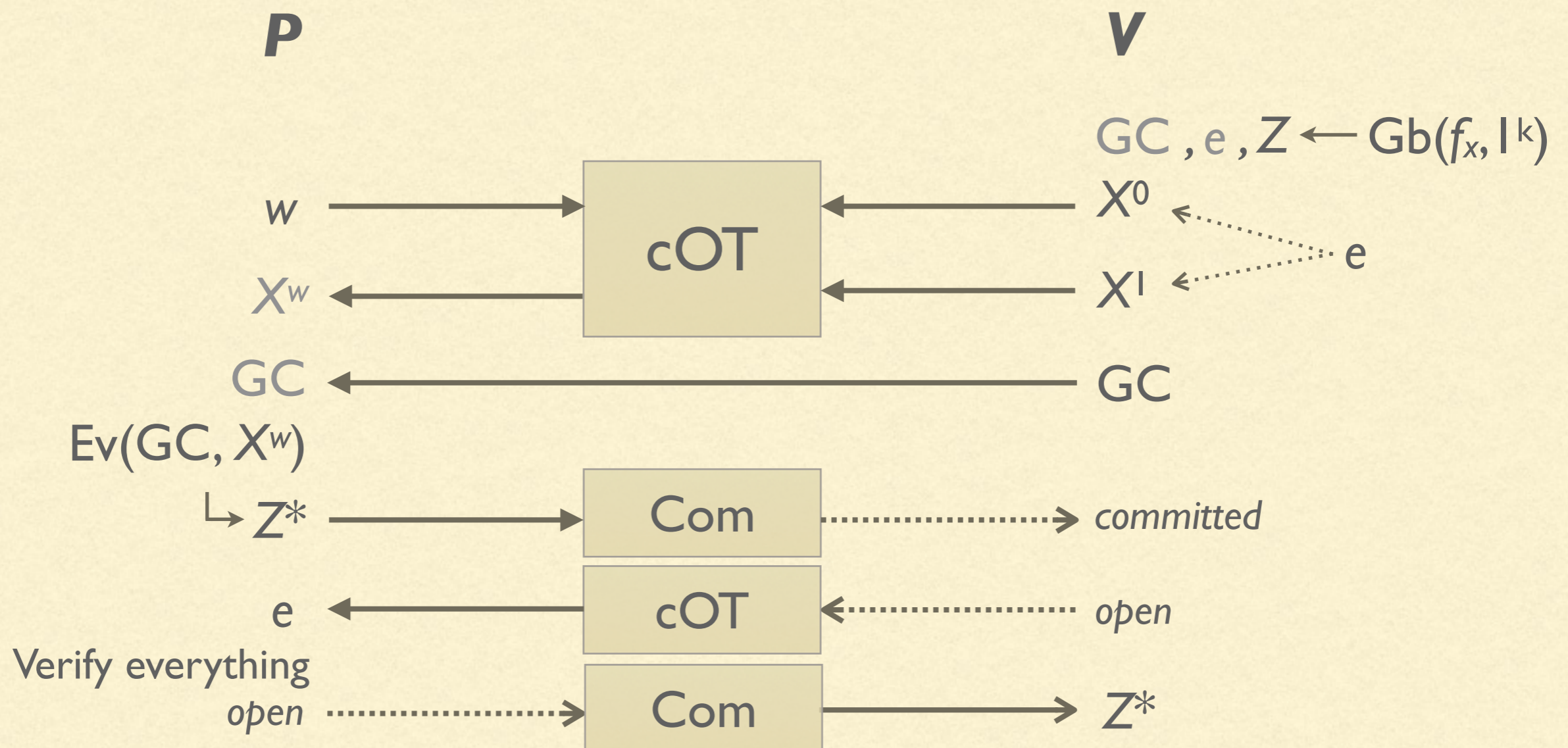
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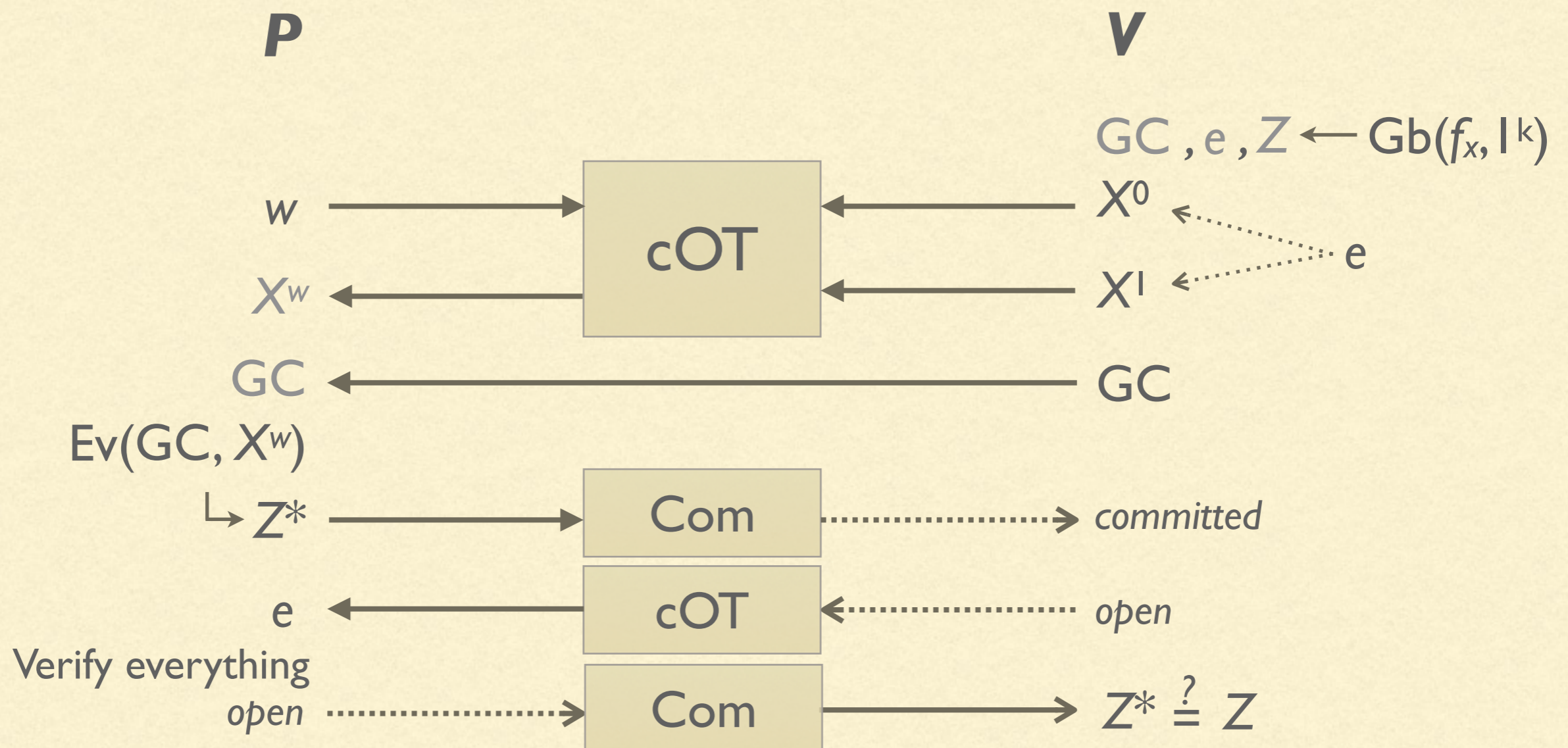
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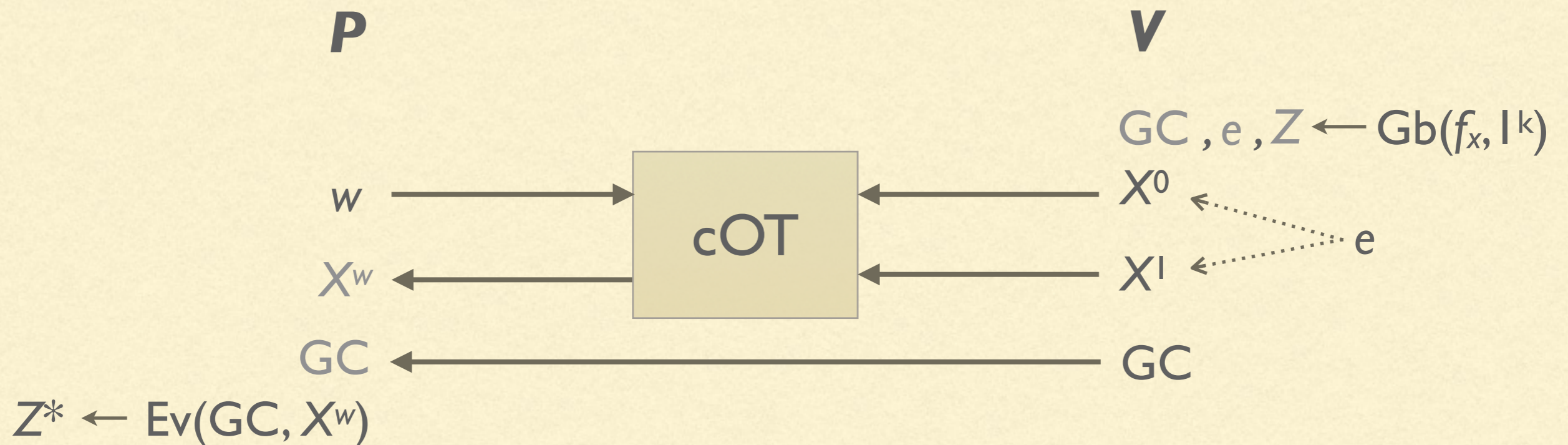
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REDUCING TO $(OT+1)$ ROUNDS

- ***P***'s verification phase made non-interactive (still not adaptive)

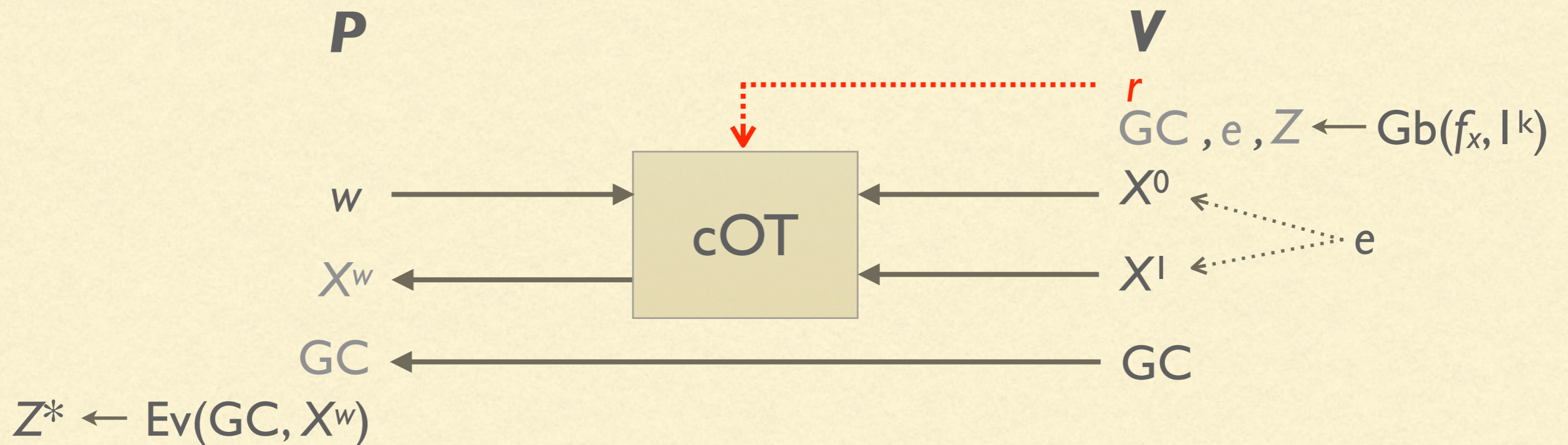


Verify everything

$$Z^* \stackrel{?}{=} Z$$

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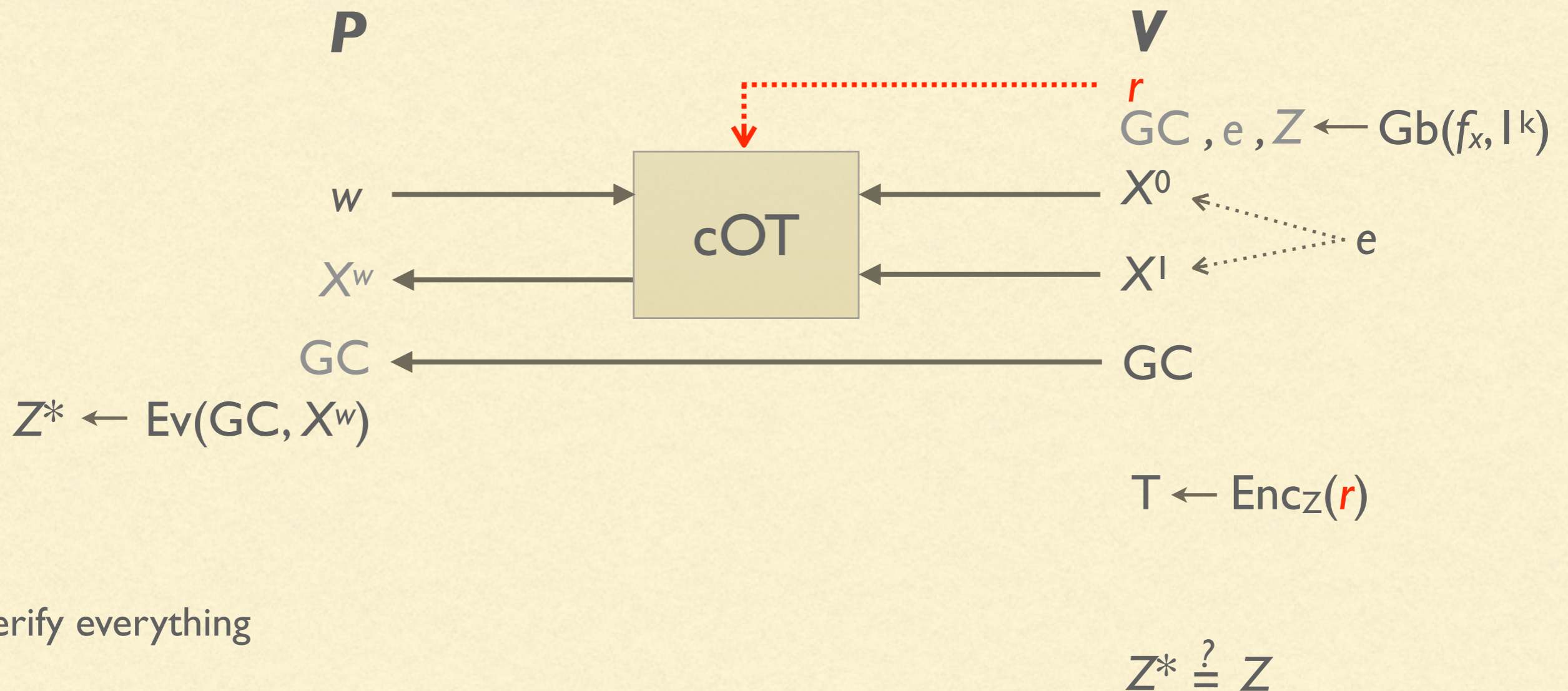


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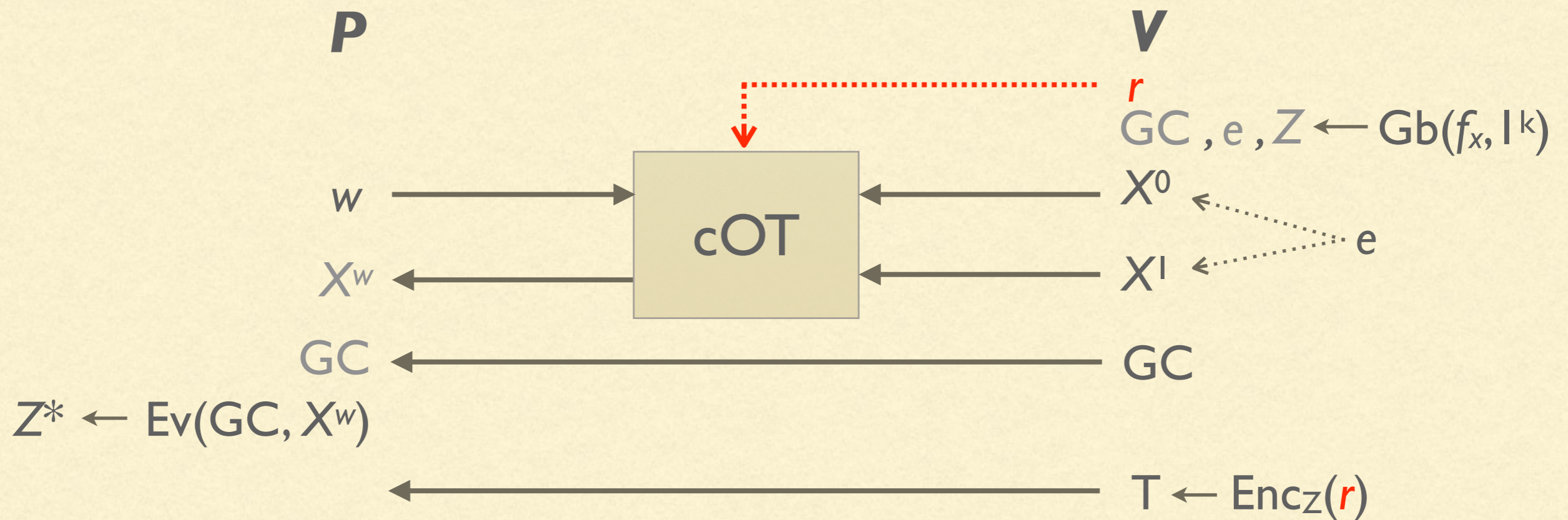
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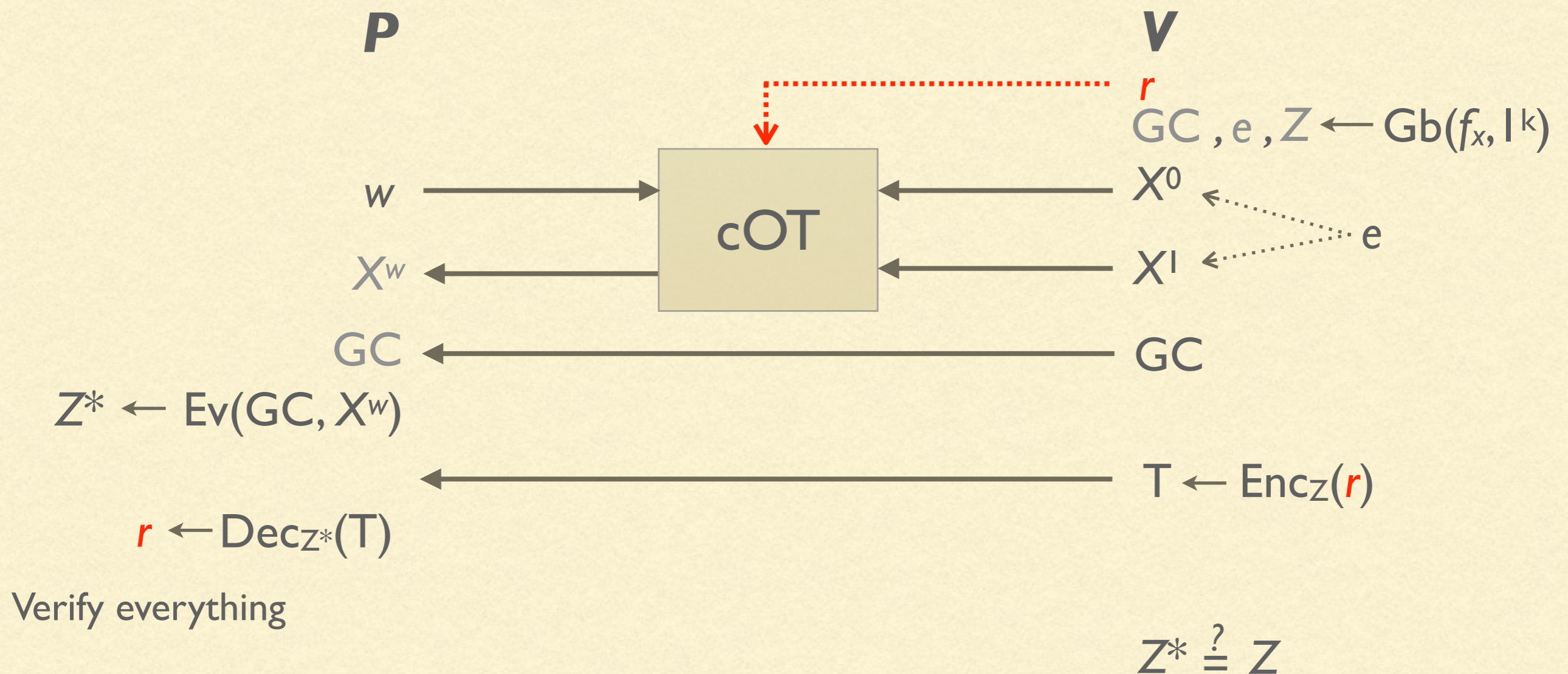


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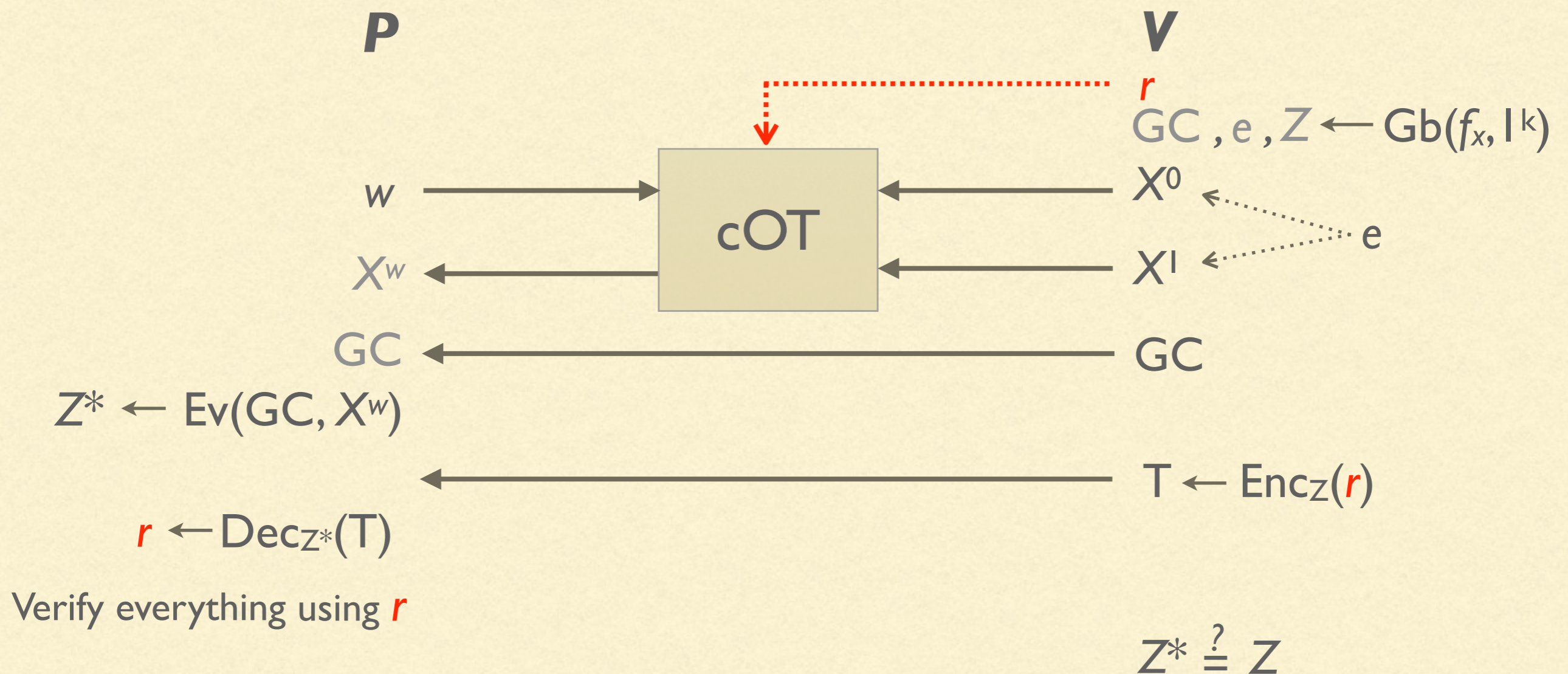
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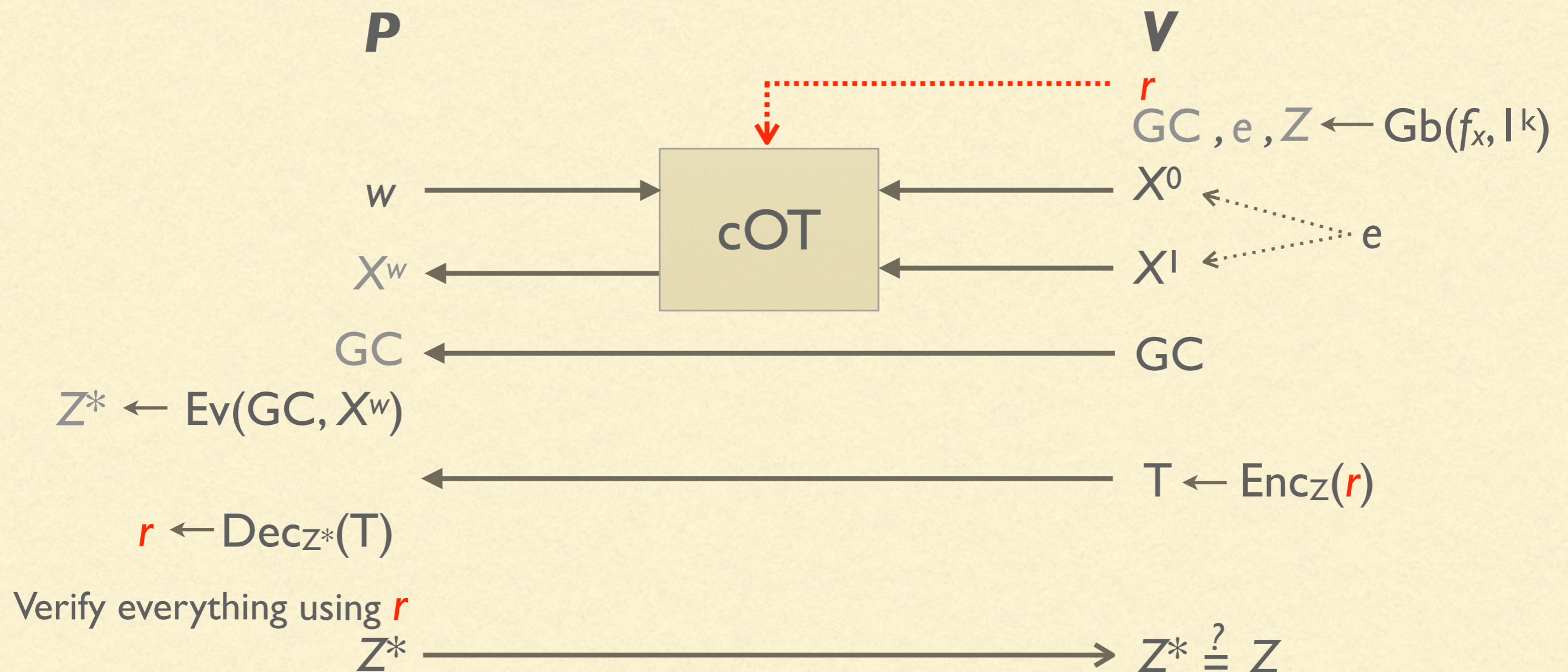
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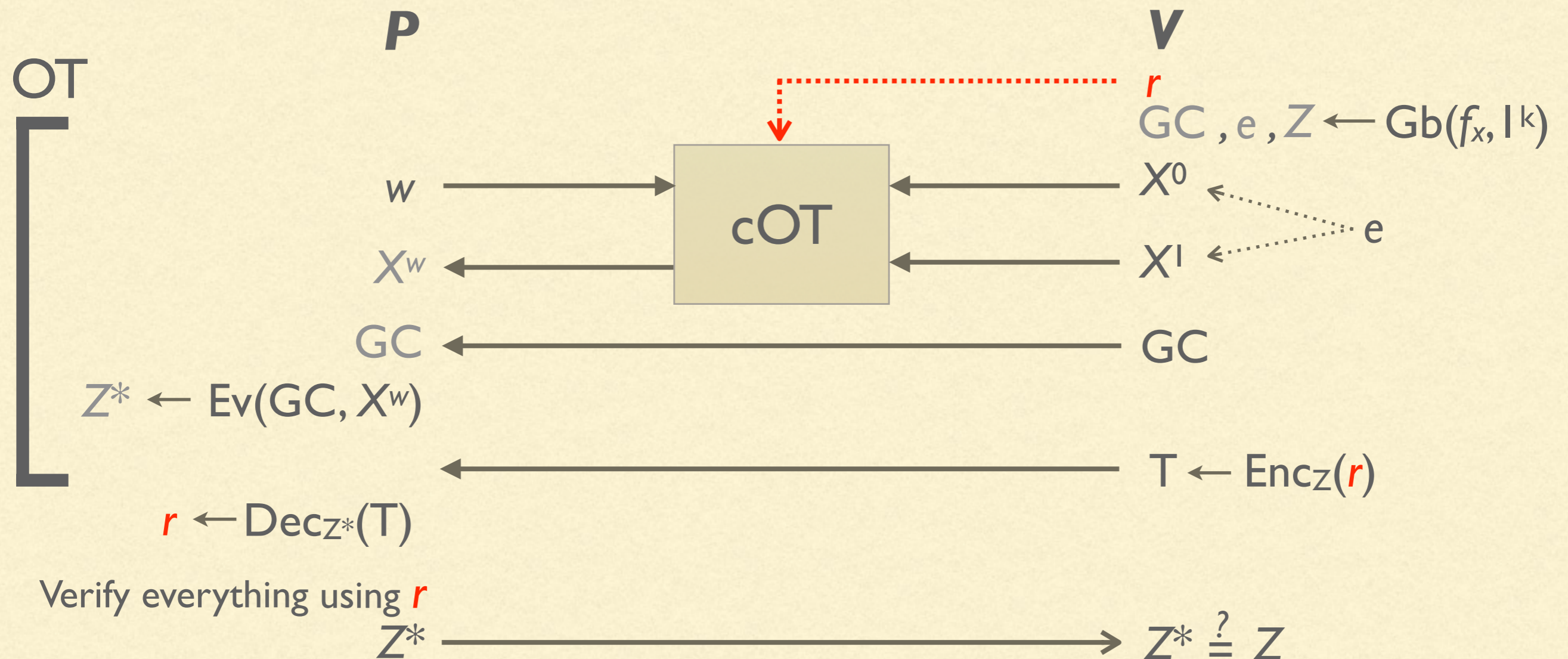
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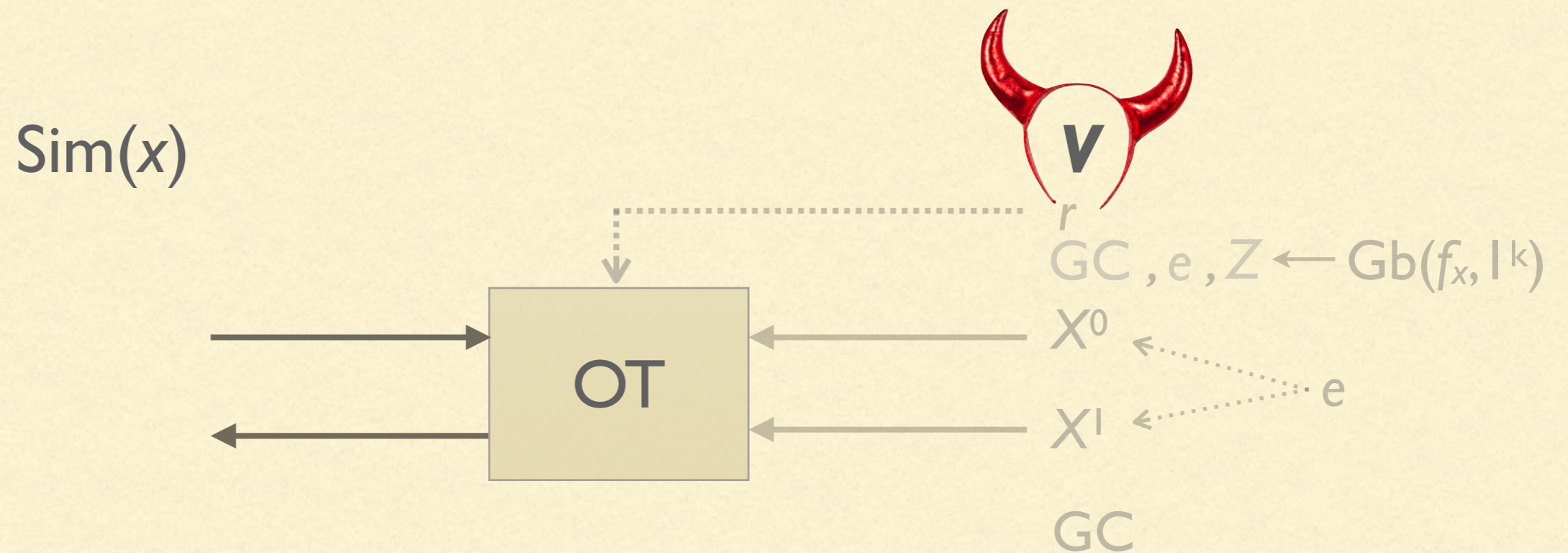
REDUCING TO $(OT+1)$ ROUNDS

- Encryption scheme has to be “committing”
 - Circular security and observability of decryption key: solved by random oracle (non-programmable)
 - Still simulatable; less work for prover, verifier is the same
-

ADAPTIVE SECURITY

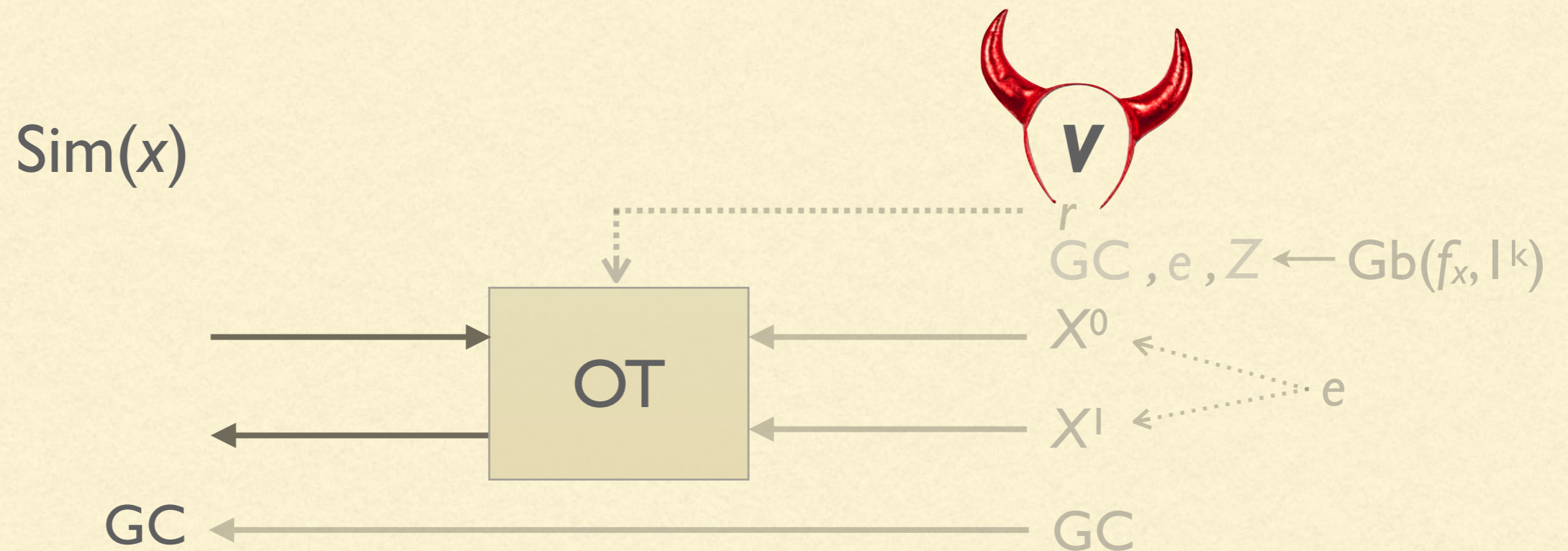
- Many cases of corruption order to consider
 - Hardest case is when Verifier is initially corrupted, and Prover is corrupted post-execution. We focus on this case.
 - For simplicity, we focus on adaptivity of OT+I version
-

HARDEST CASE: **V**, **P**



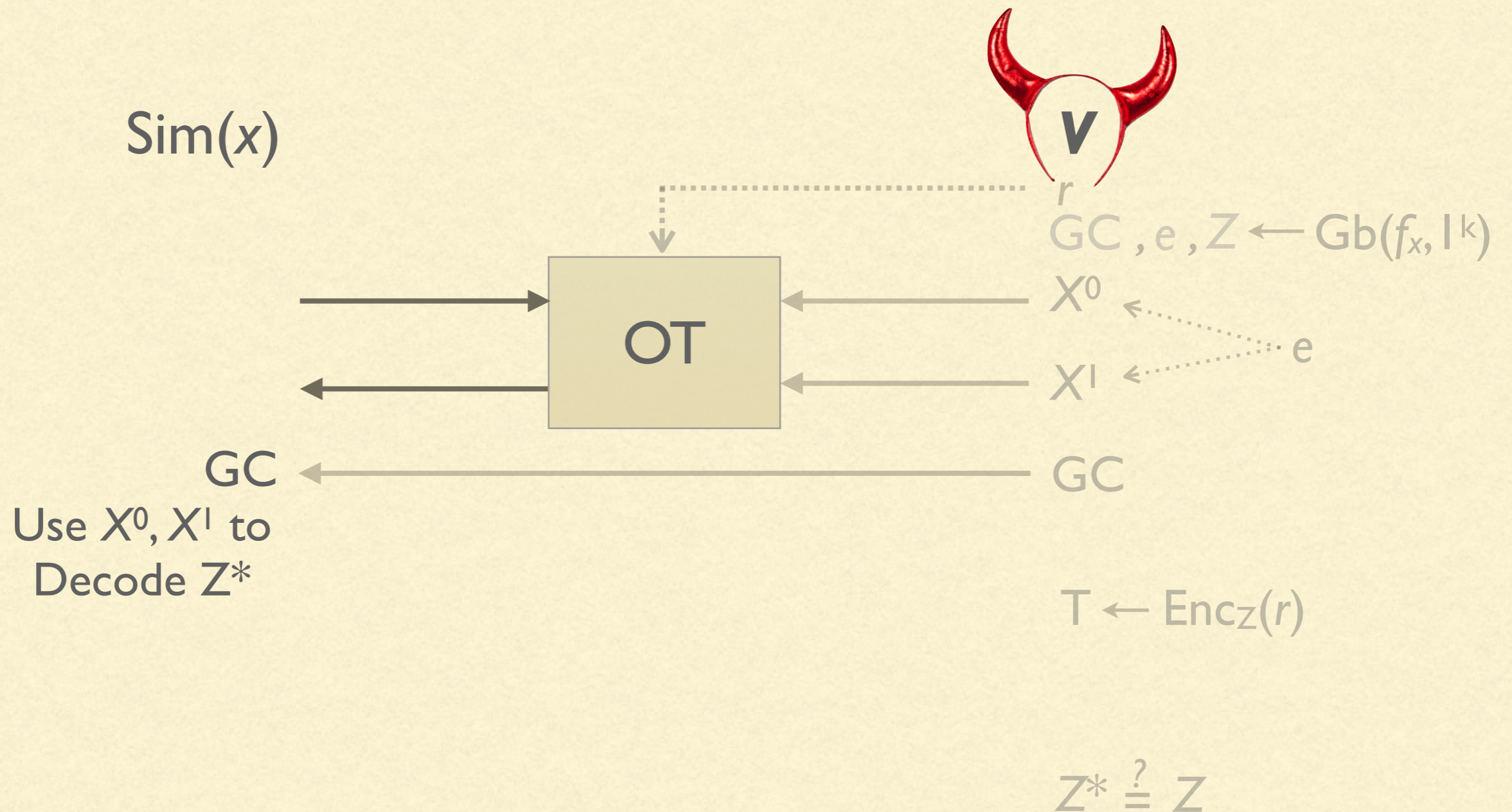
As with [JKO13], simulator extracts X^0, X^1 from OT.

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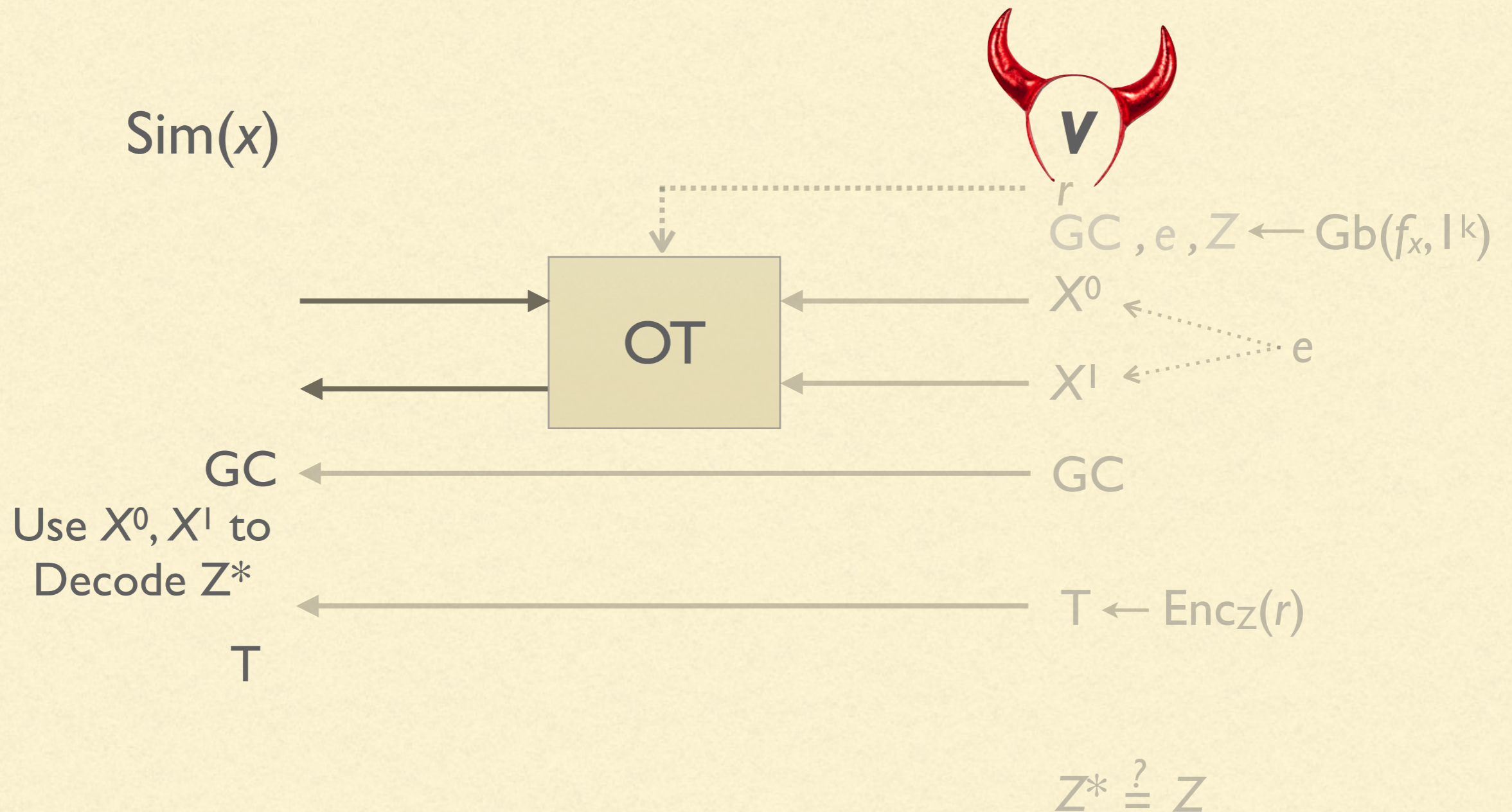


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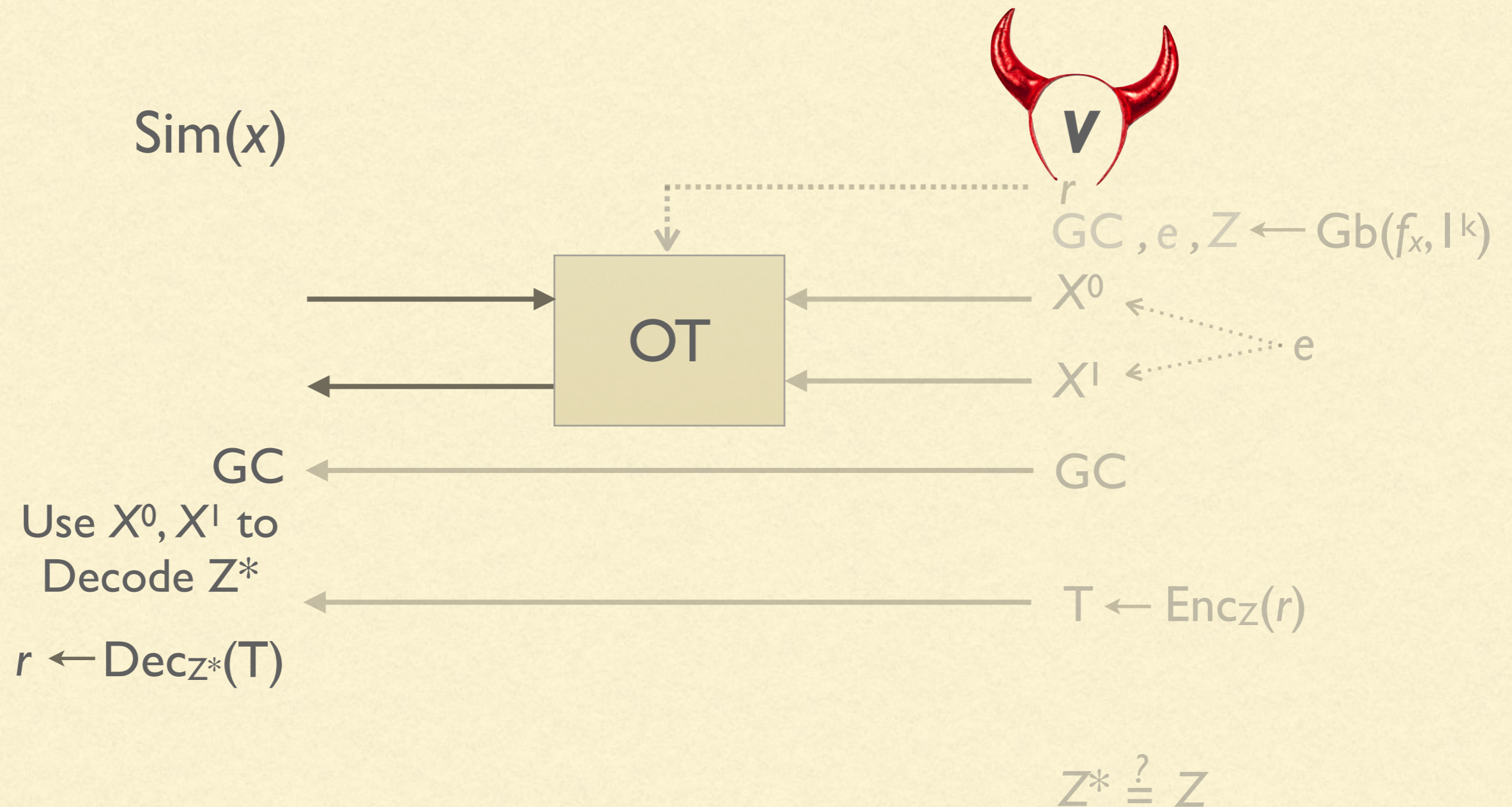
HARDEST CASE: , P



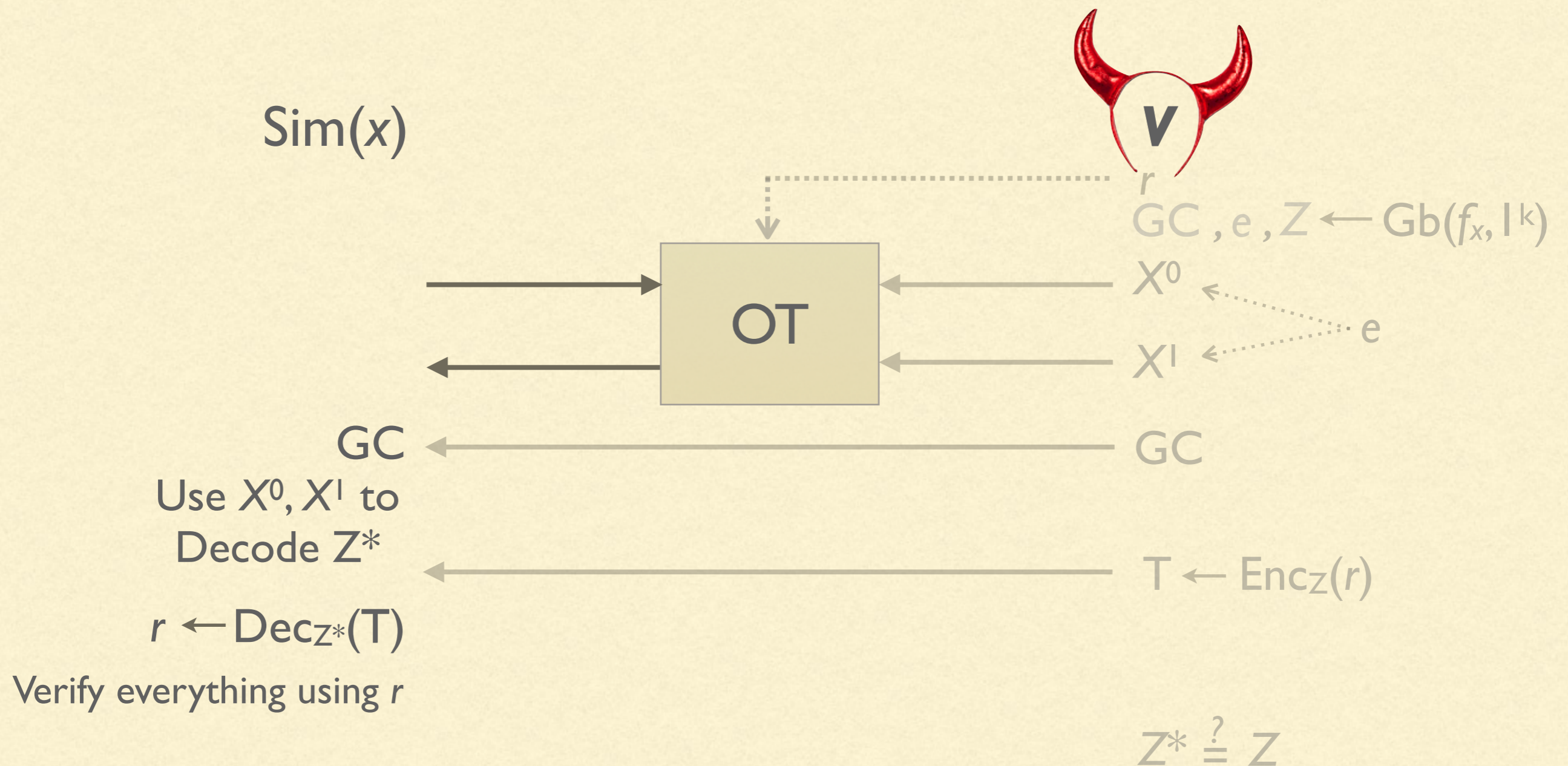
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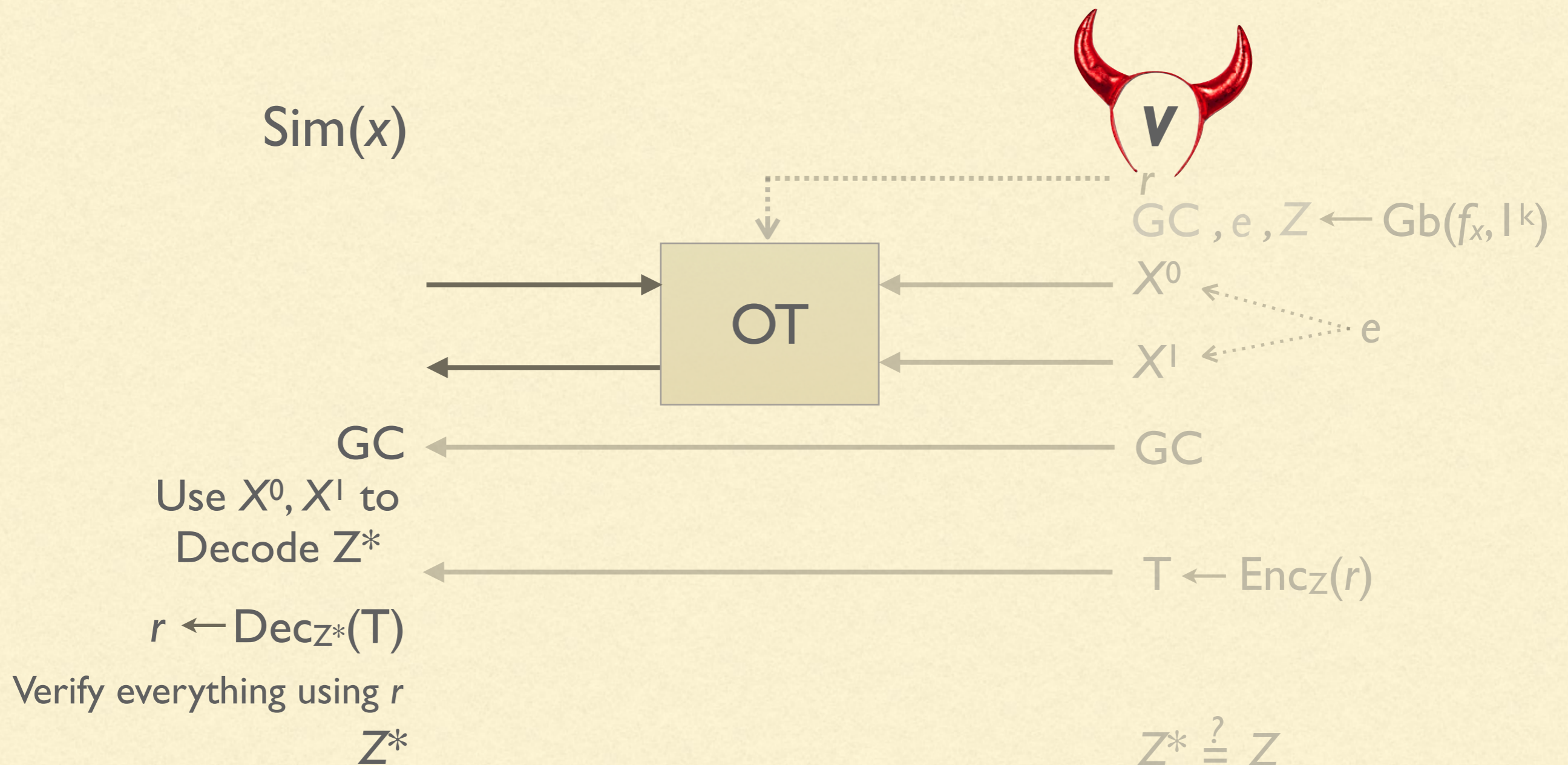
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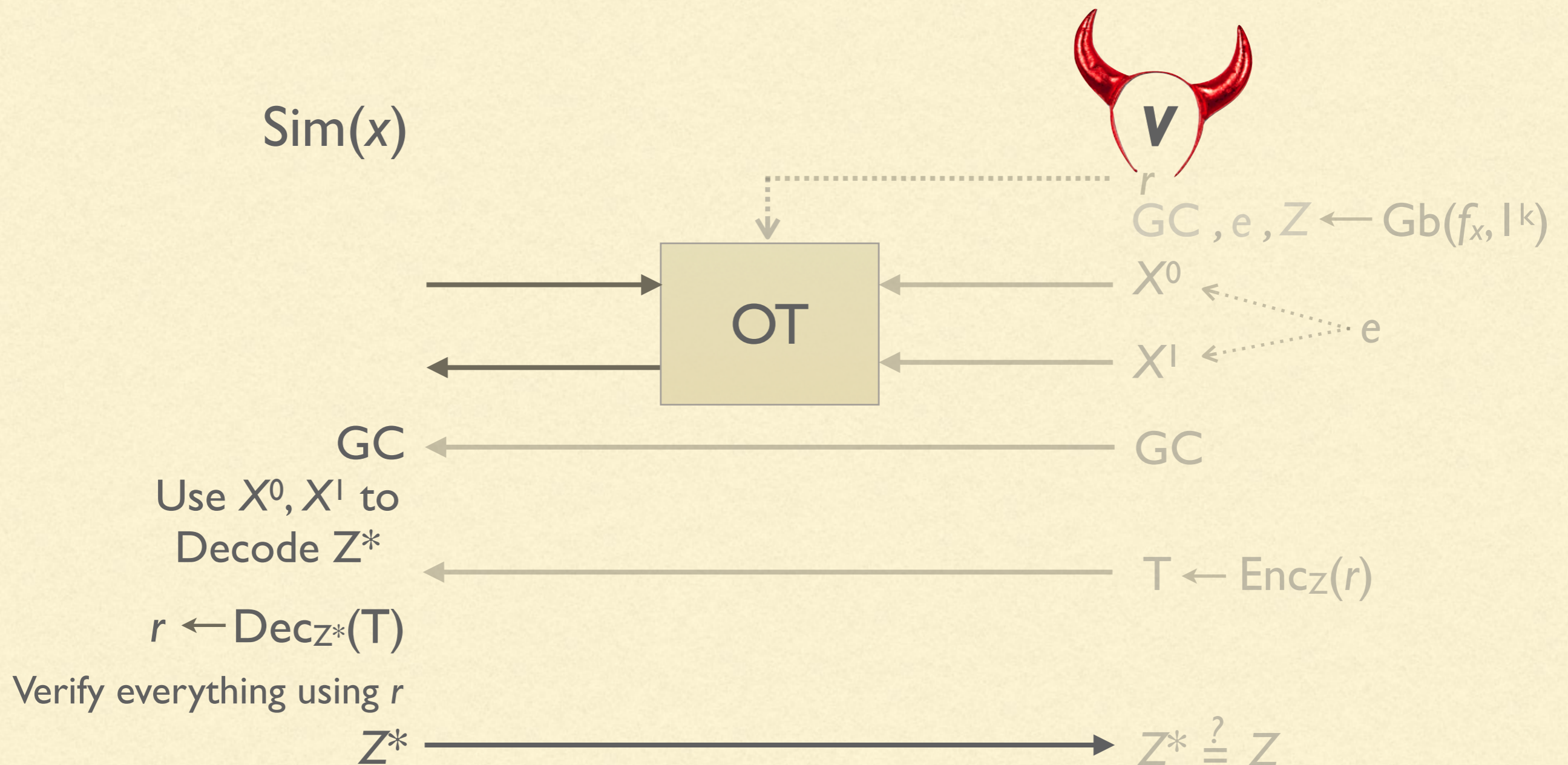
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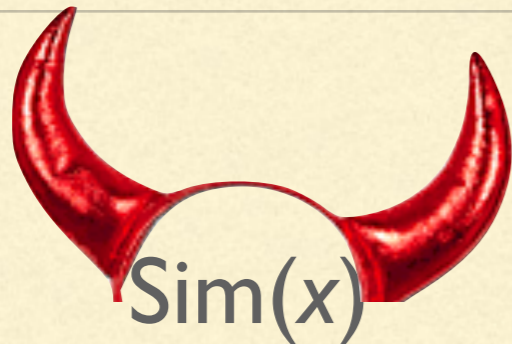
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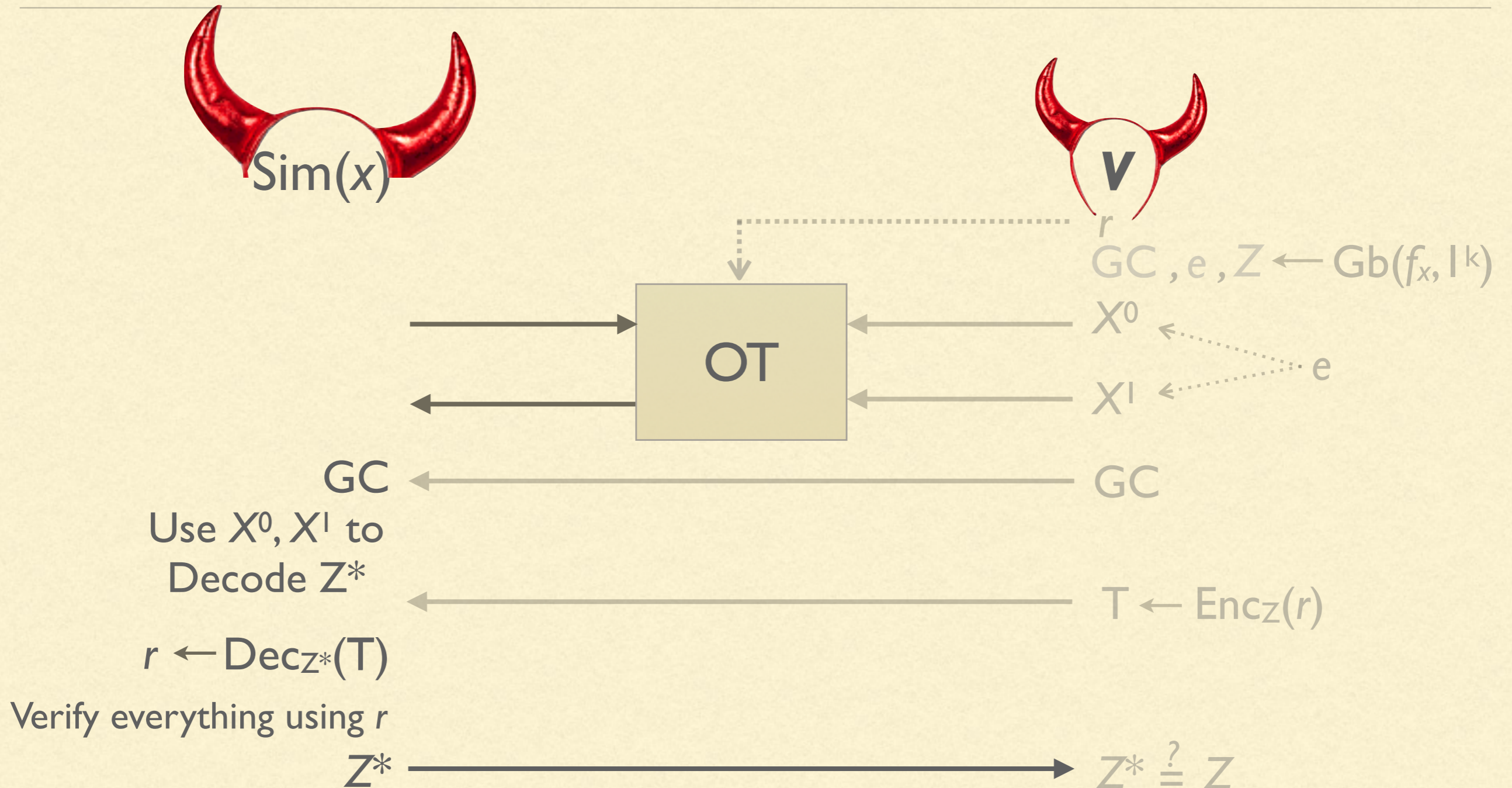


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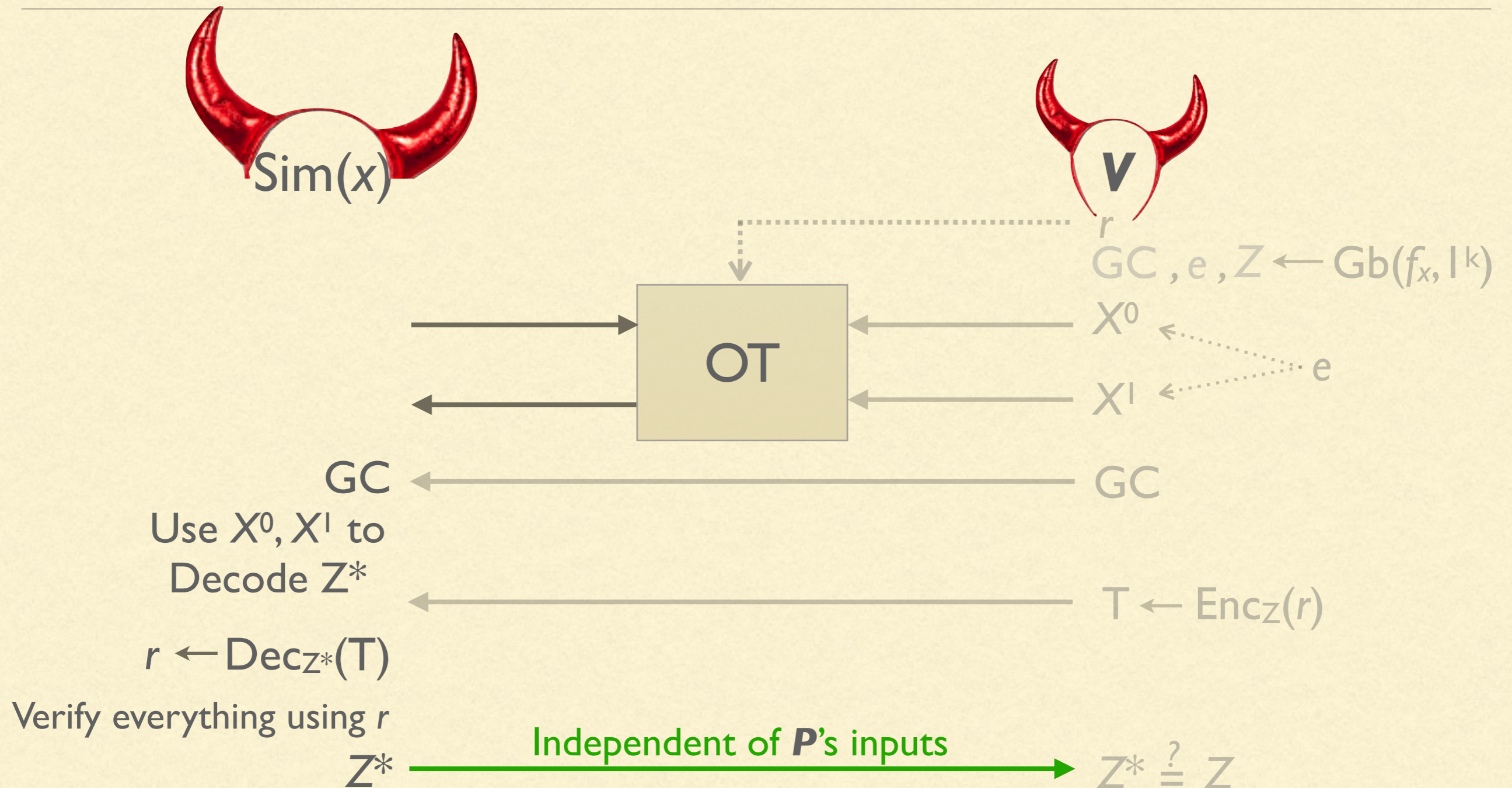


HARDEST CASE:


 $\text{Sim}(x)$



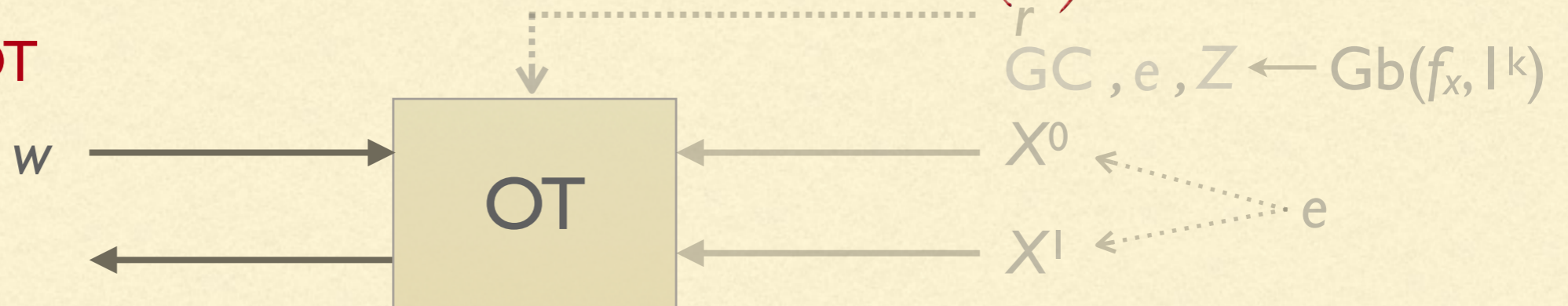
HARDEST CASE:



HARDEST CASE:

 $\text{Sim}(x)$

Need to explain OT



GC

Use X^0, X^1 to
Decode Z^*

$r \leftarrow \text{Dec}_{Z^*}(T)$

Verify everything using r

Z^*

Independent of **P**'s inputs

 **V**

$GC, e, Z \leftarrow Gb(f_x, l^k)$

$X^0 \leftarrow e$

$X^1 \leftarrow e$

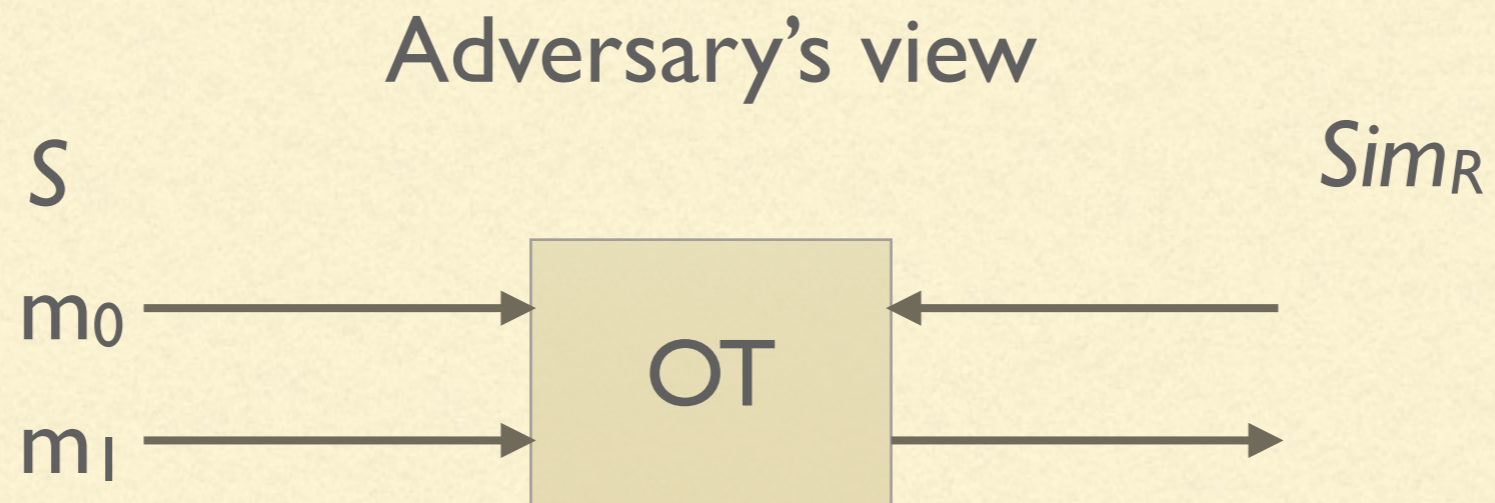
GC

$T \leftarrow \text{Enc}_Z(r)$

$Z^* \stackrel{?}{=} Z$

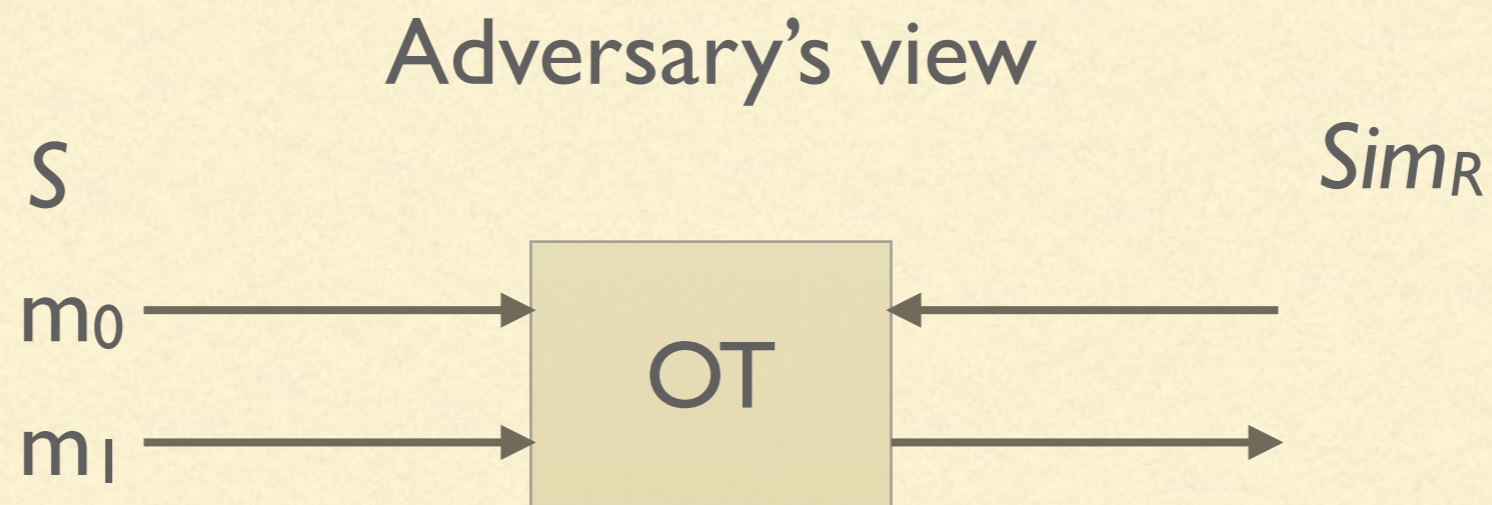
RECEIVER EQUIVOCAL OT

- Notion introduced in [Beaver 96]



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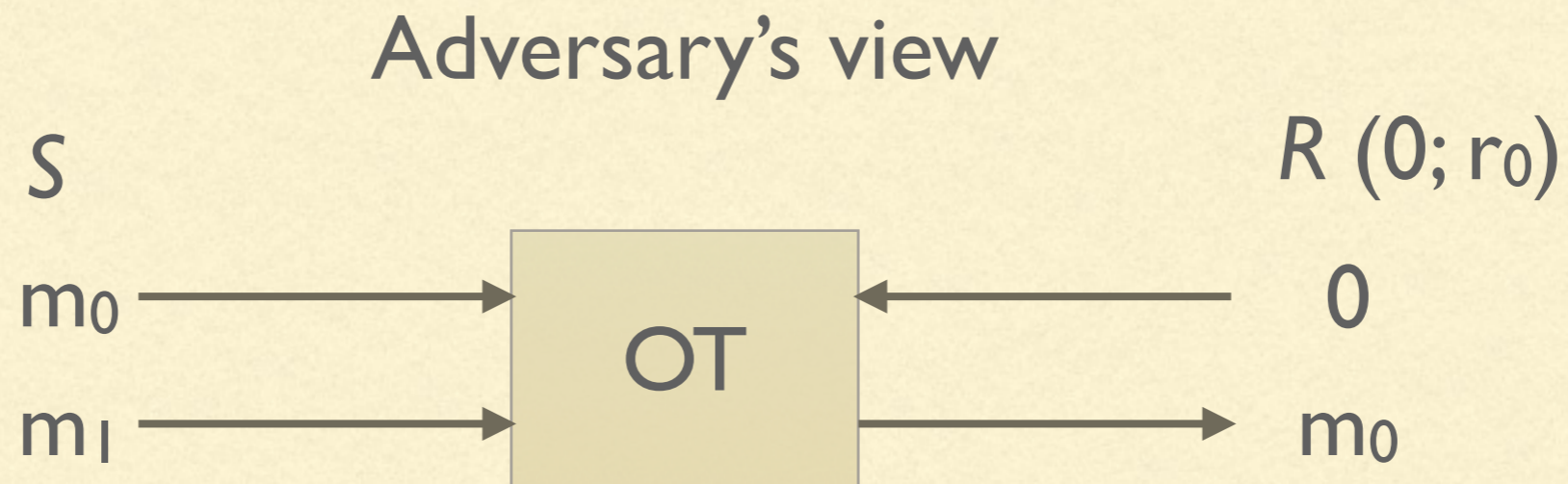
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- Sim_R is able to produce r_0 and r_1
-

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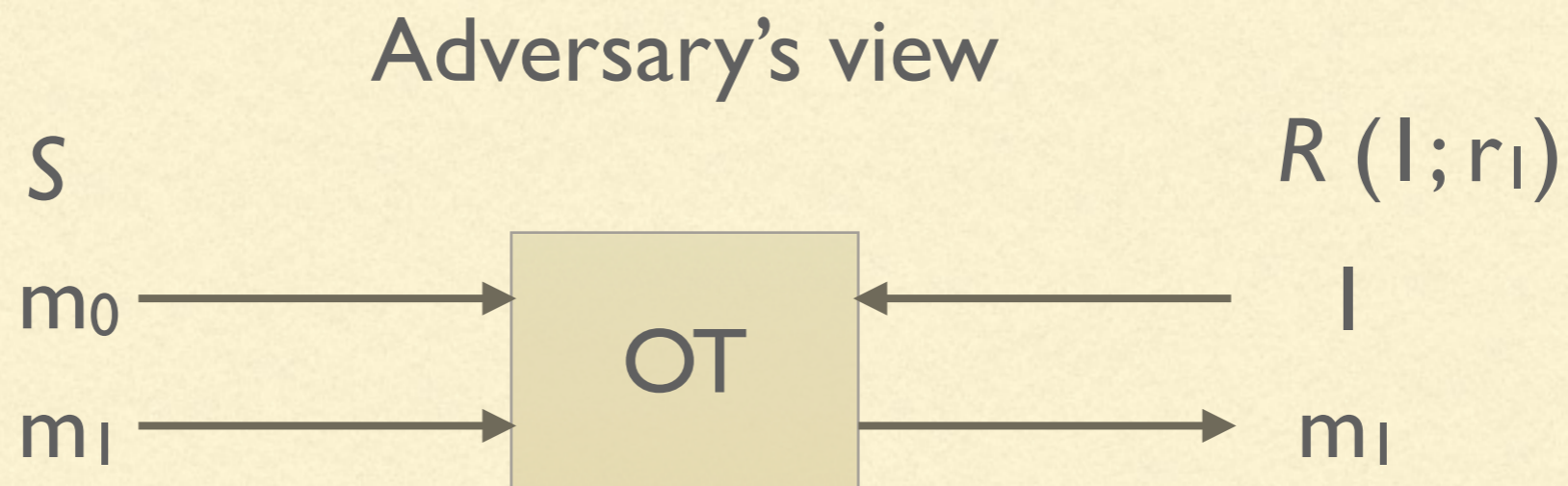
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- The OT framework of [Peikert-Vaikuntanathan-Waters 08] satisfies one-sided adaptivity (but not full adaptivity)

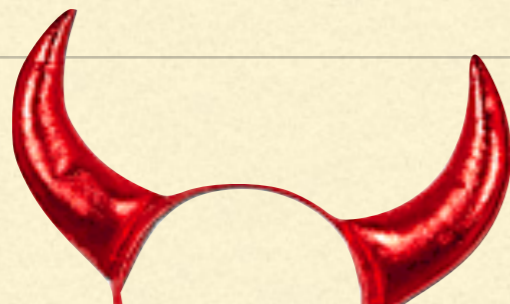
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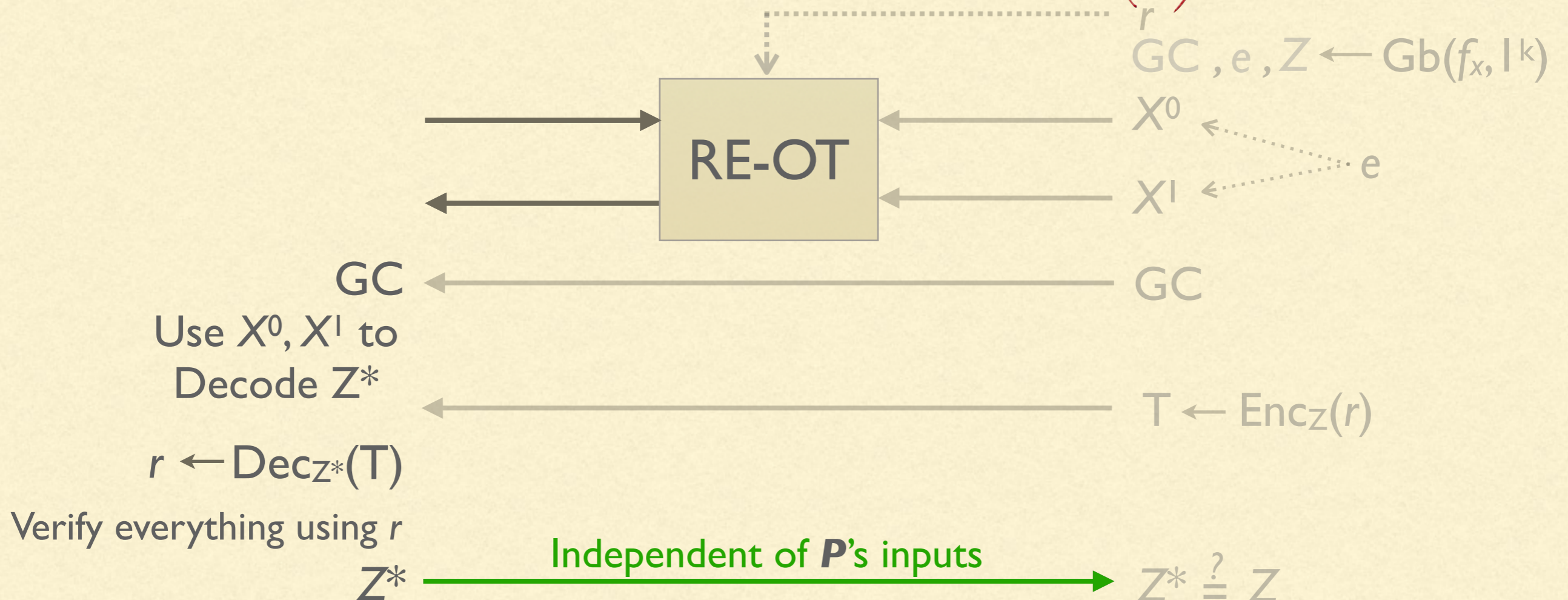
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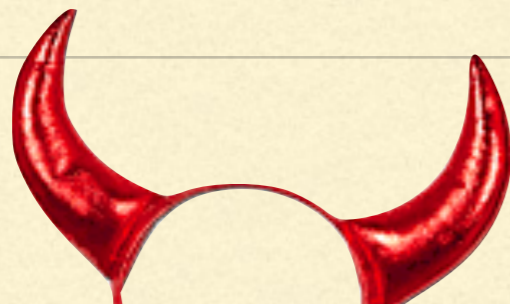
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 - UC-secure with local CRS as trusted setup
-

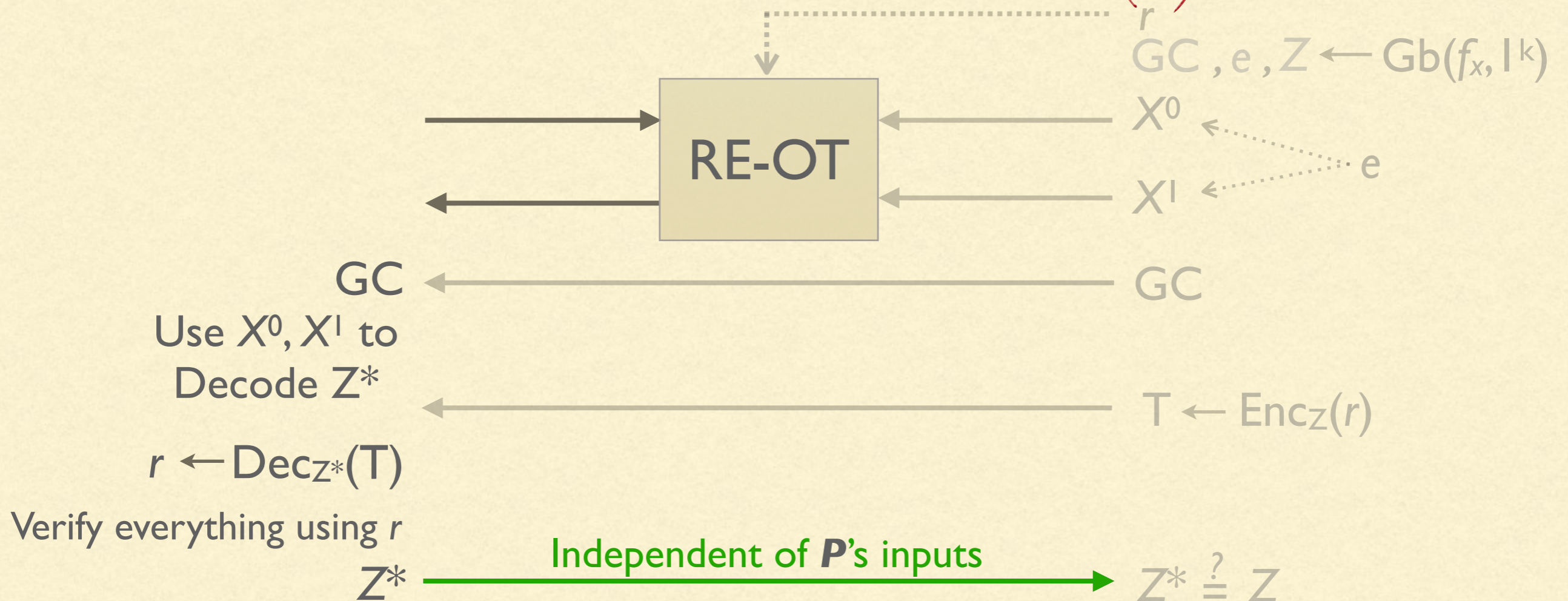
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 $\text{Sim}(x, w):$

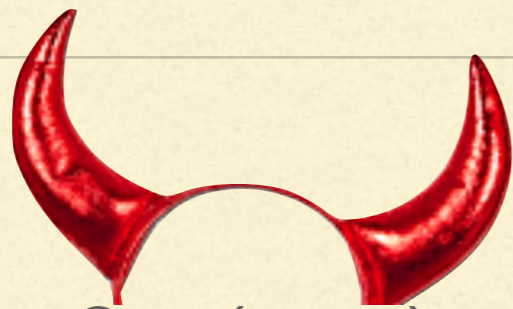


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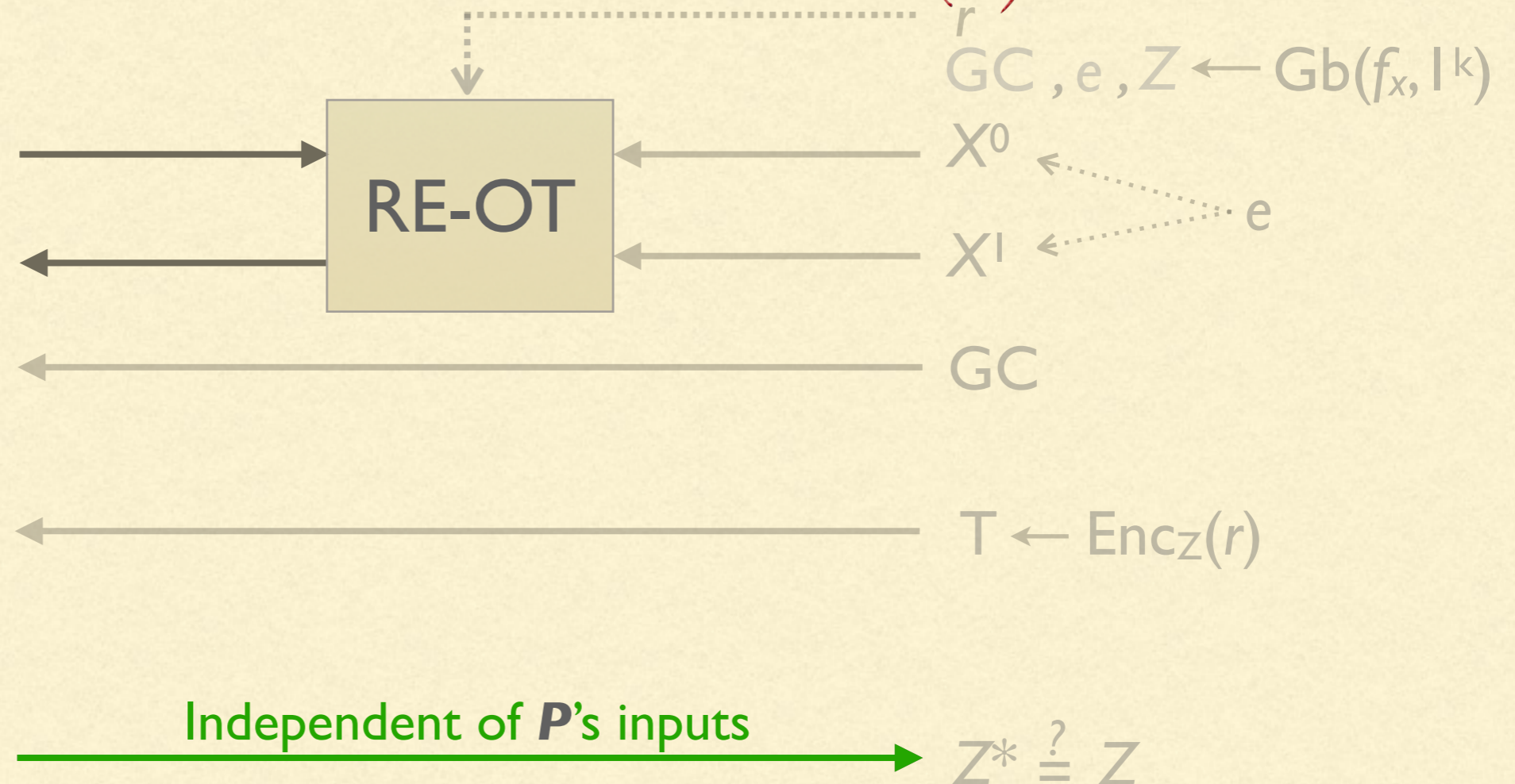

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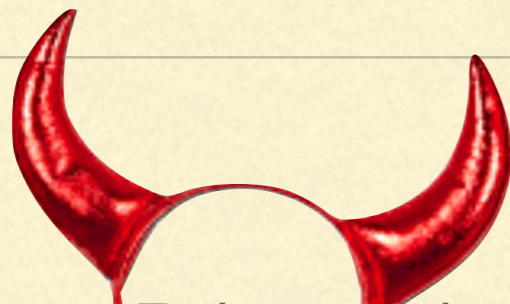
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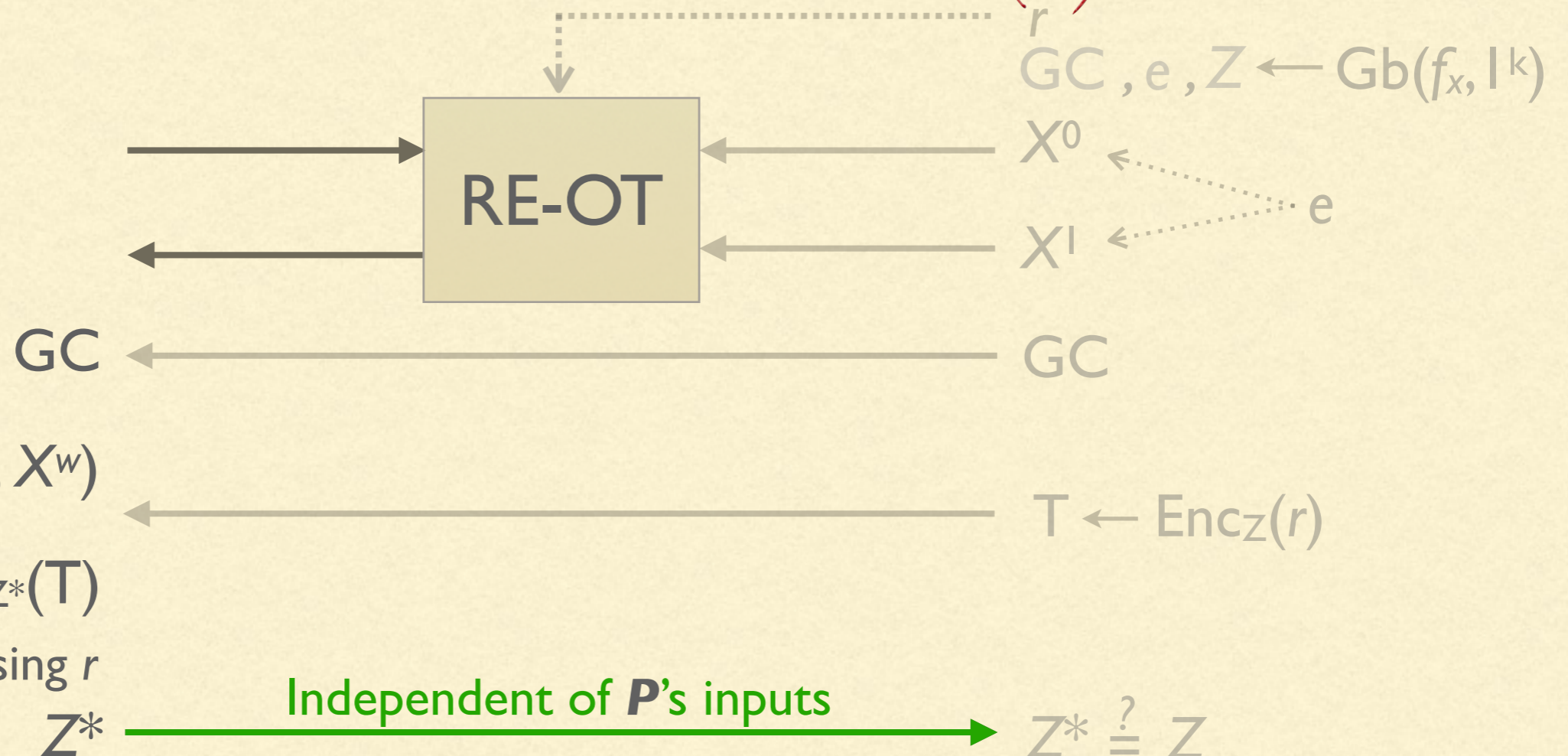


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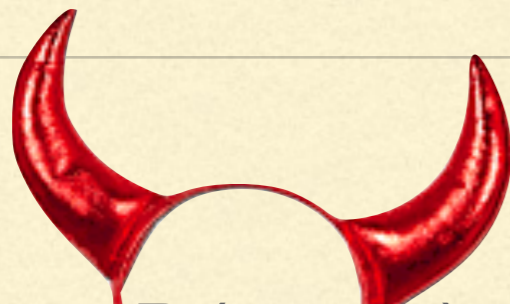


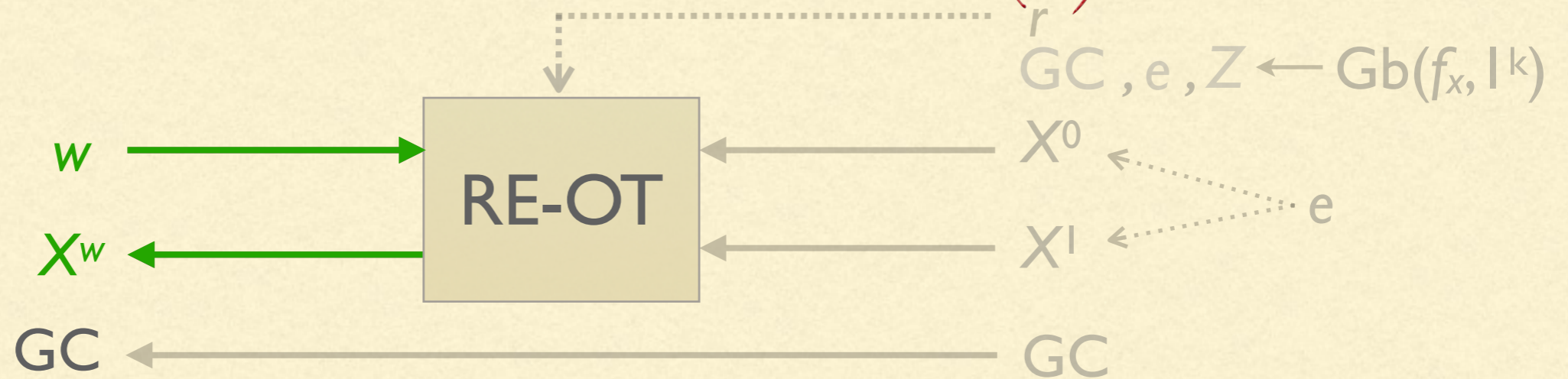
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$Z^* \leftarrow Ev(GC, X^w)$

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 - Also in paper: 2-round ZK proofs from GCs (cut and choose), authenticity-free garbling
-

THANK YOU
