

# Proactive Threshold Wallets With Offline Devices

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Northeastern  
University



AARHUS  
UNIVERSITY

**Kzen**

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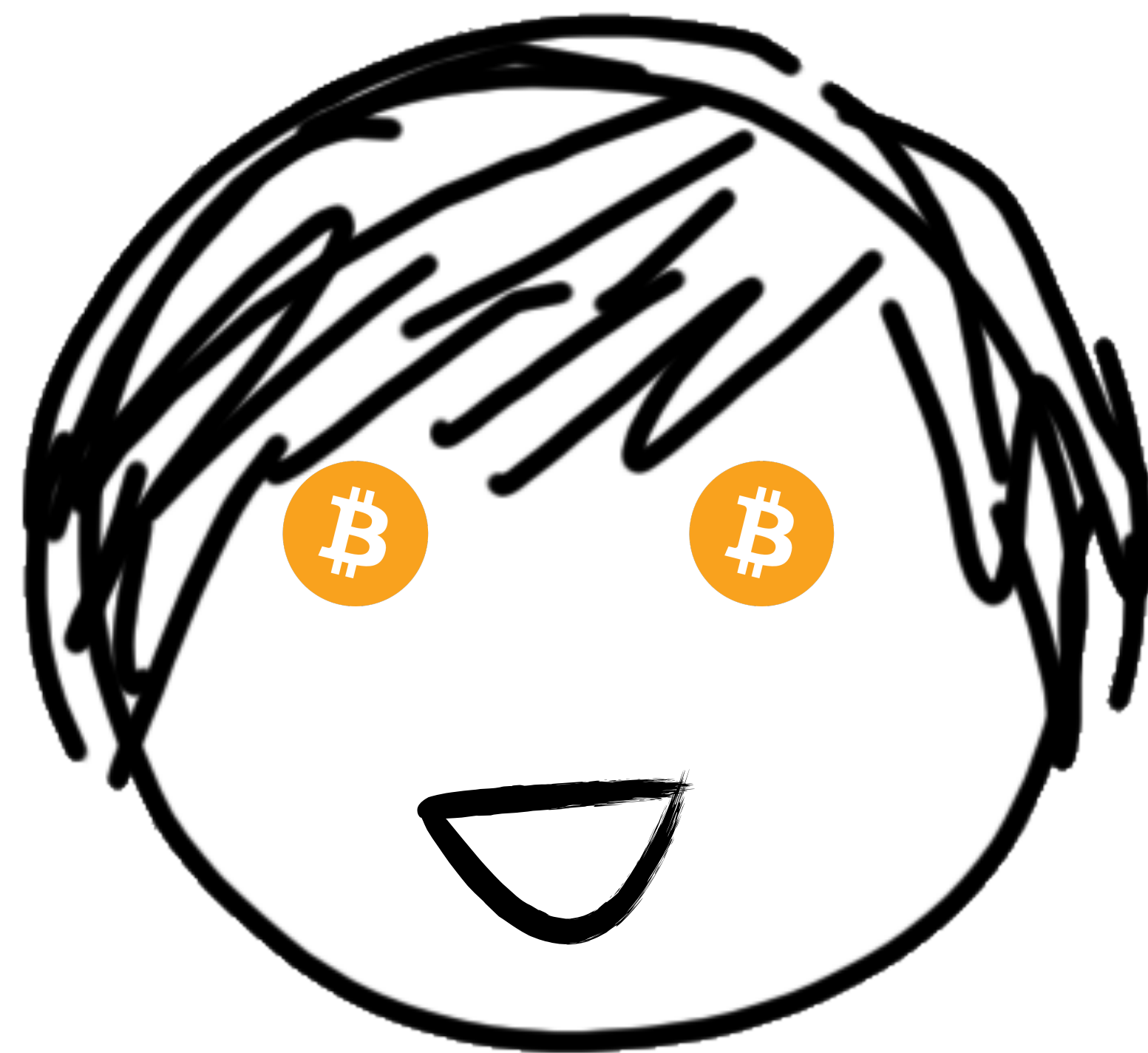
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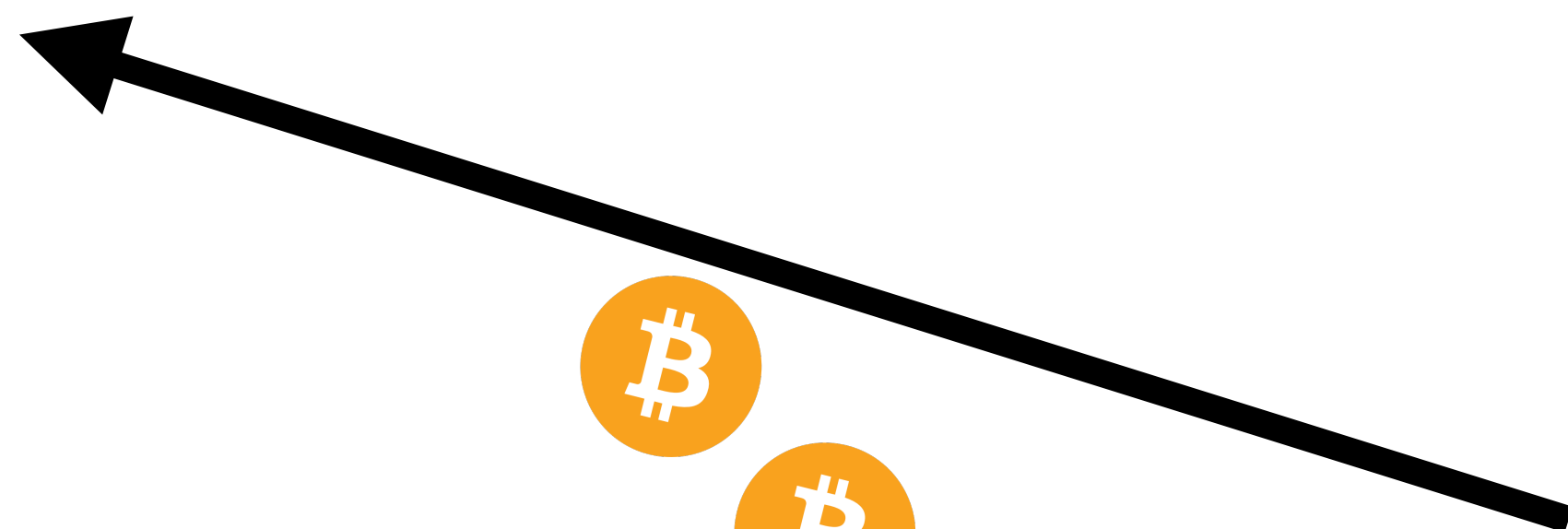
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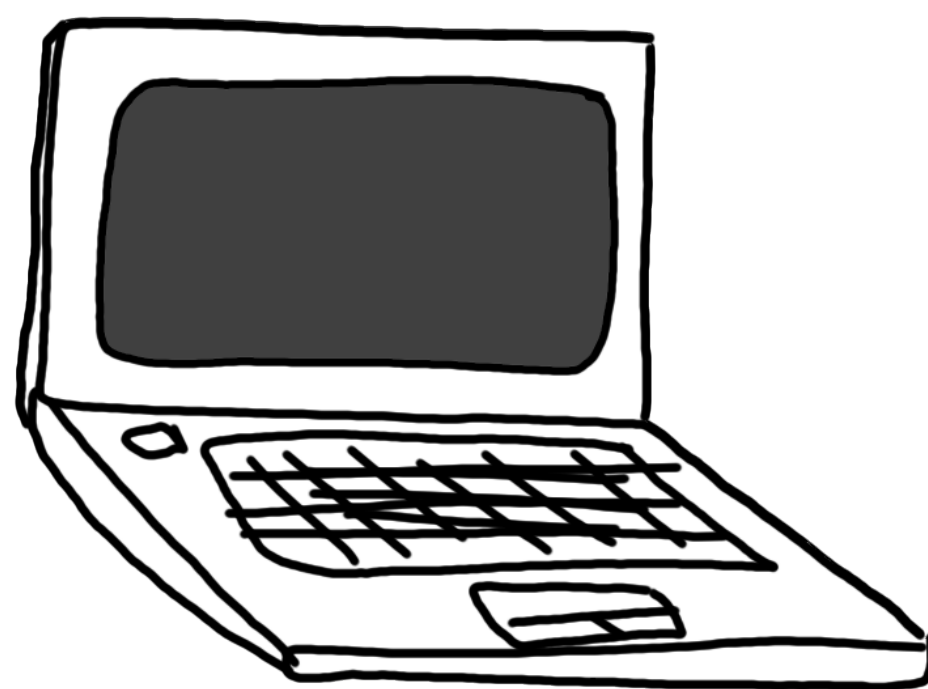
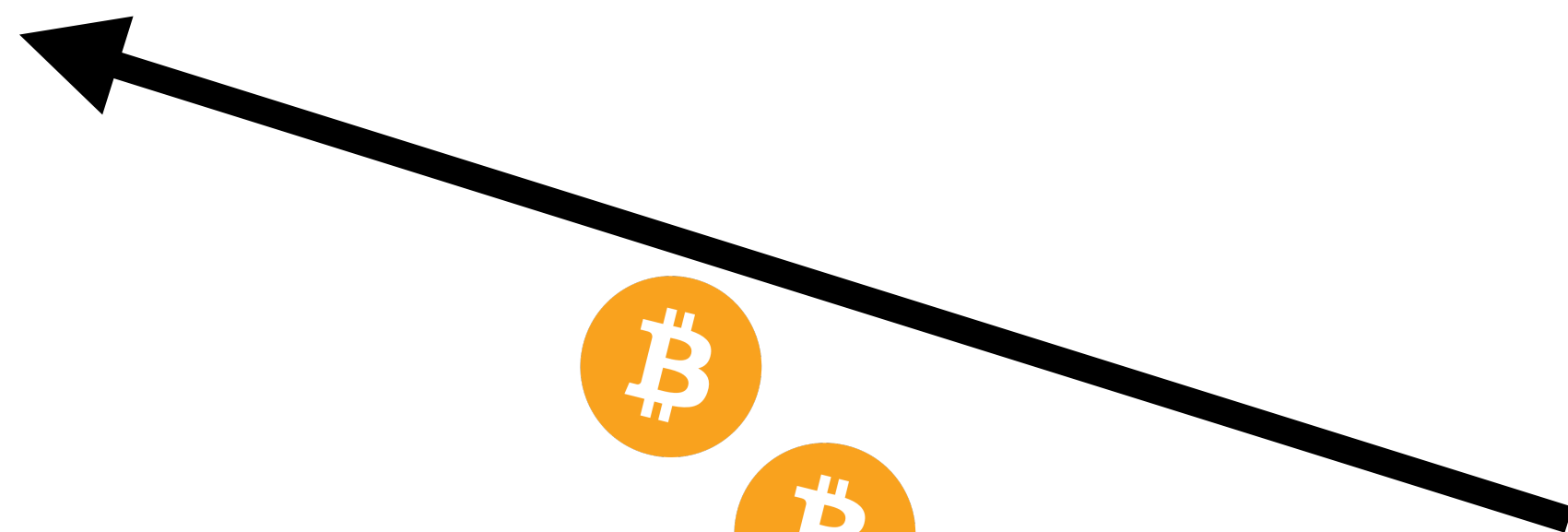
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- Formalize notion of **unanimous erasure**
- **(2,n) setting**: **novel protocol** native to mode of operation for wallets, shown practical via implementation
- **(t,n) setting**: prove it's **impossible** to achieve unanimous erasure in standard model (even given trusted setup, ledger)

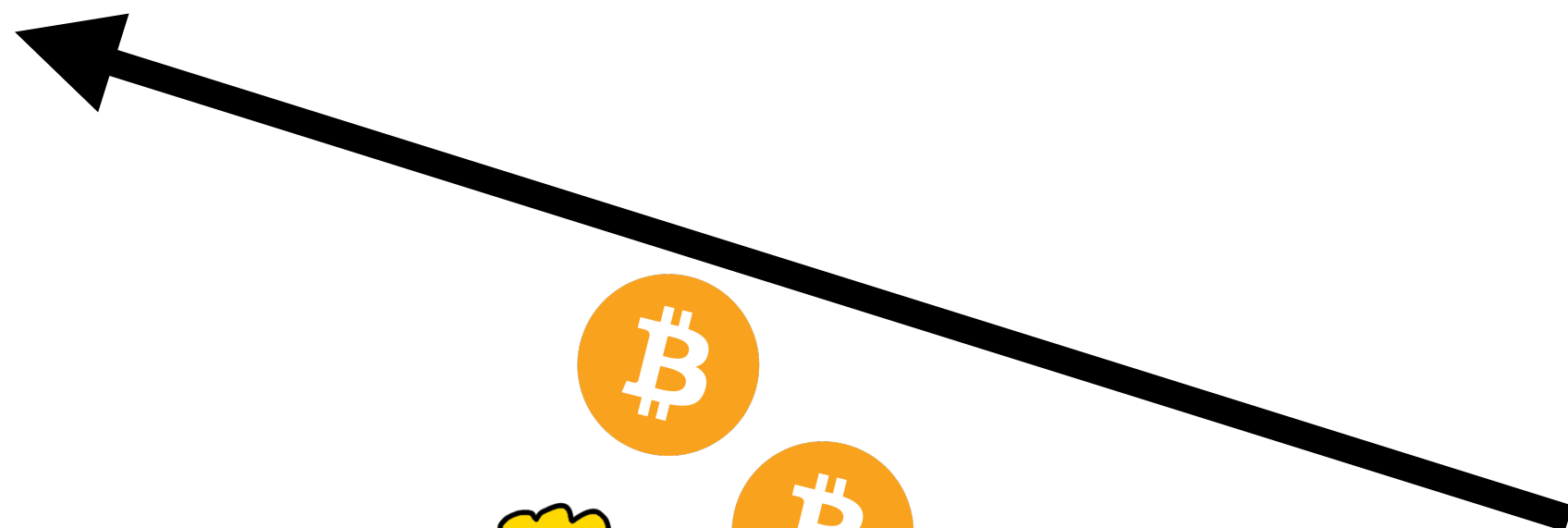






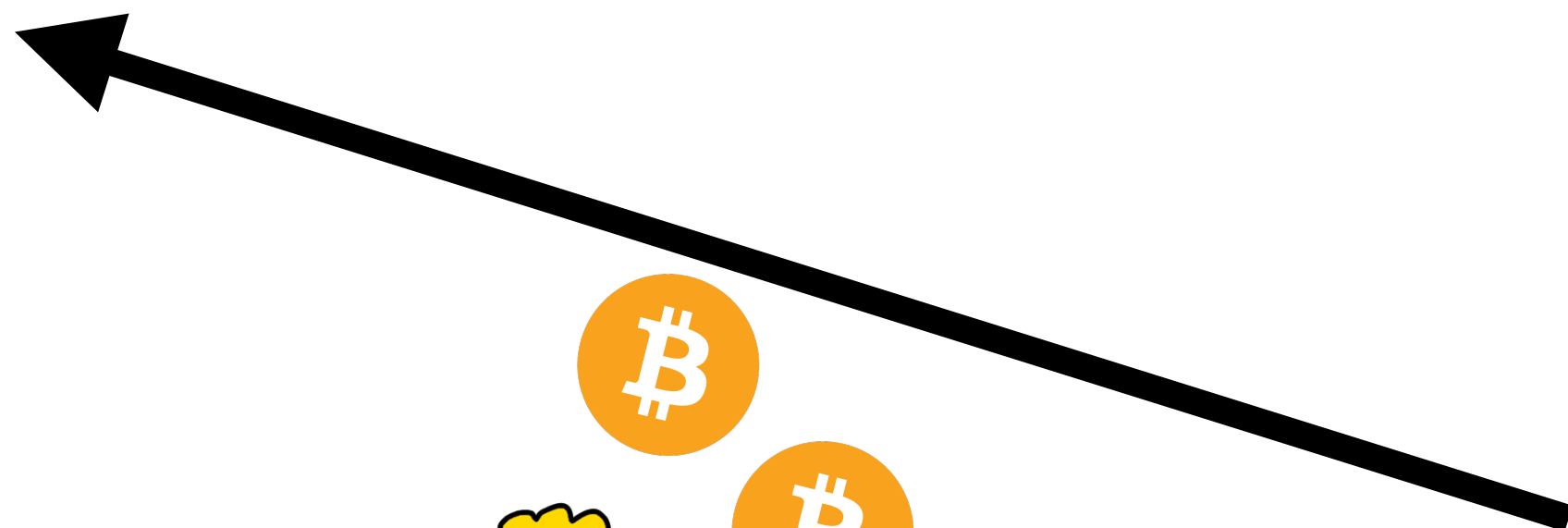
sk





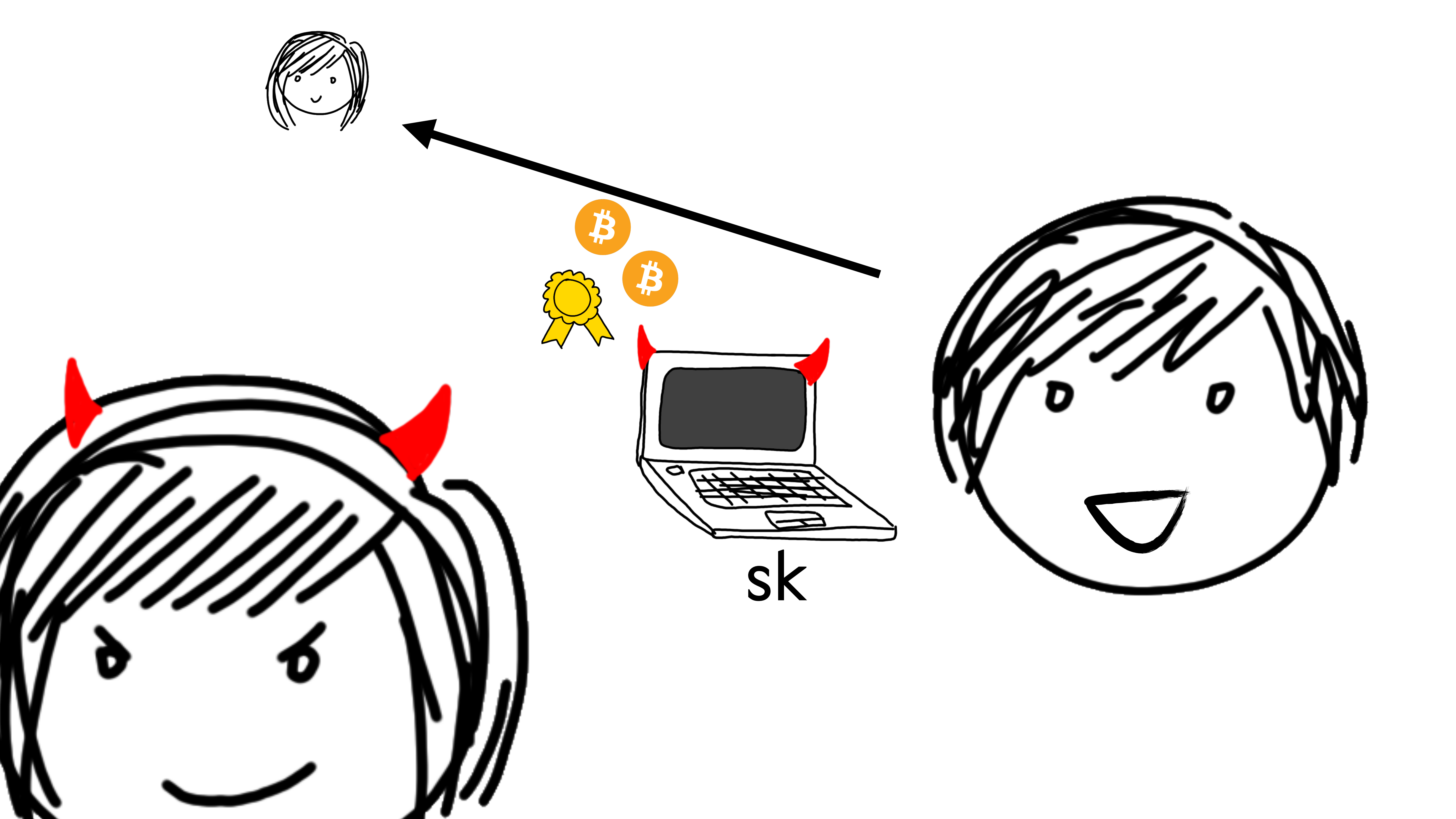
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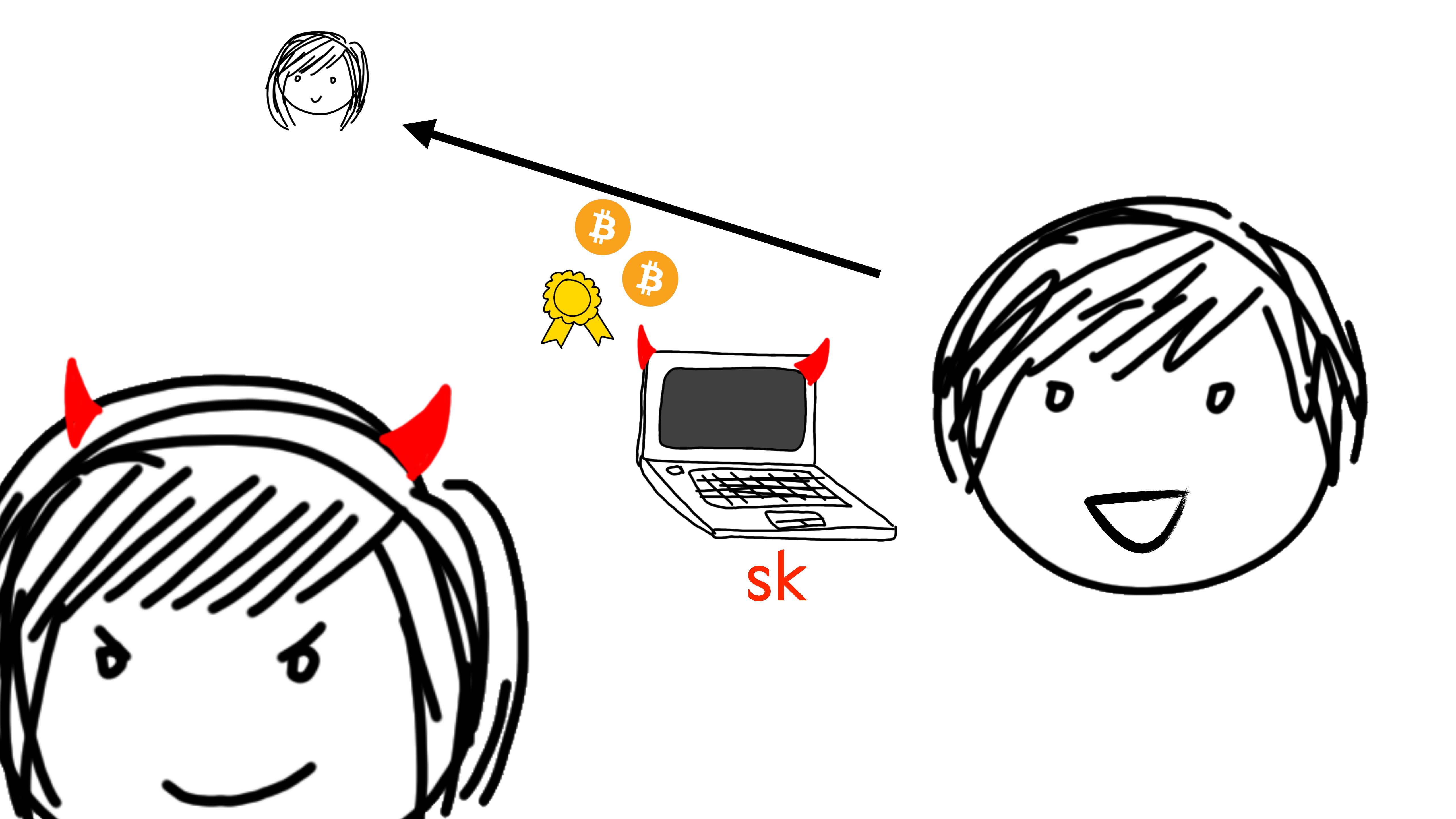


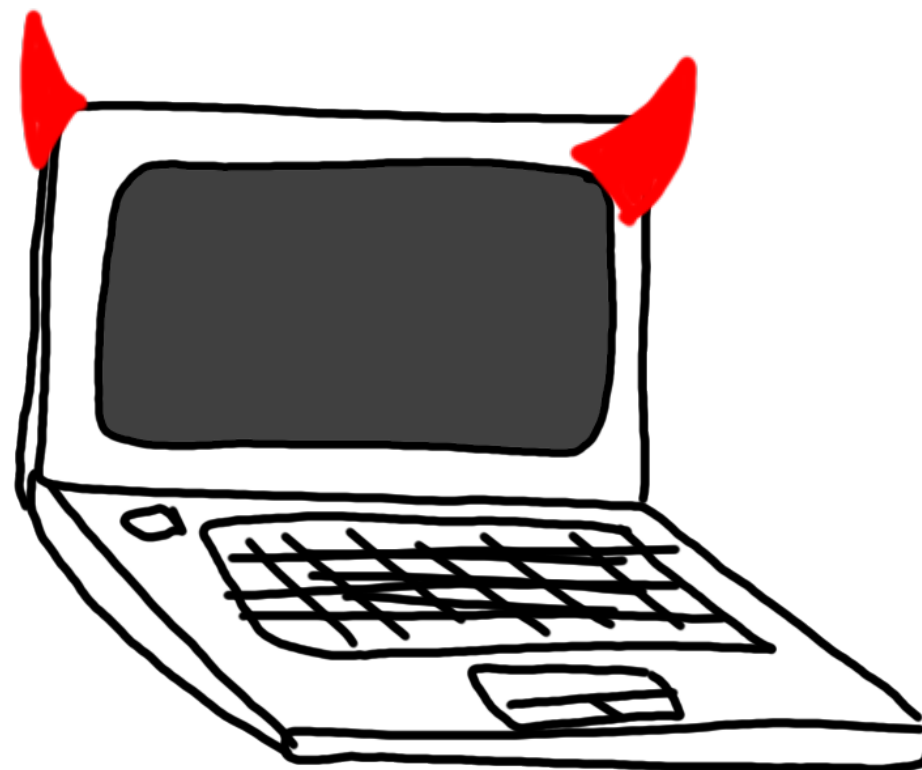
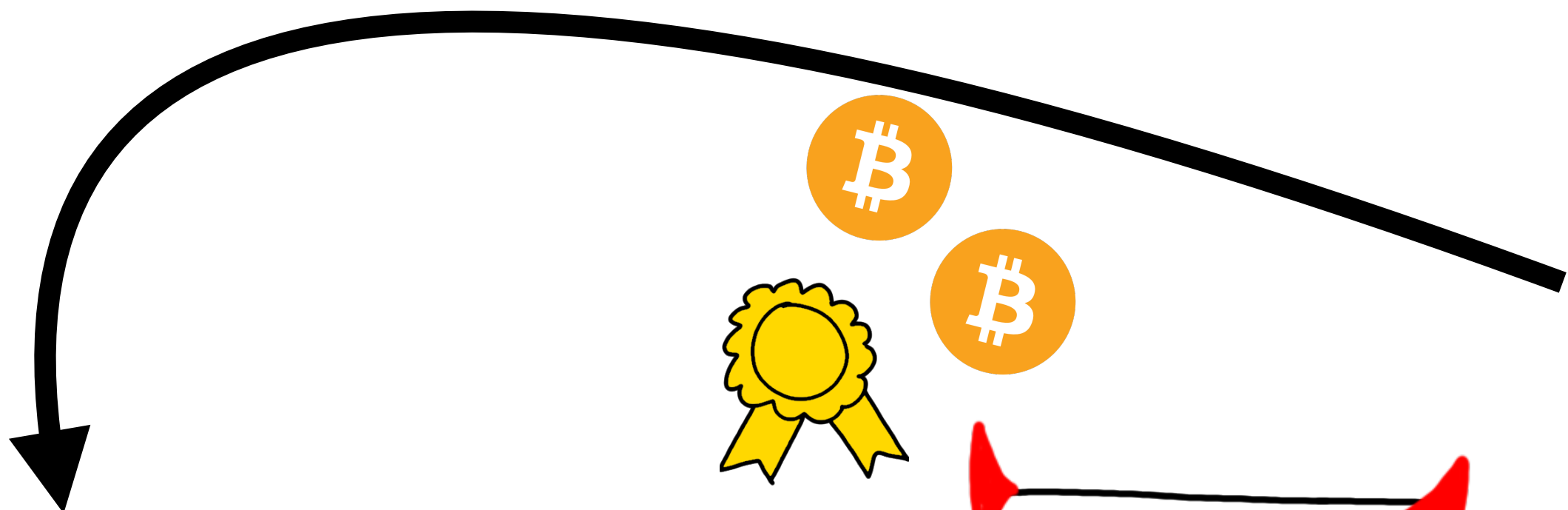


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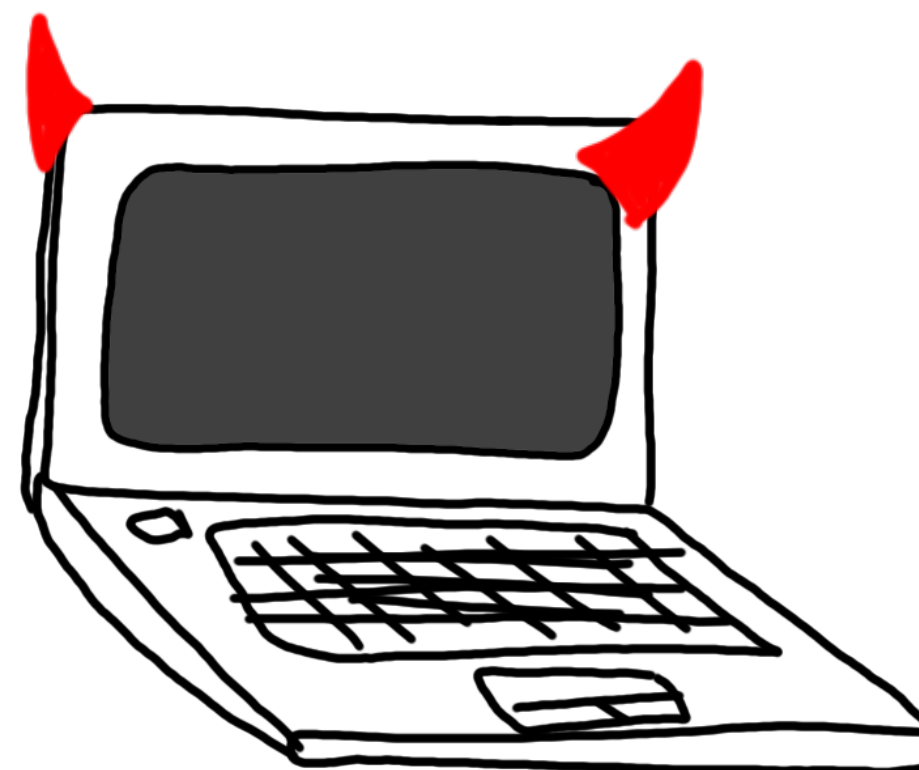
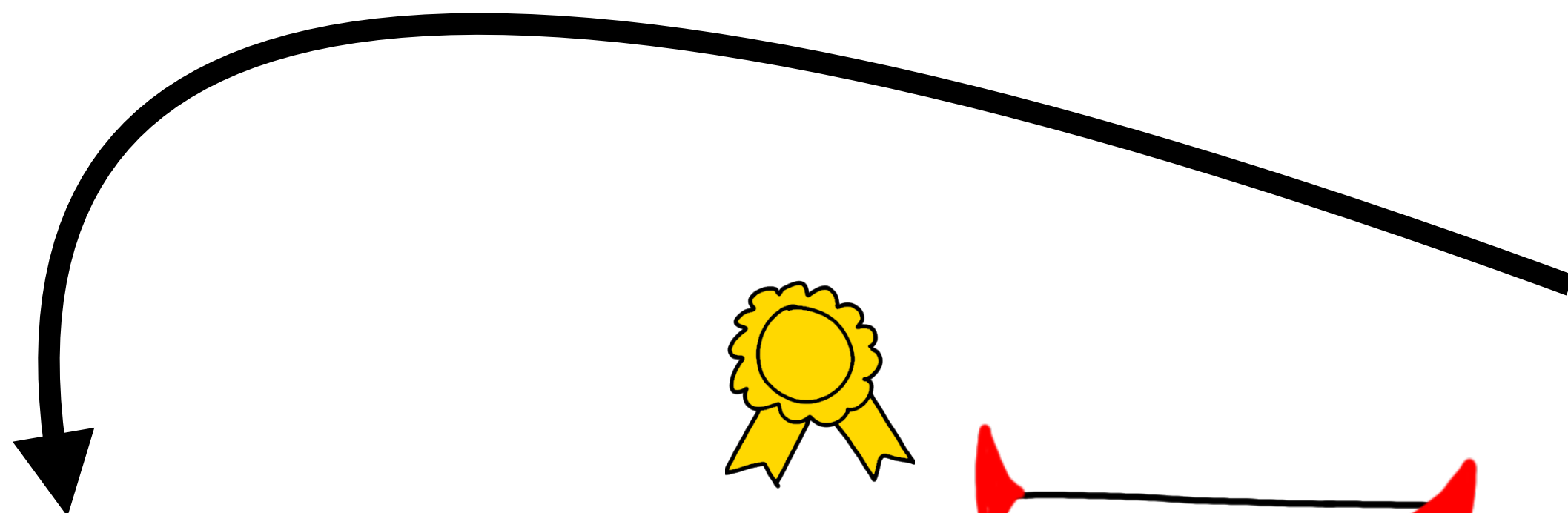






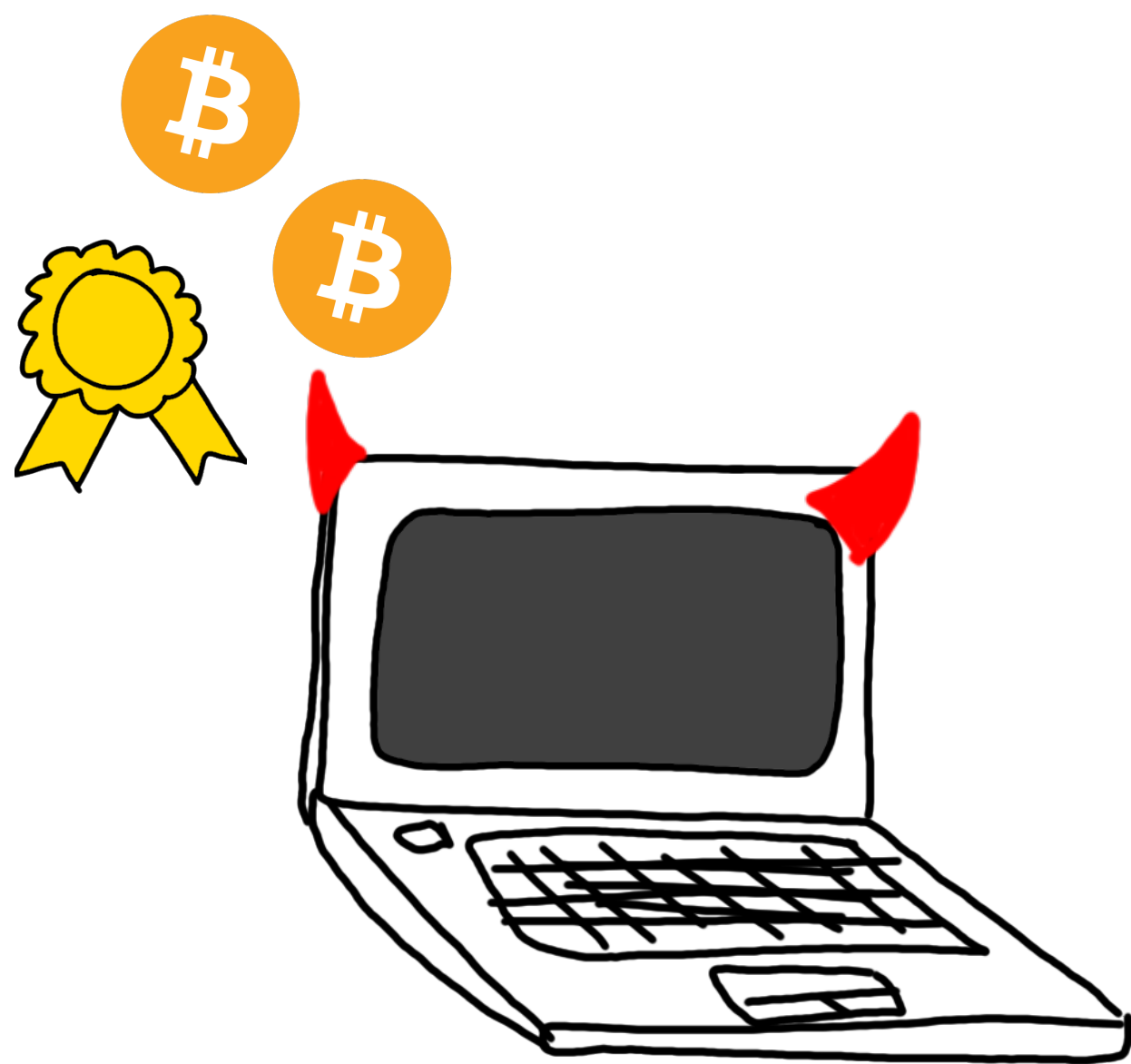
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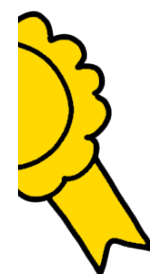
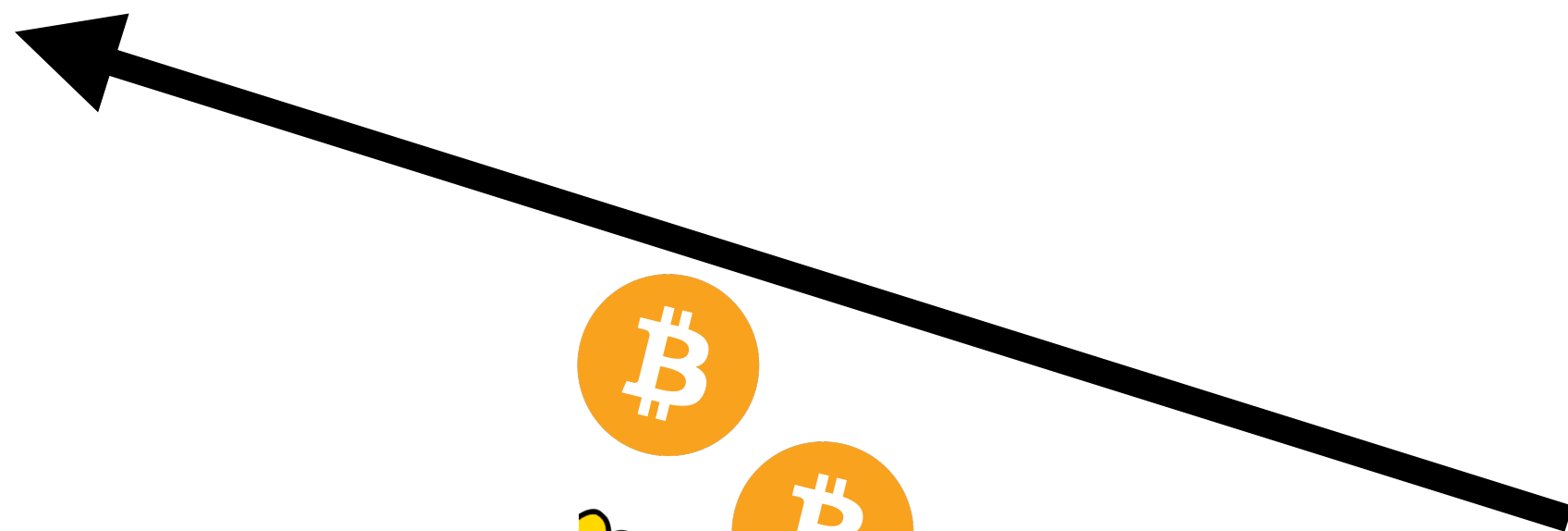




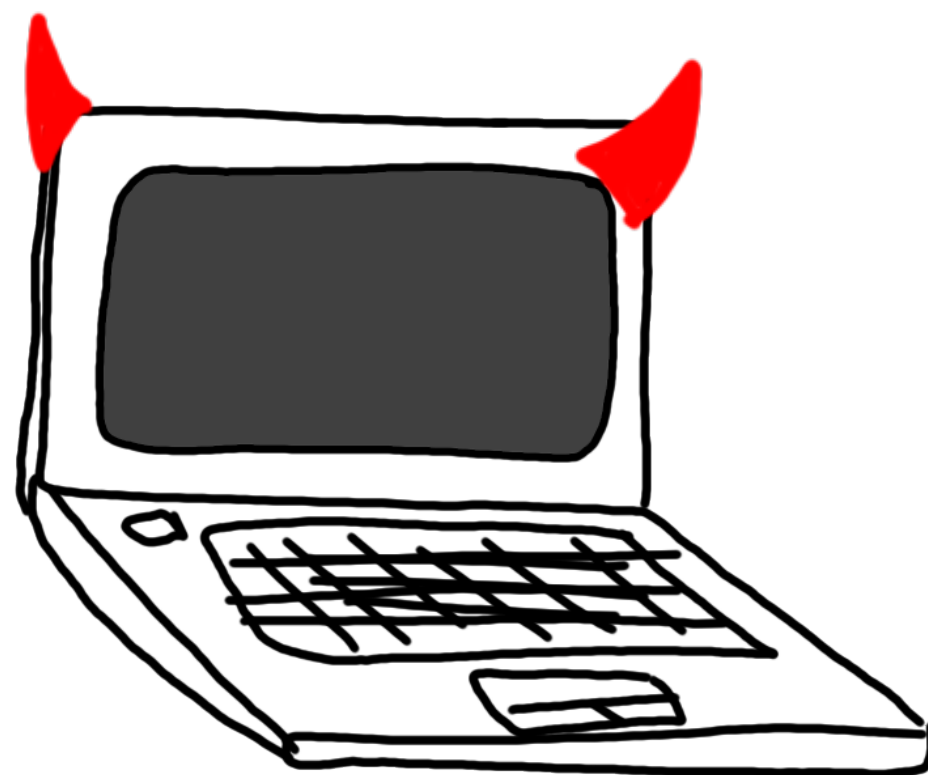
sk







sk

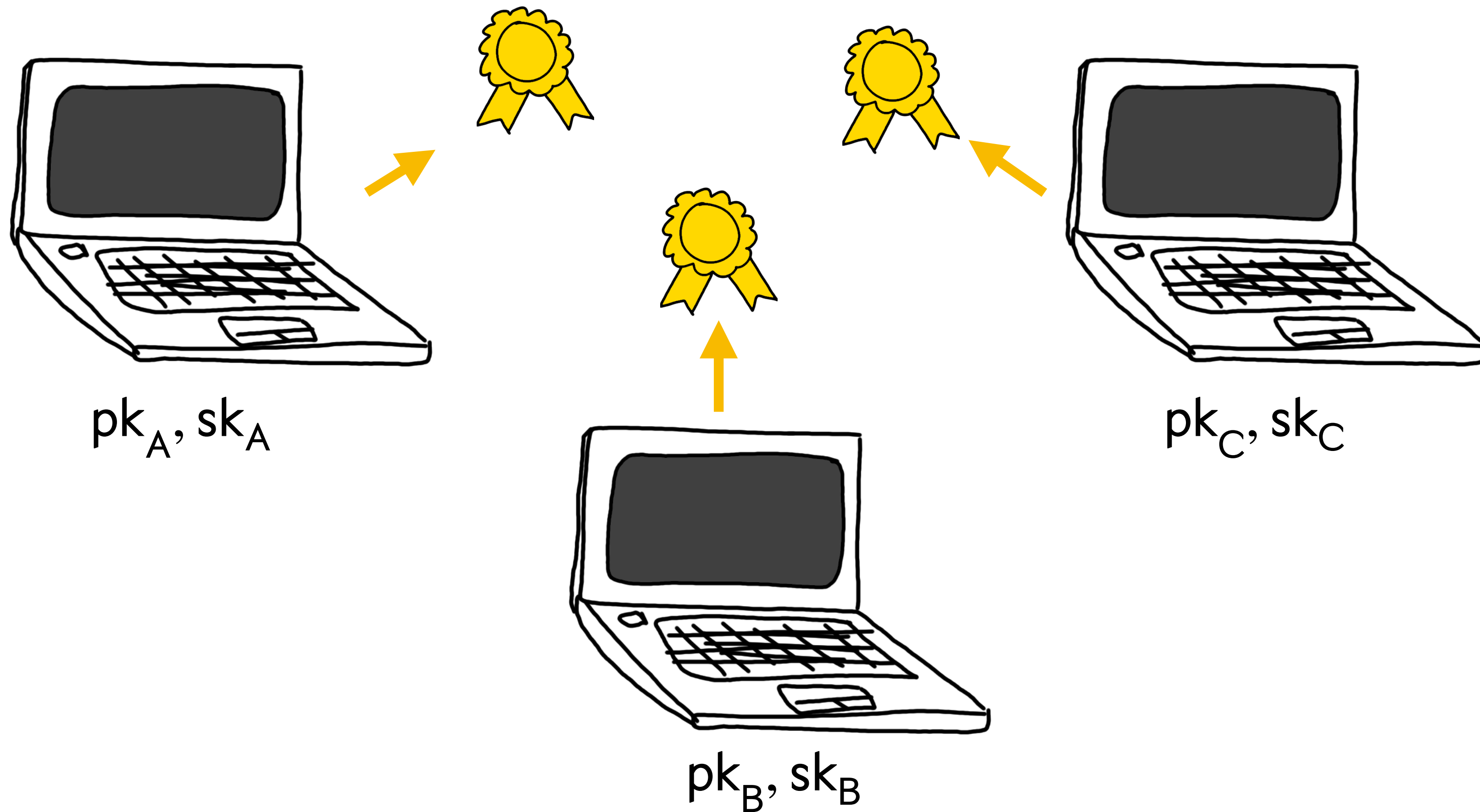


sk'





# Multi-Sig





# Disadvantages





# Disadvantages



- No Anonymity (org structure revealed)
- Size is linear in party count
- Not drop-in replacement

# Threshold Signature

$$\{sk_A, sk_B, sk_C\} \leftarrow \text{Share}(sk)$$

pk



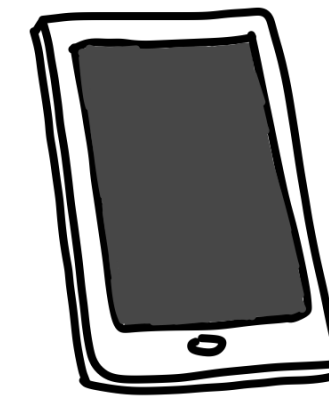
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$$\{sk_A, sk_B, sk_C\} \leftarrow \text{Share}(sk)$$



$sk_A$

$pk$



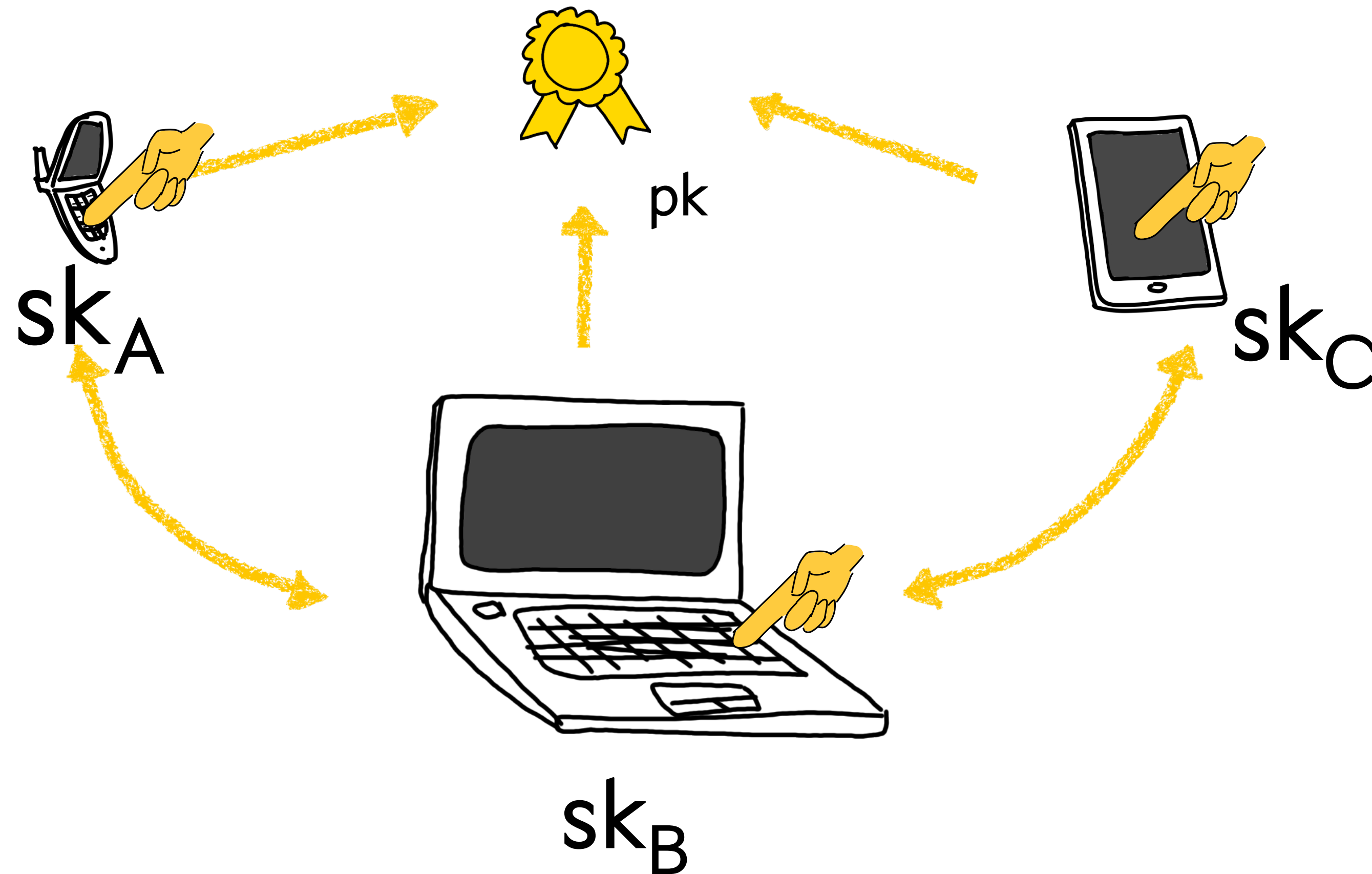
$sk_C$



$sk_B$

# Threshold Signature

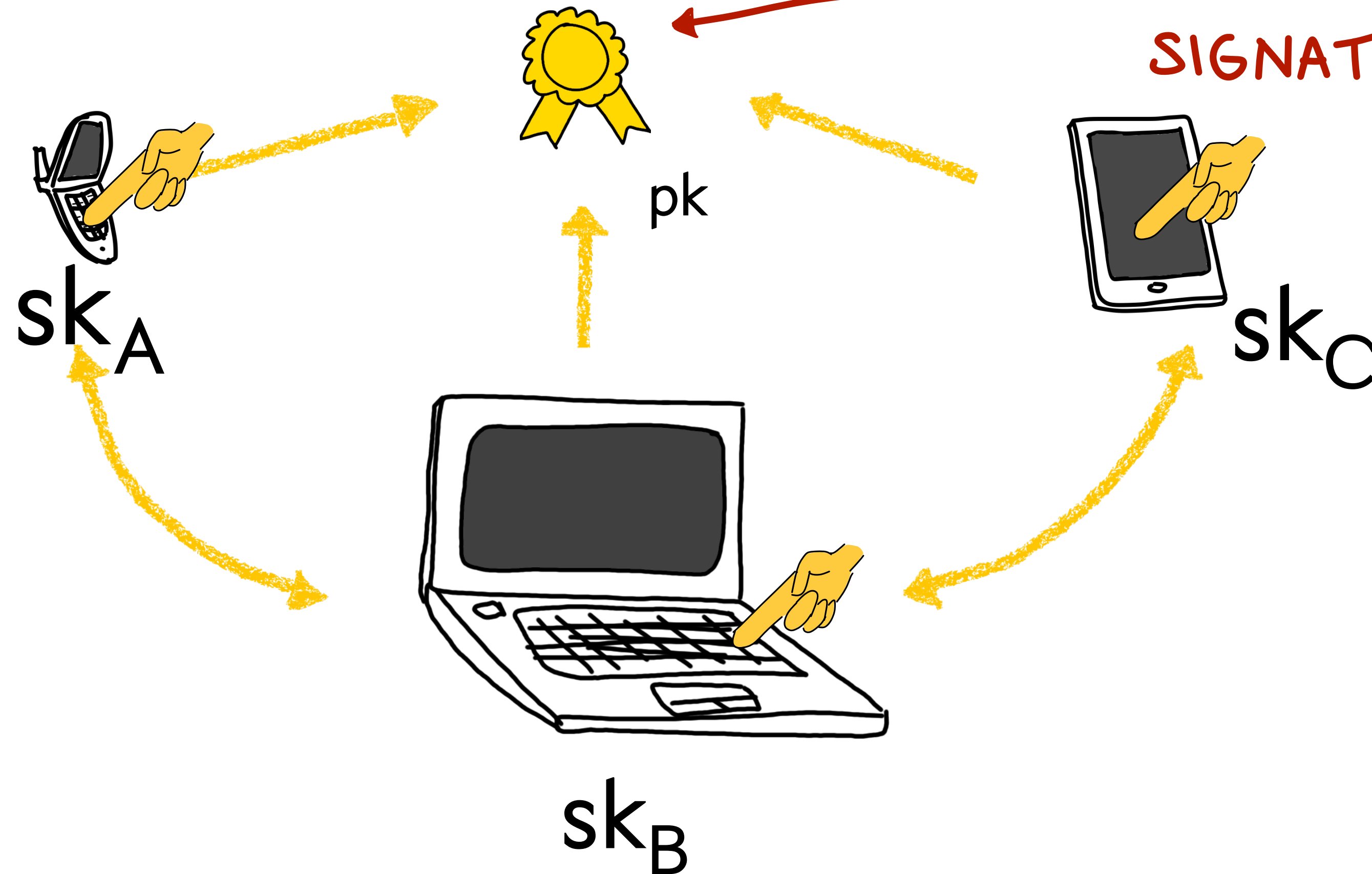
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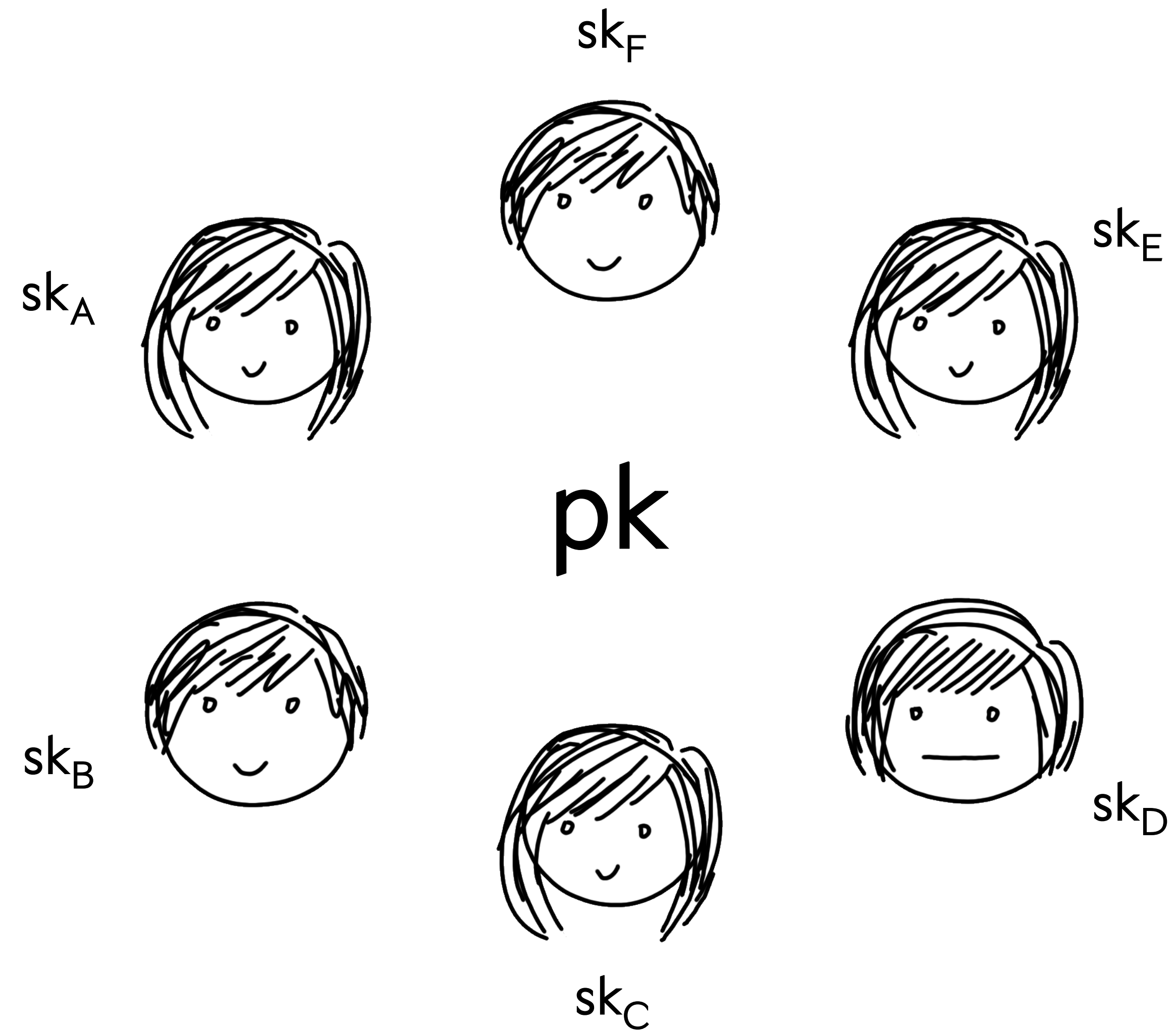
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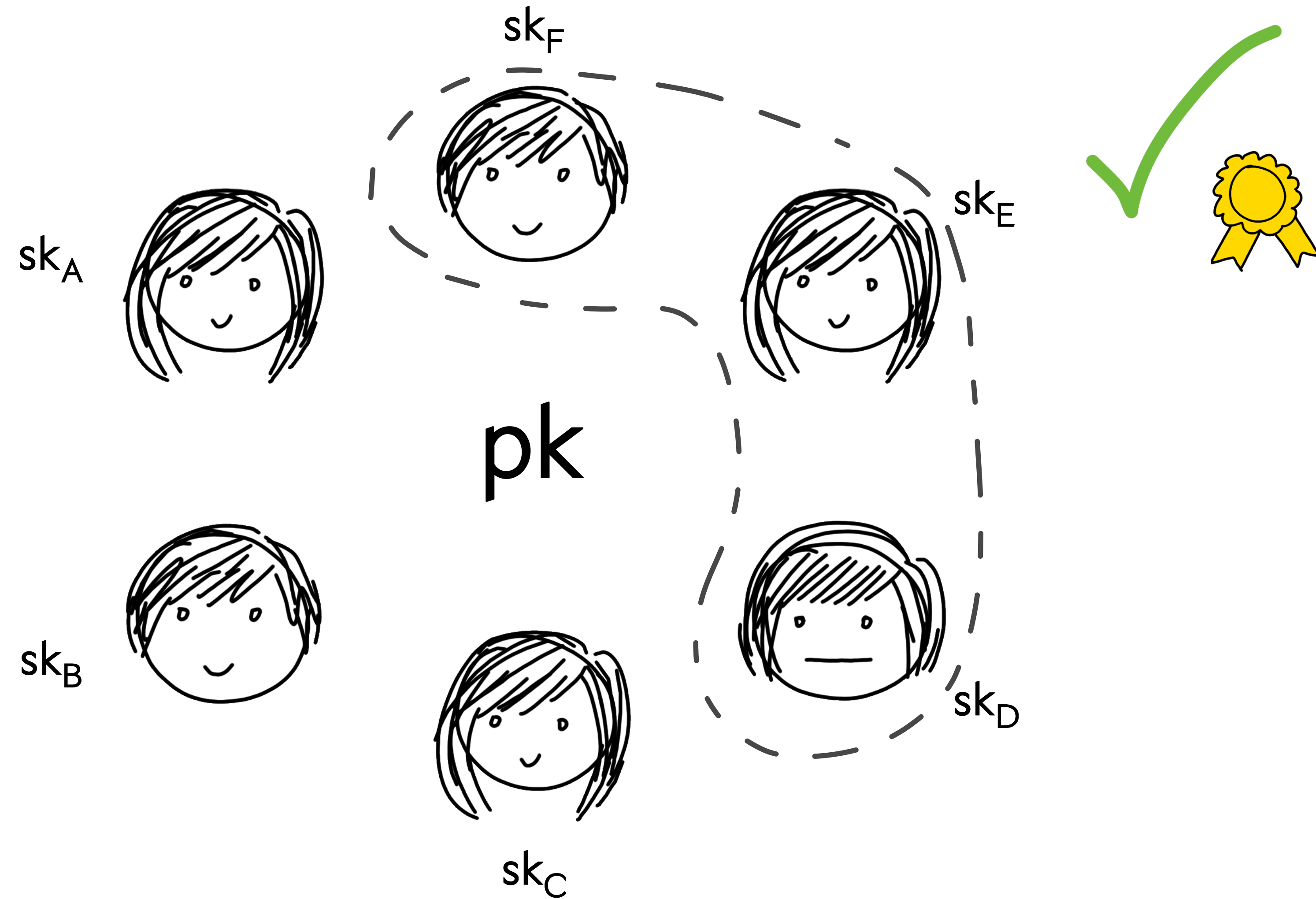
INDISTINGUISHABLE  
FROM ORDINARY  
SIGNATURE



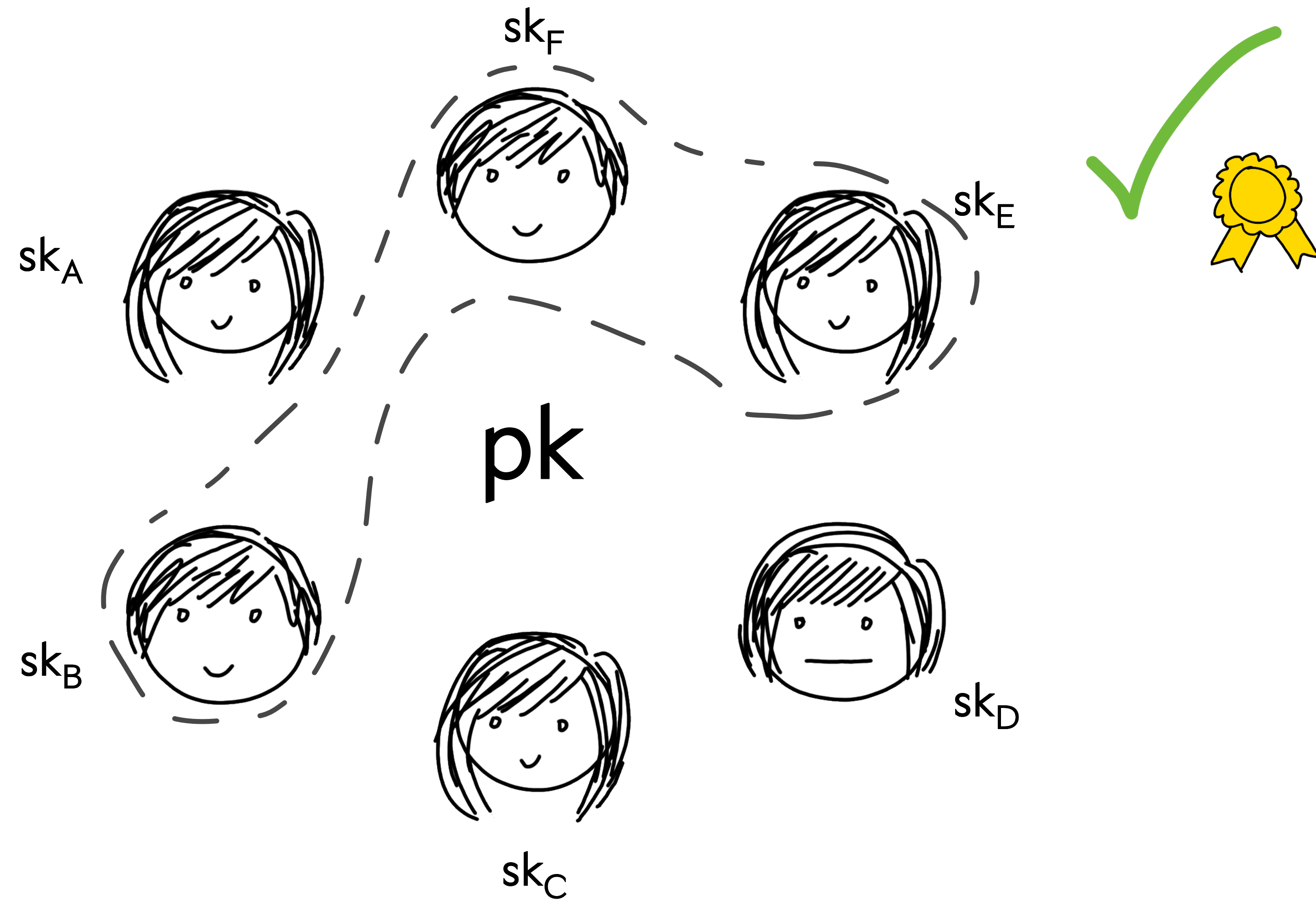
# 3-of-n Signature Scheme



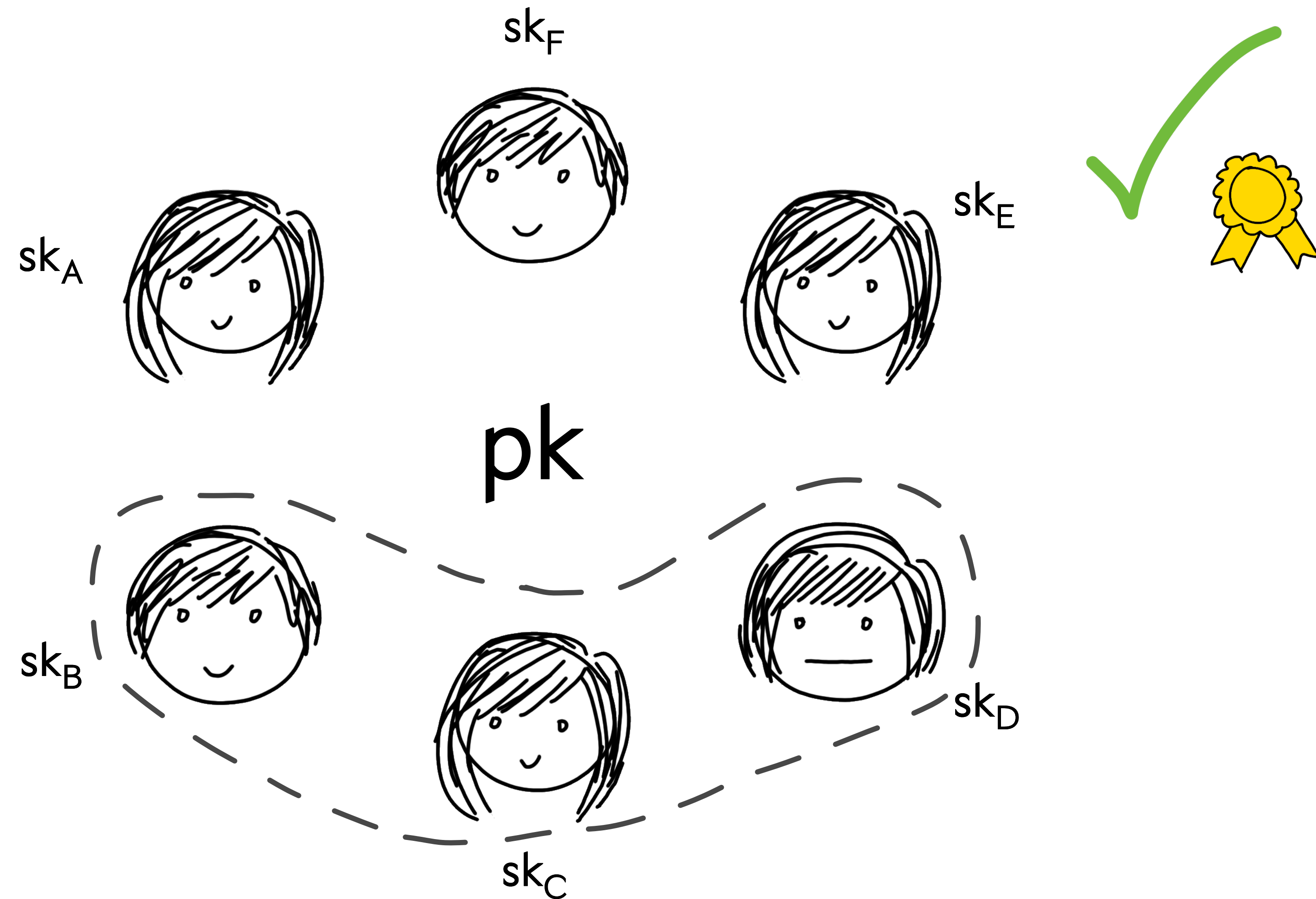
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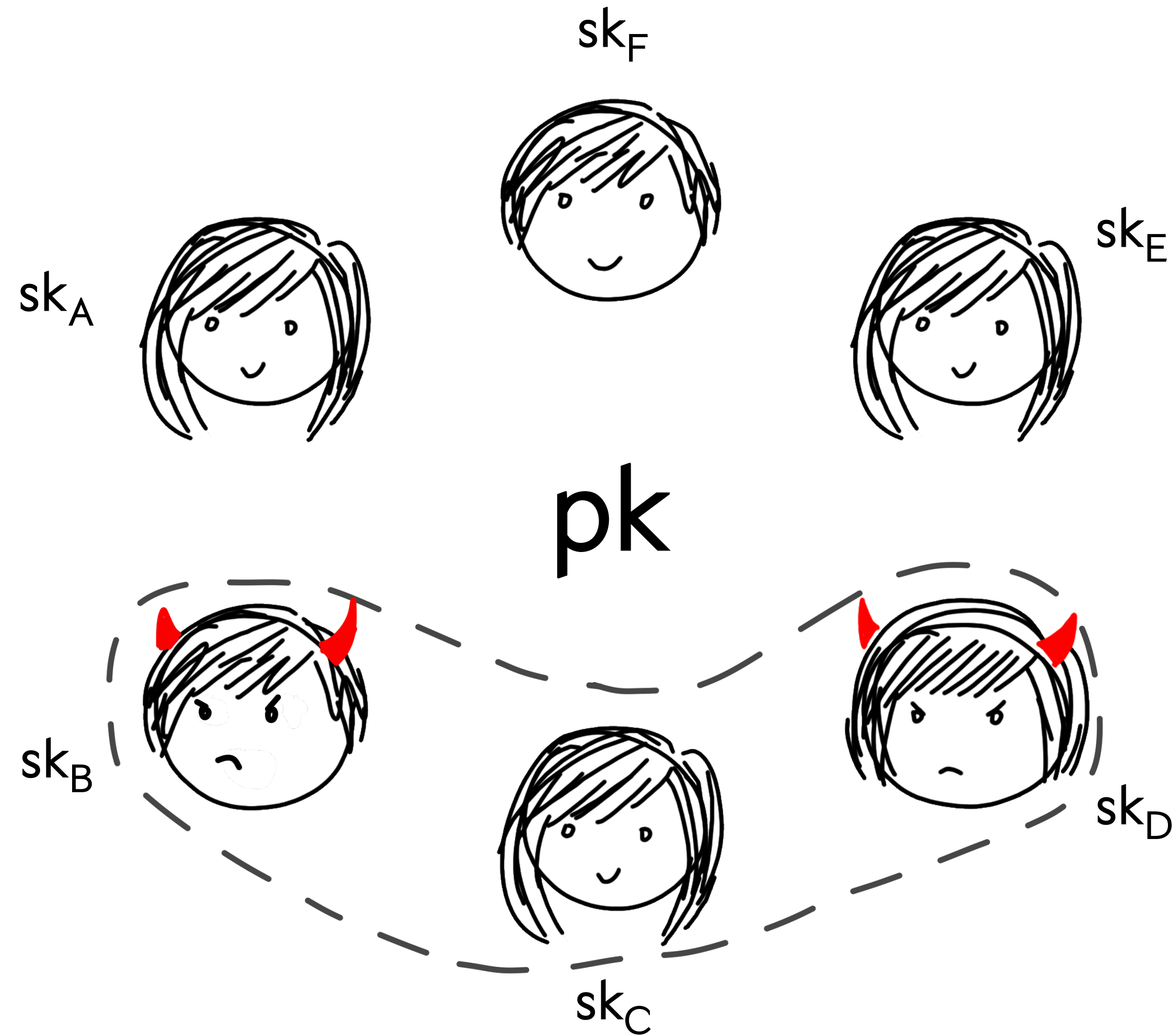
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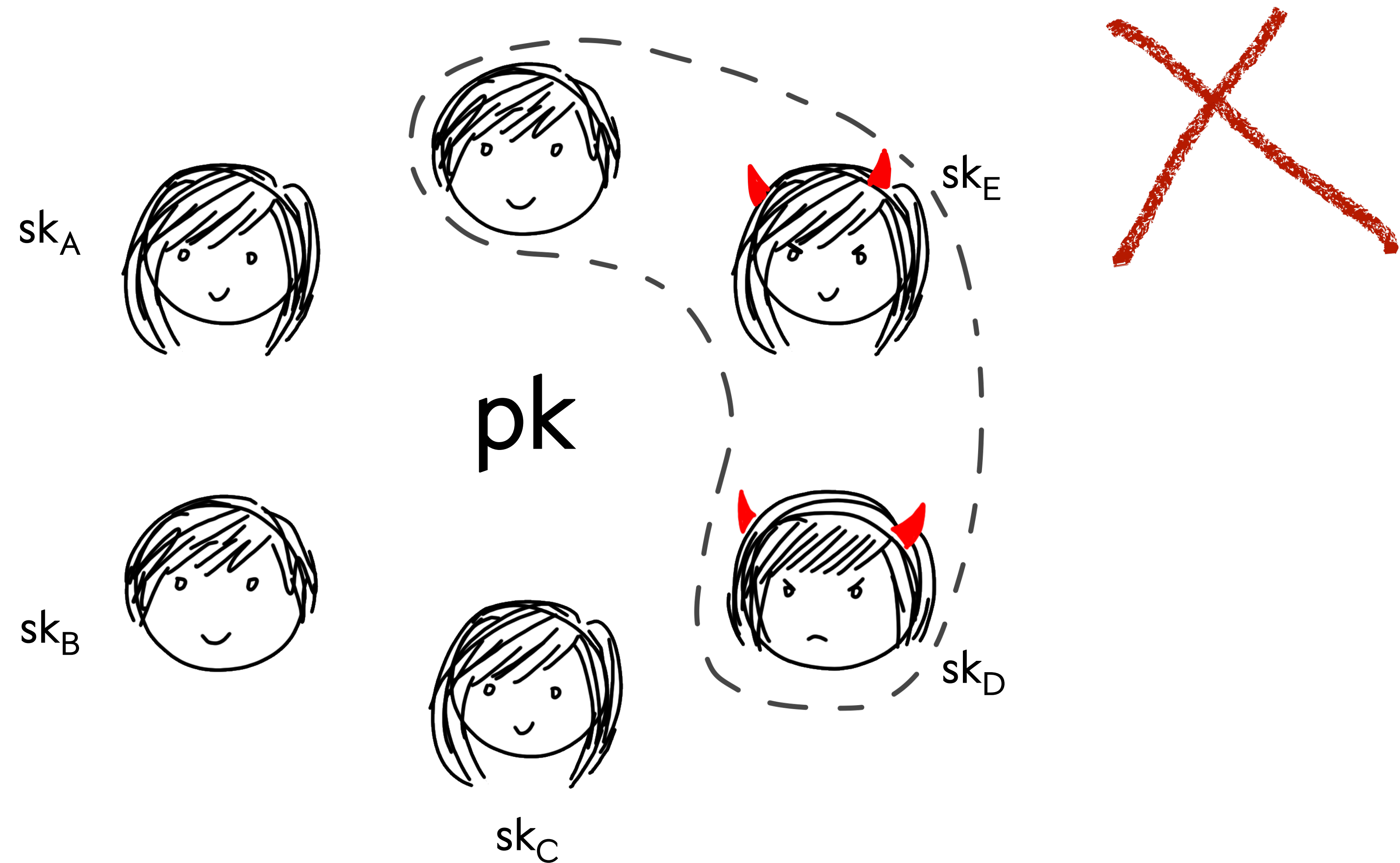
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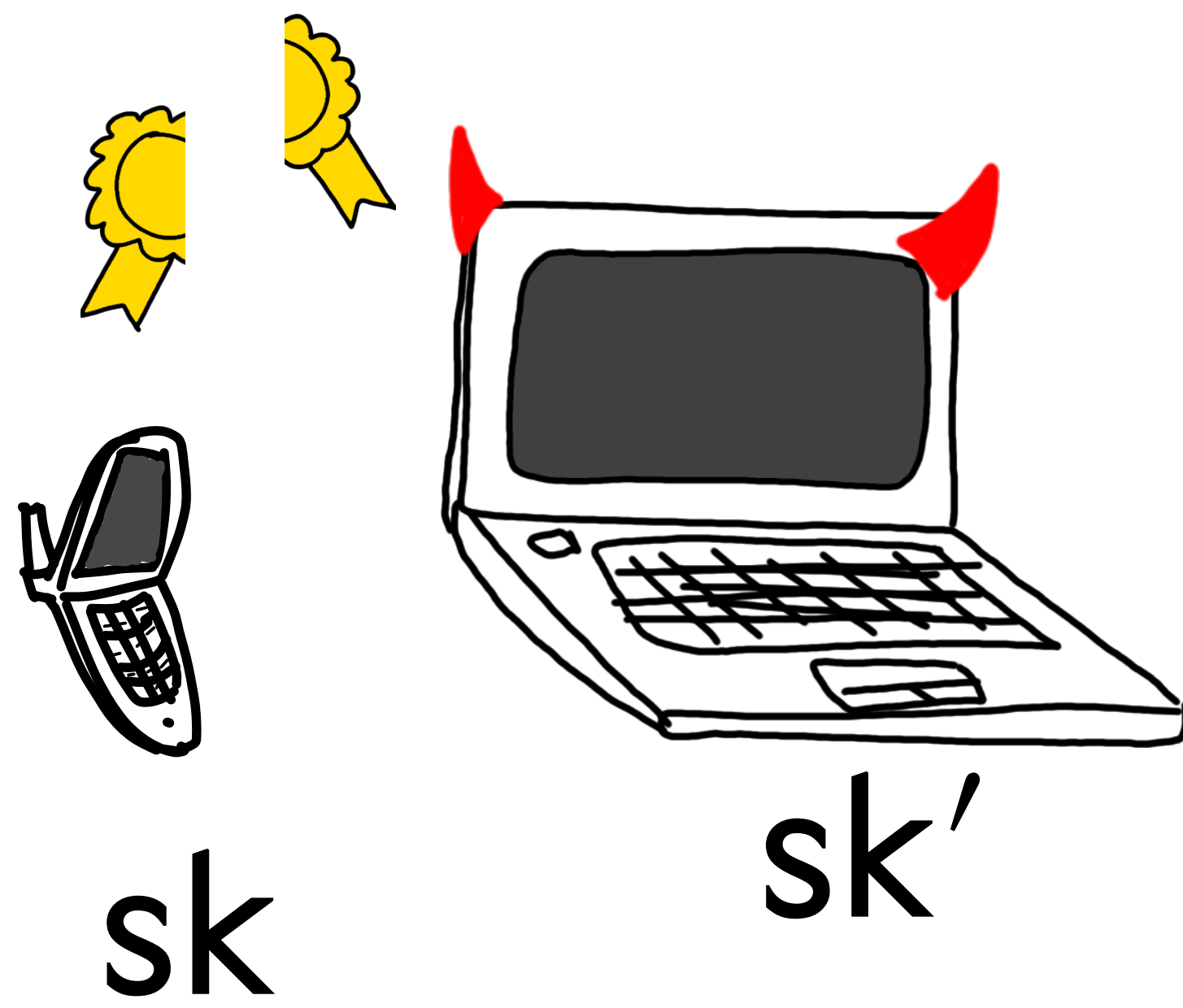


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sk'



sk'



sk



sk' sk



sk'



sk' sk



sk



sk'



sk' sk



sk

MON





sk'



sk' sk



sk'



sk

MON



sk'



sk

TUE





sk'



sk' sk



sk'



sk

MON



sk'



sk

TUE



sk'



sk

WED





sk' sk



sk' sk



sk'



sk'



sk'



sk

MON



sk

TUE



sk

WED





sk' sk



sk' sk



sk'



sk'



sk'



sk

MON



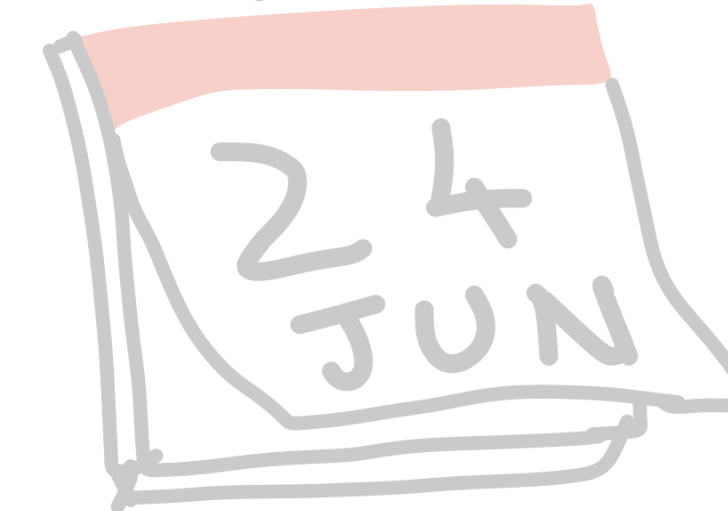
sk

TUE



sk

WED





sk' sk



sk

MON



sk

TUE



sk

WED





sk' sk



sk

MON



sk

TUE



sk

WED





sk'

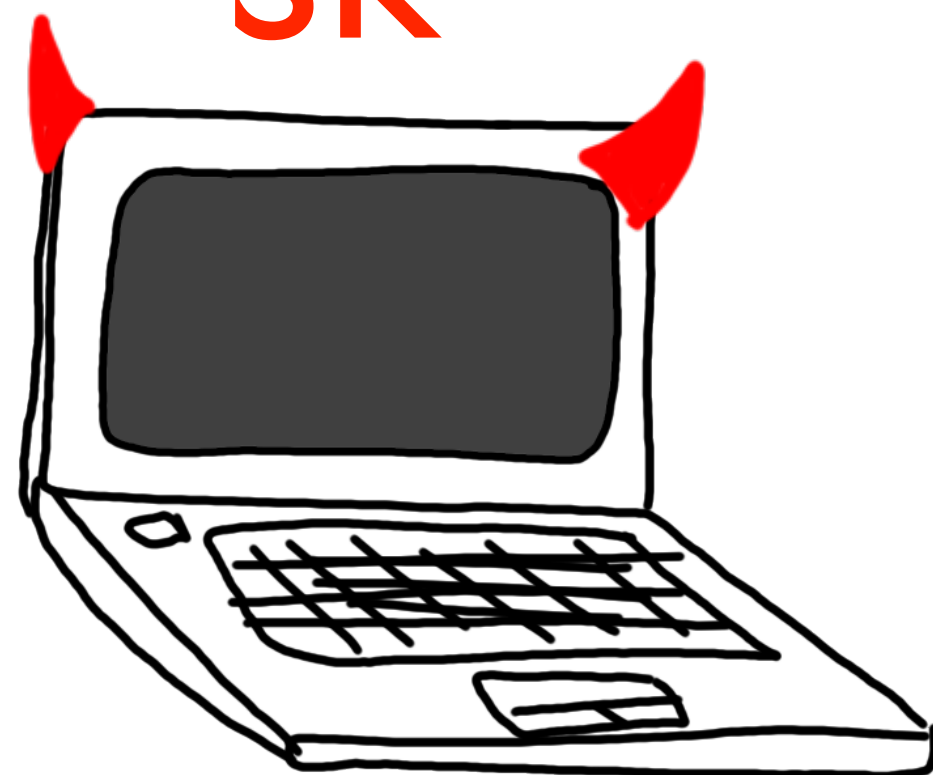


sk



sk'

sk'



sk

MON



sk



sk'



sk



$$sk + sk' = x$$



sk





sk'



sk



$$sk + sk' = x$$



sk

MON



TUE

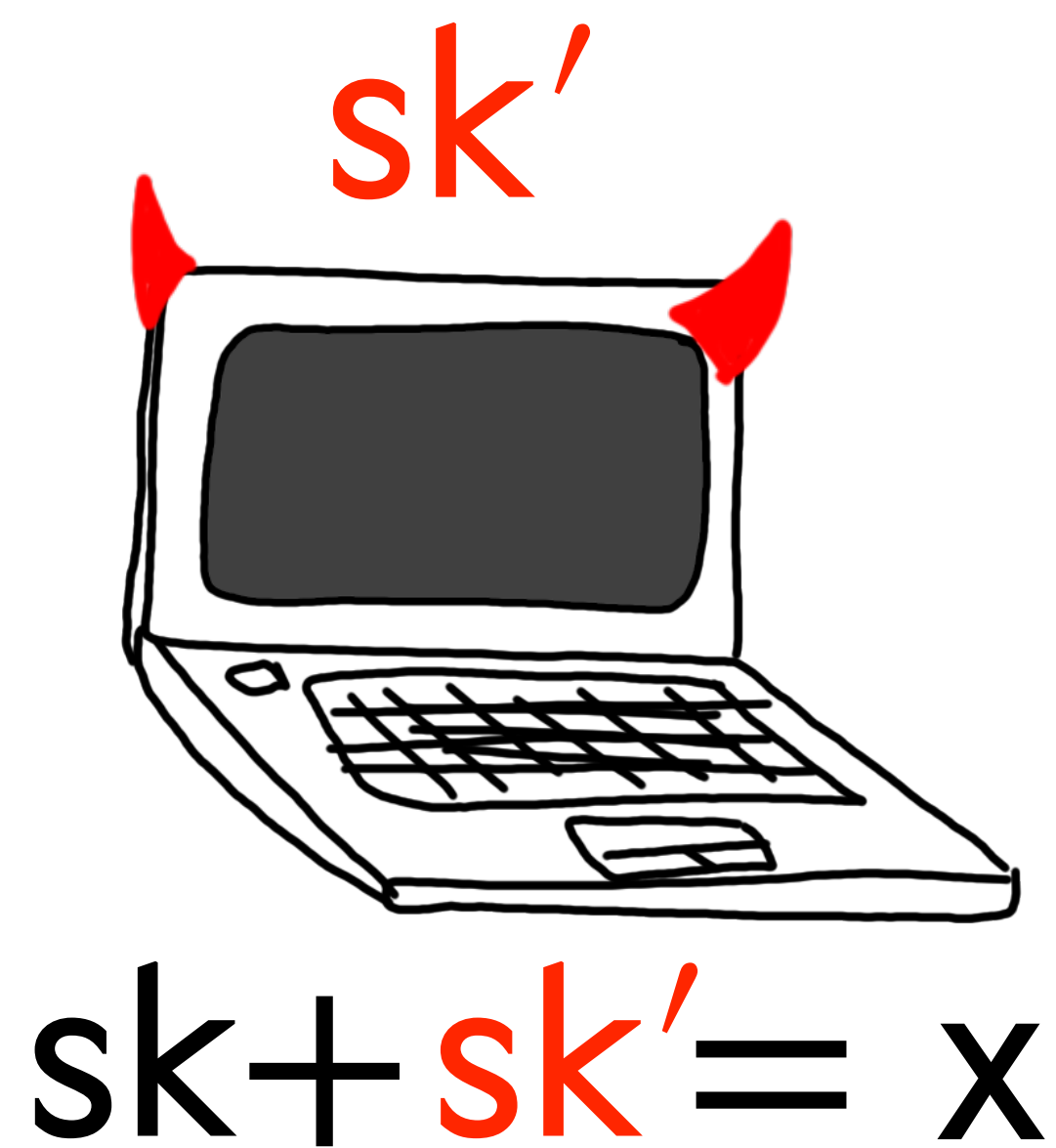




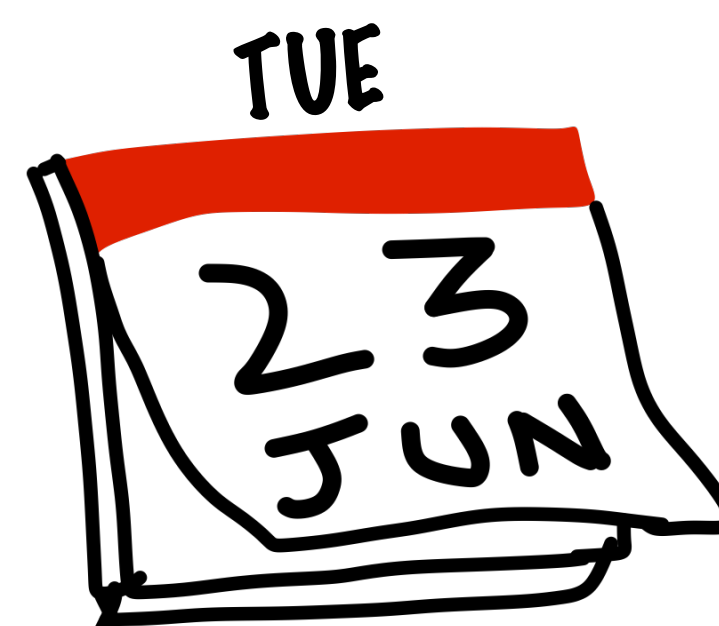
sk'



sk



sk





$sk'$



$sk$



$$sk + sk' = x$$



$sk$

MON



$sk_T$

TUE





$sk'$



$sk$



$$sk + sk' = x$$



$sk$

MON



$$sk_T + sk_T' = x$$



$sk_T$

TUE





$sk'$



$sk$



$$sk + sk' = x$$



$sk$

MON



$$sk_T + sk'_T = x$$



$sk_T$

TUE



$$sk'_W + sk_W = x$$



$sk_W$

WED





$sk'$



$sk$



$$sk + sk' = x$$



$sk$

MON



$$sk_T + sk'_T = x$$



$sk_T$

TUE



$$sk'_w + sk_w = x$$



$sk_w$

WED





$sk'$   $sk_w$



$sk$



$$sk + sk' = x$$



$sk$

MON



$$sk_T + sk'_T = x$$



$sk_T$

TUE



$$sk'_w + sk_w = x$$



$sk_w$

WED





$sk' \ sk_w$

$$sk + sk' = x$$

$$sk_T + sk'_T = x$$

$$sk'_w + sk_w = x$$



$sk$





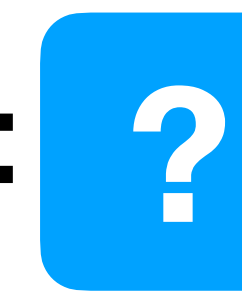
$sk' sk_w$



$+ sk' =$



$+ sk_w =$



$sk$



# 2 Equations in 3 variables



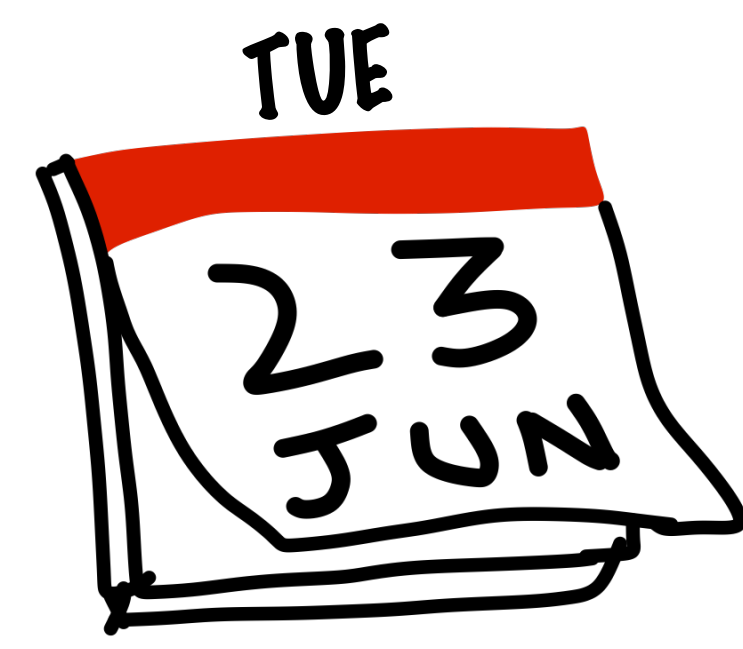
$sk'$   $sk_w$



$$\text{[Black ?]} + sk' = \text{[Blue ?]} \text{ [Grey Box]} \quad \text{[Green ?]} + sk_w = \text{[Blue ?]}$$



$sk$



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  - Dynamic committees [MZWLZJS19]

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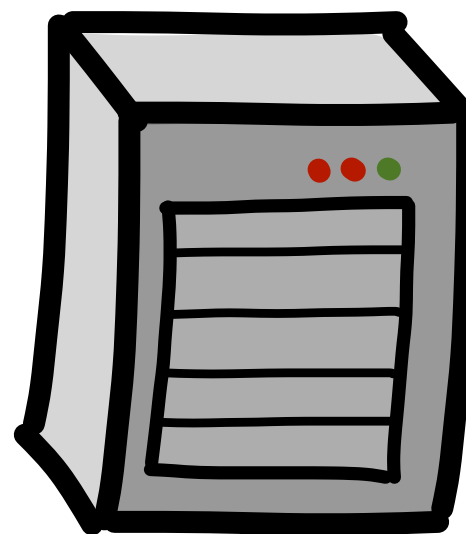
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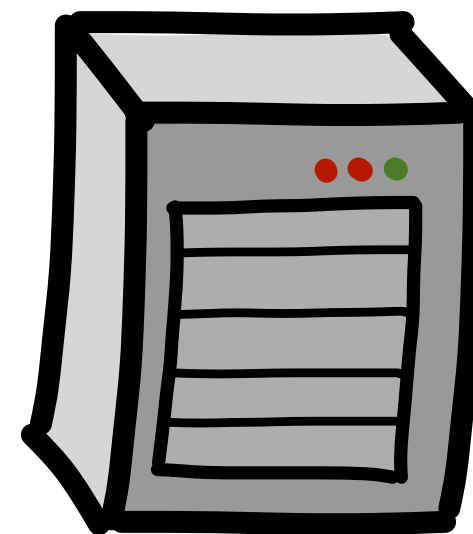
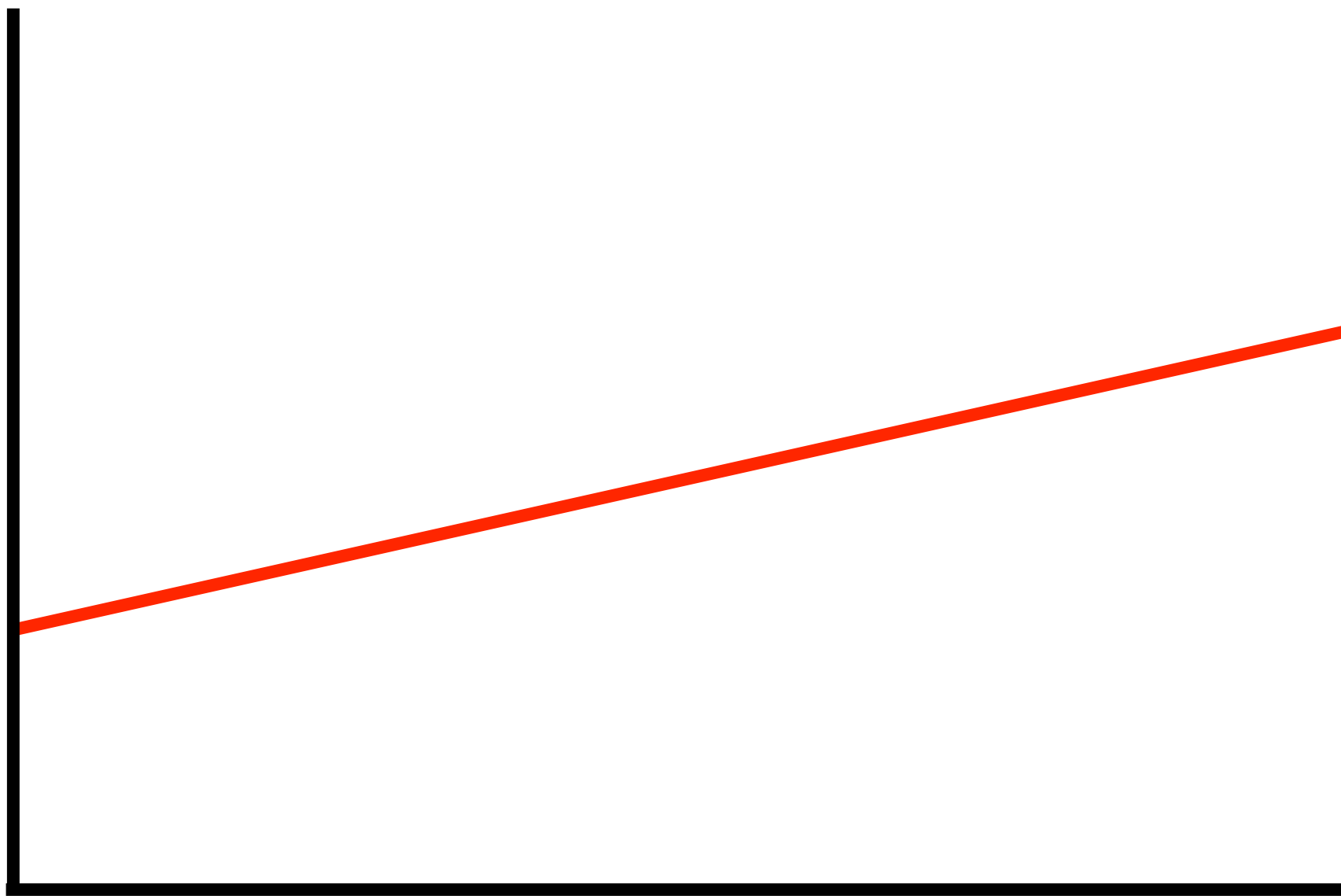
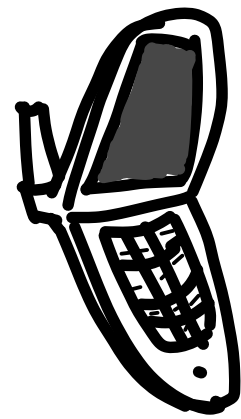
# Defining Offline Refresh



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$$f \leftarrow \mathbb{Z}_q[x]$$

Degree 1

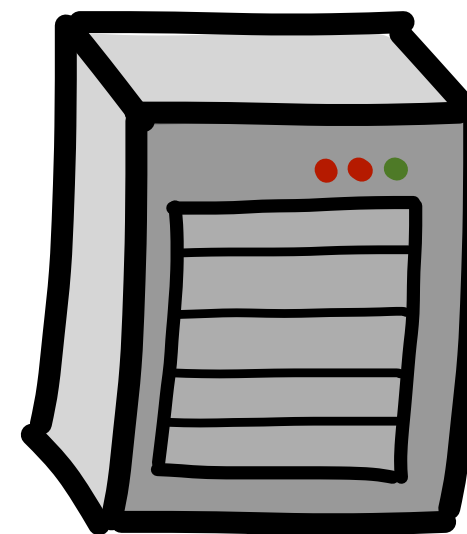
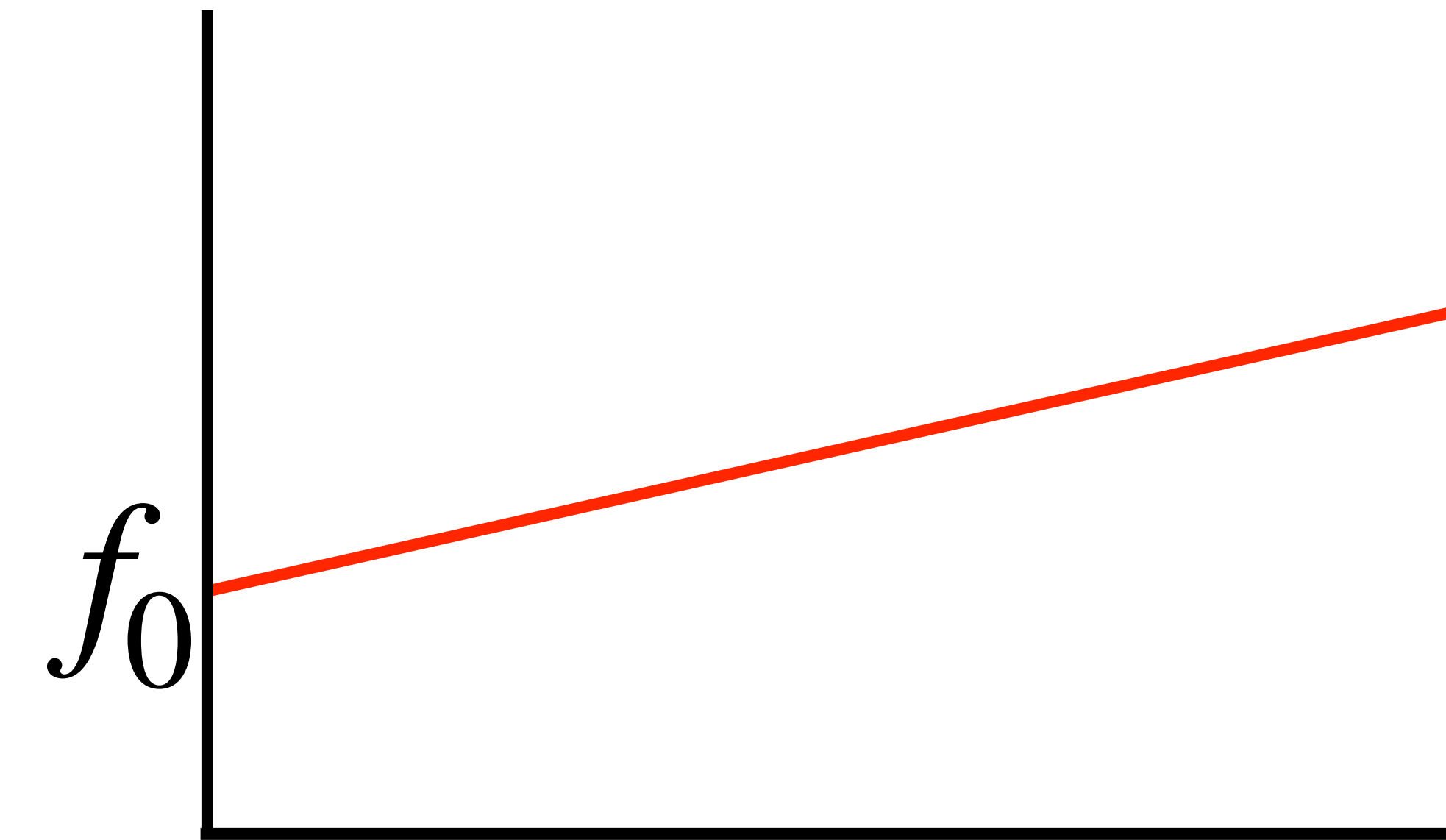


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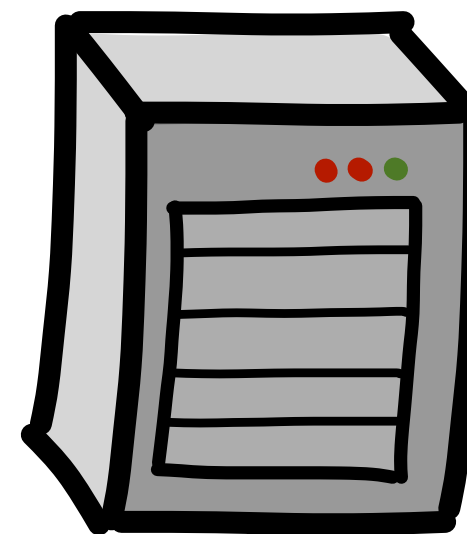
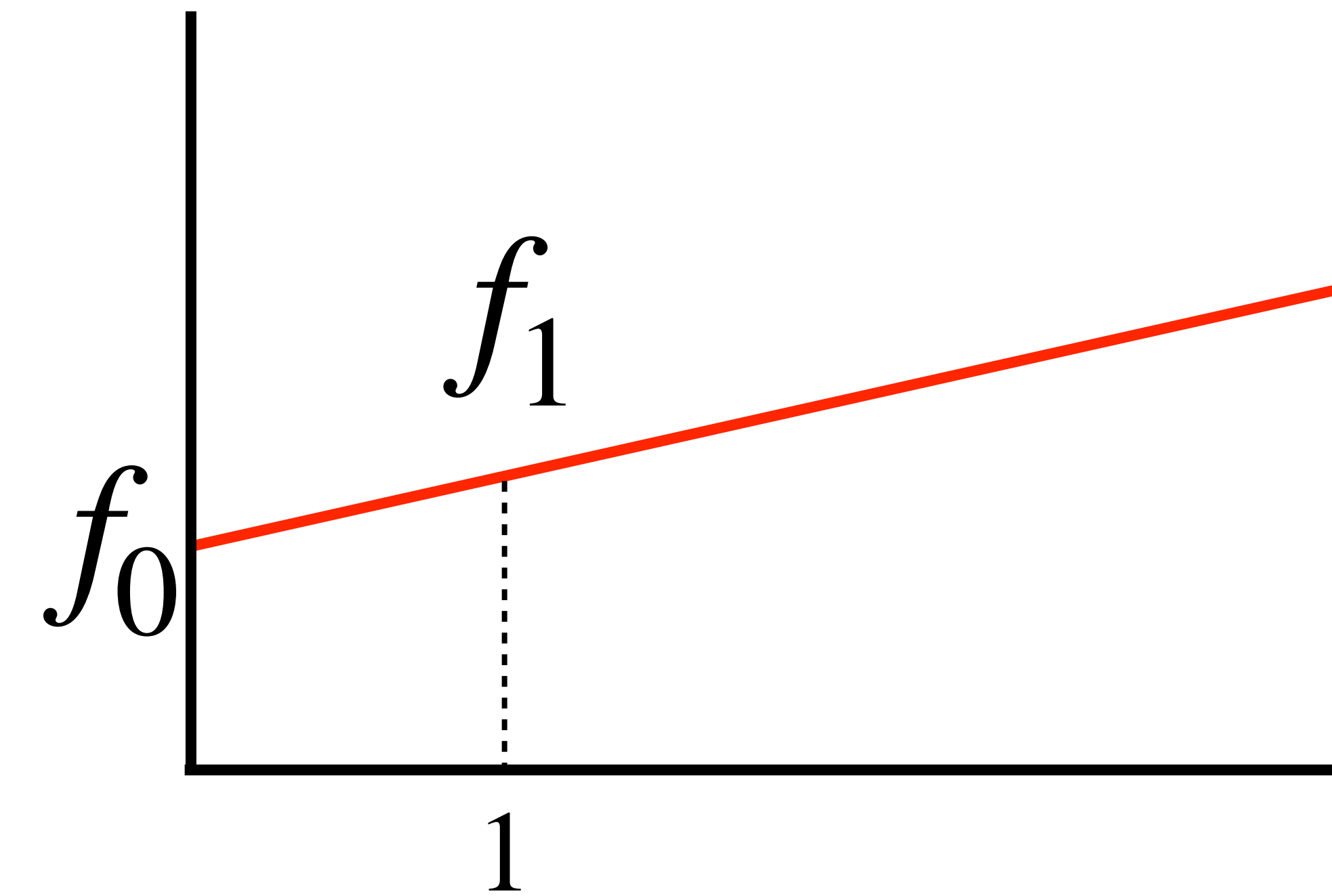


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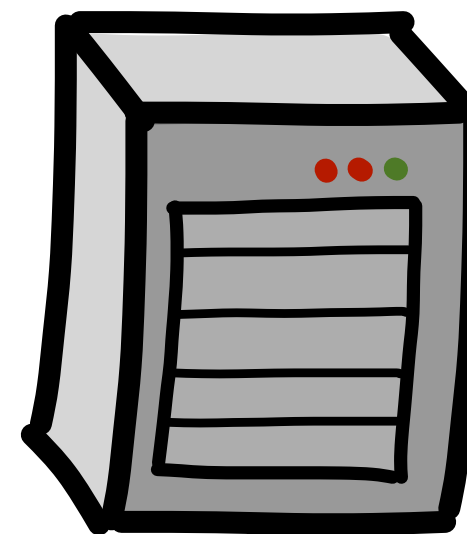
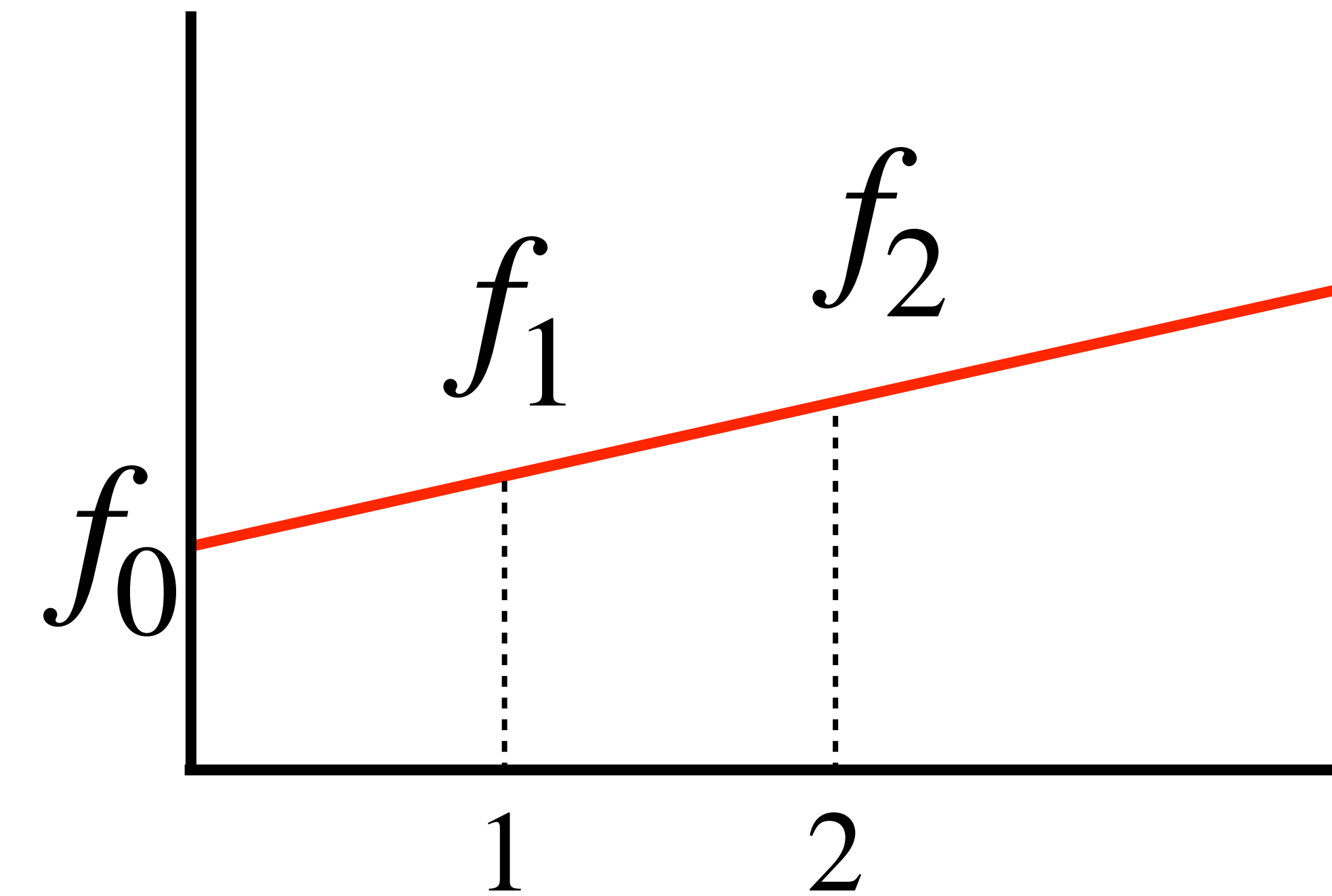


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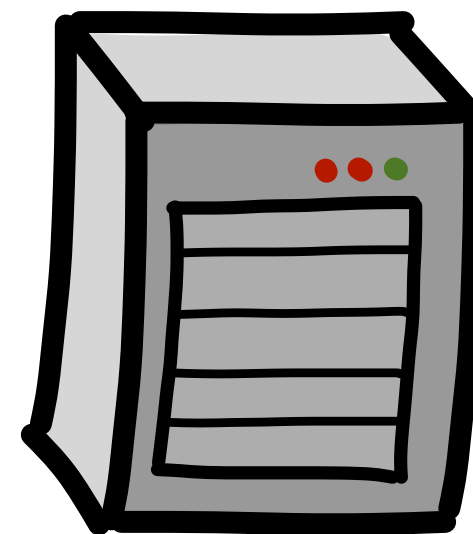
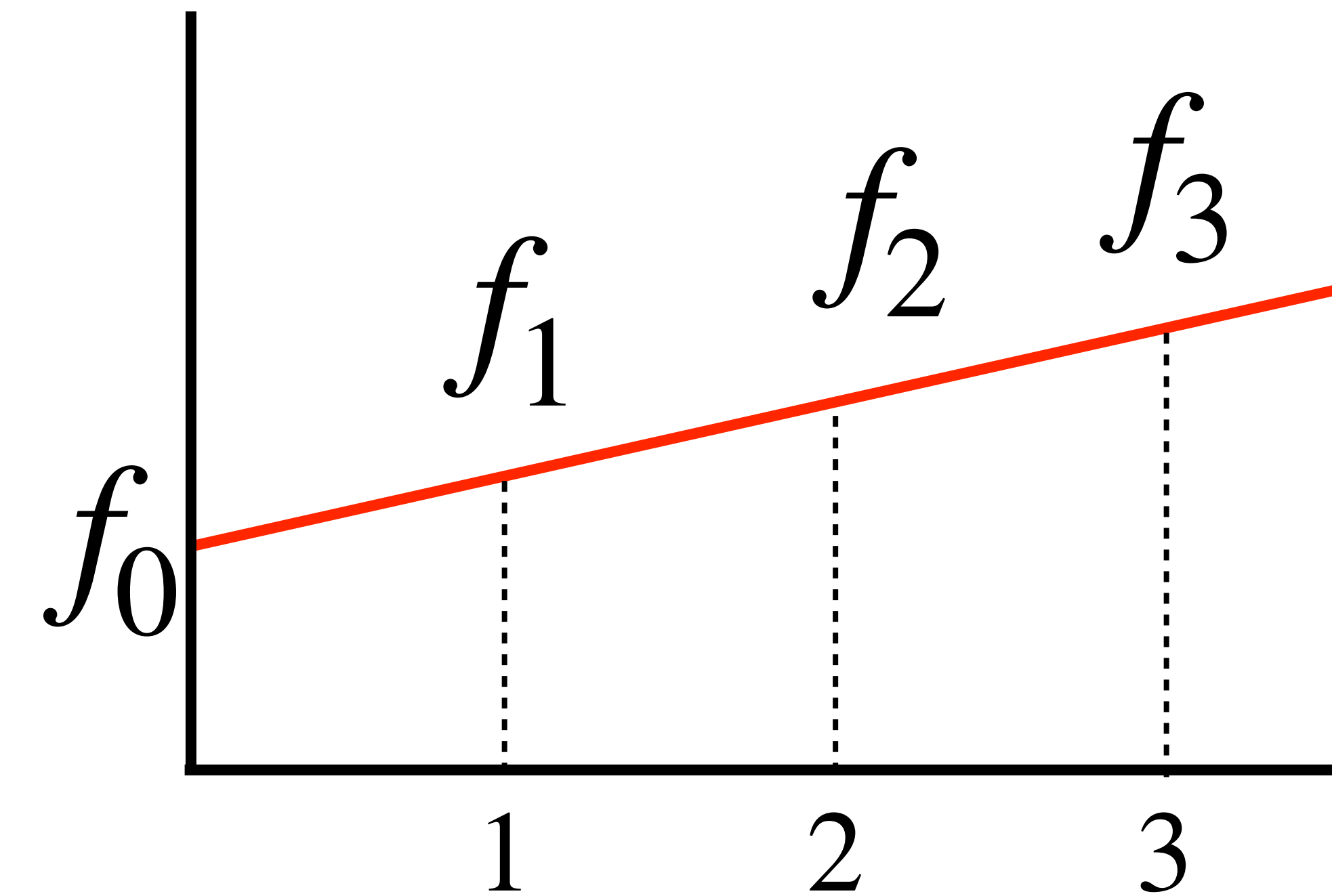


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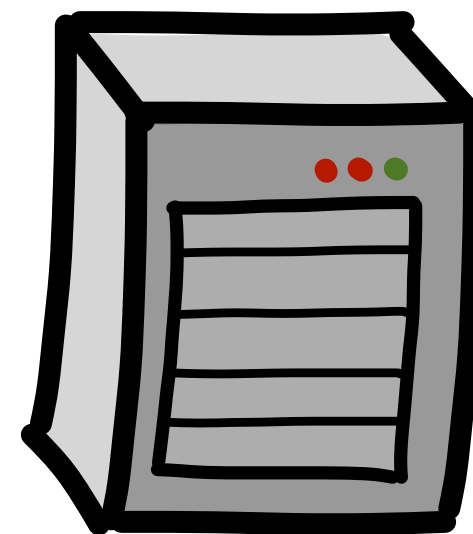
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$f_1$



$f_2$

$f_0$



$f_3$

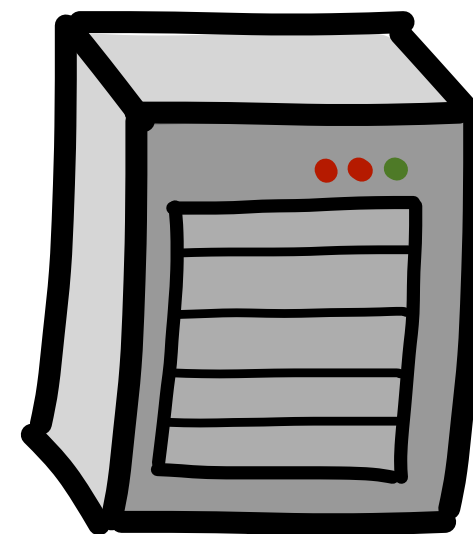
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$f_1$



$f_2$

$sk = f_0$



$f_3$

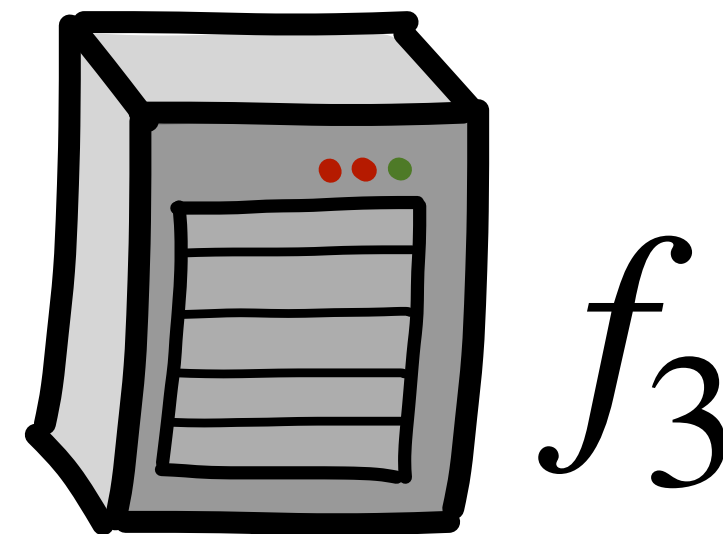
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Enough information to:

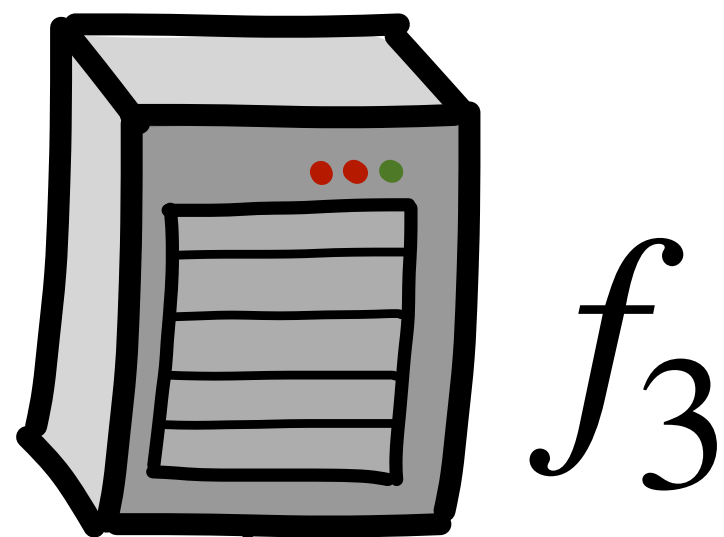
- Sign with two online
- Recover from a crash



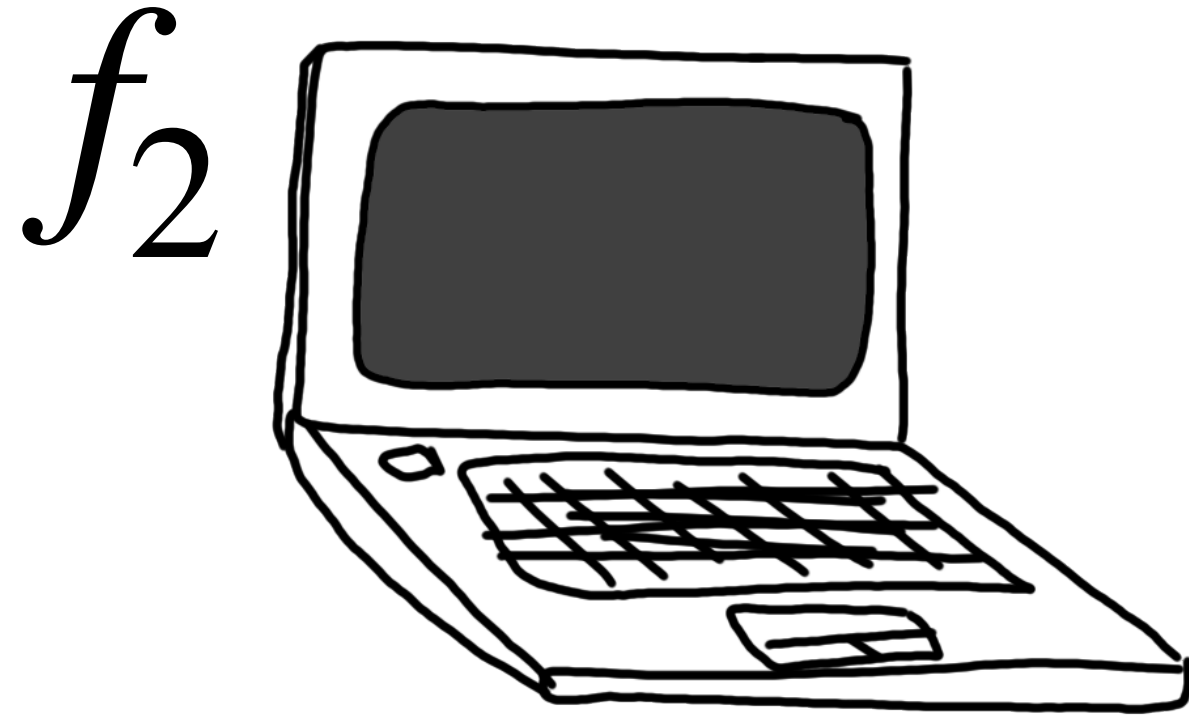
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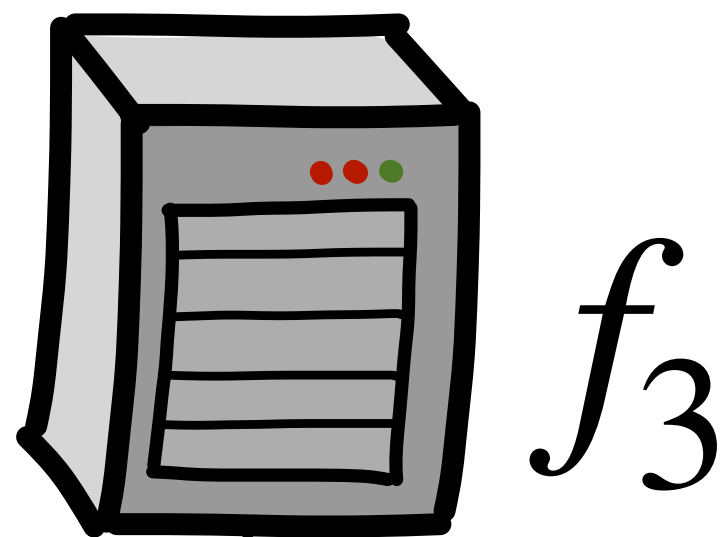
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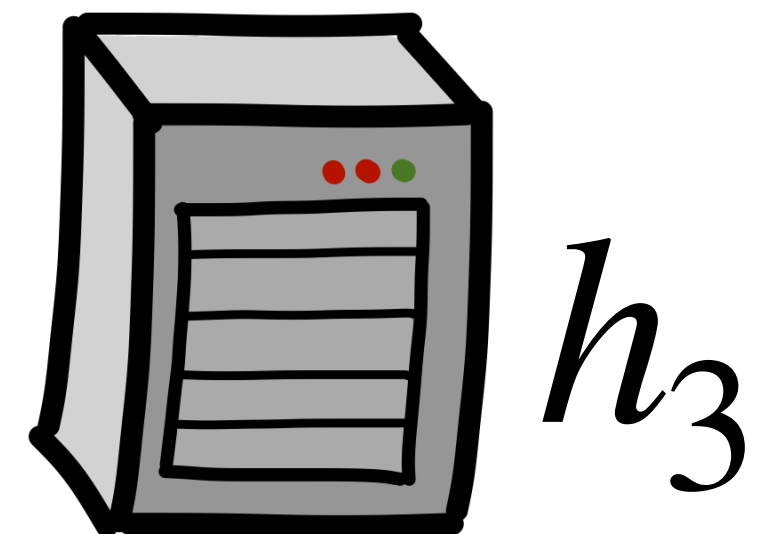
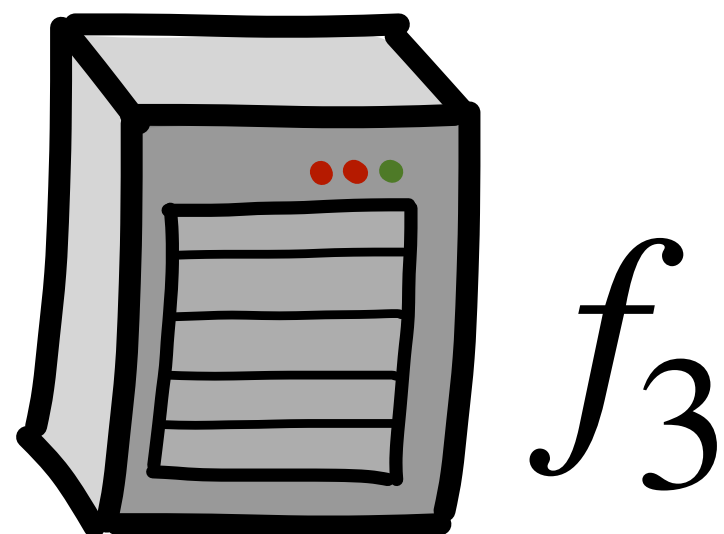
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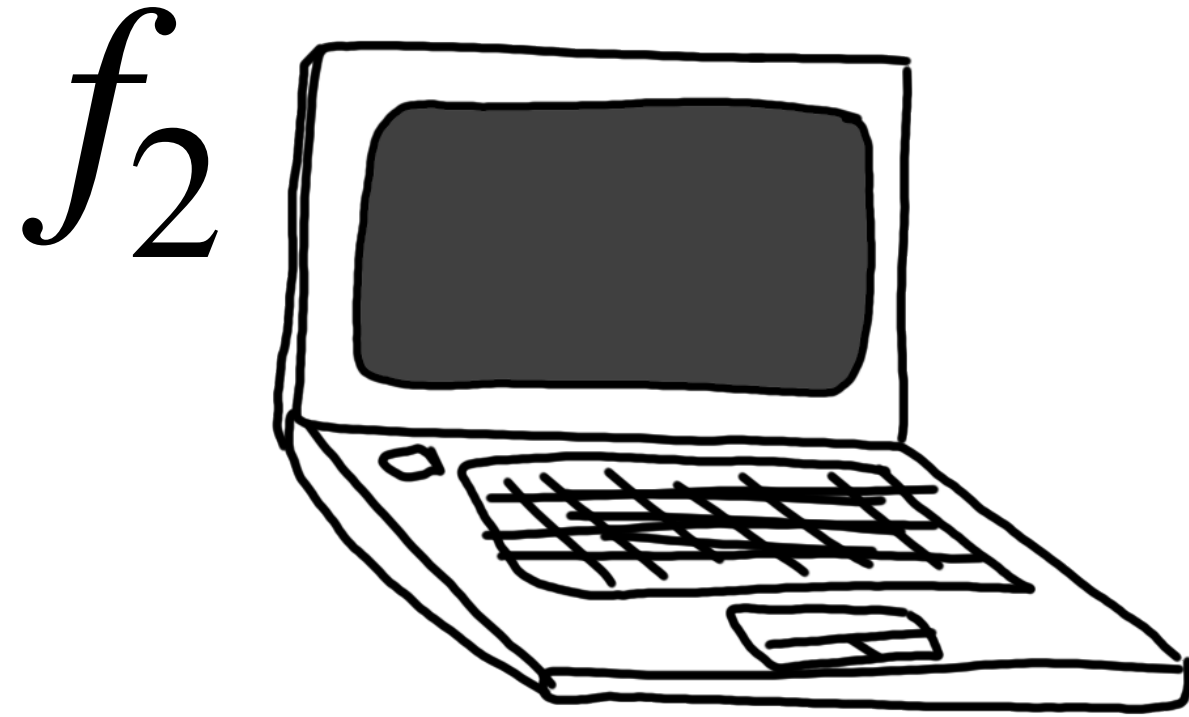
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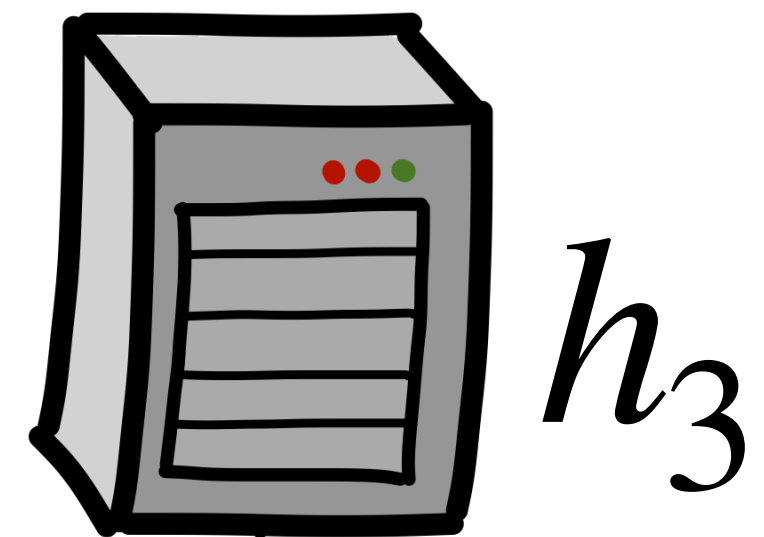
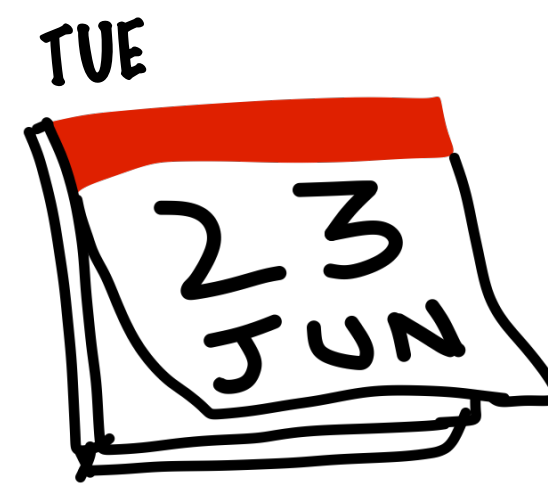
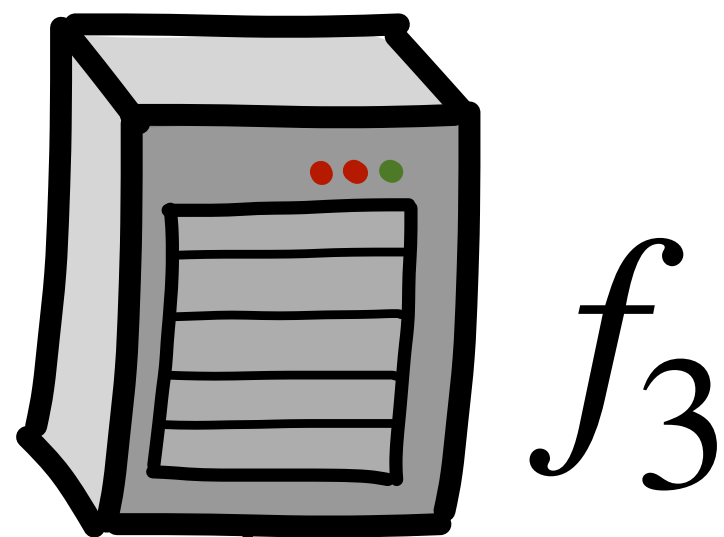
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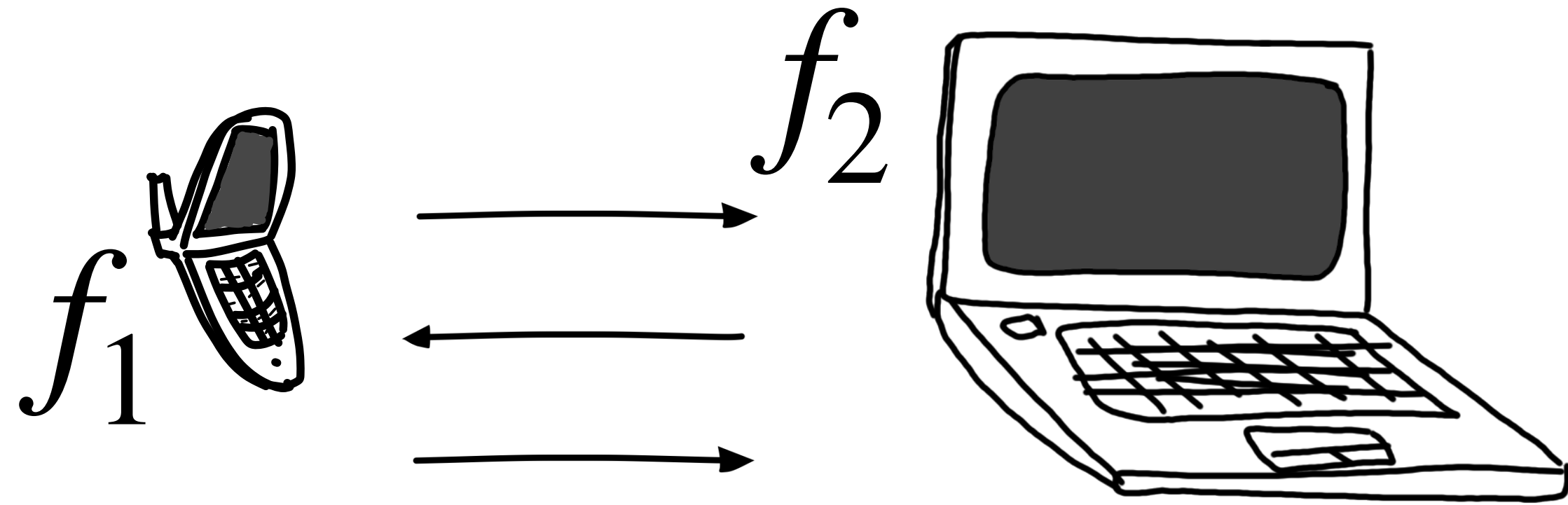
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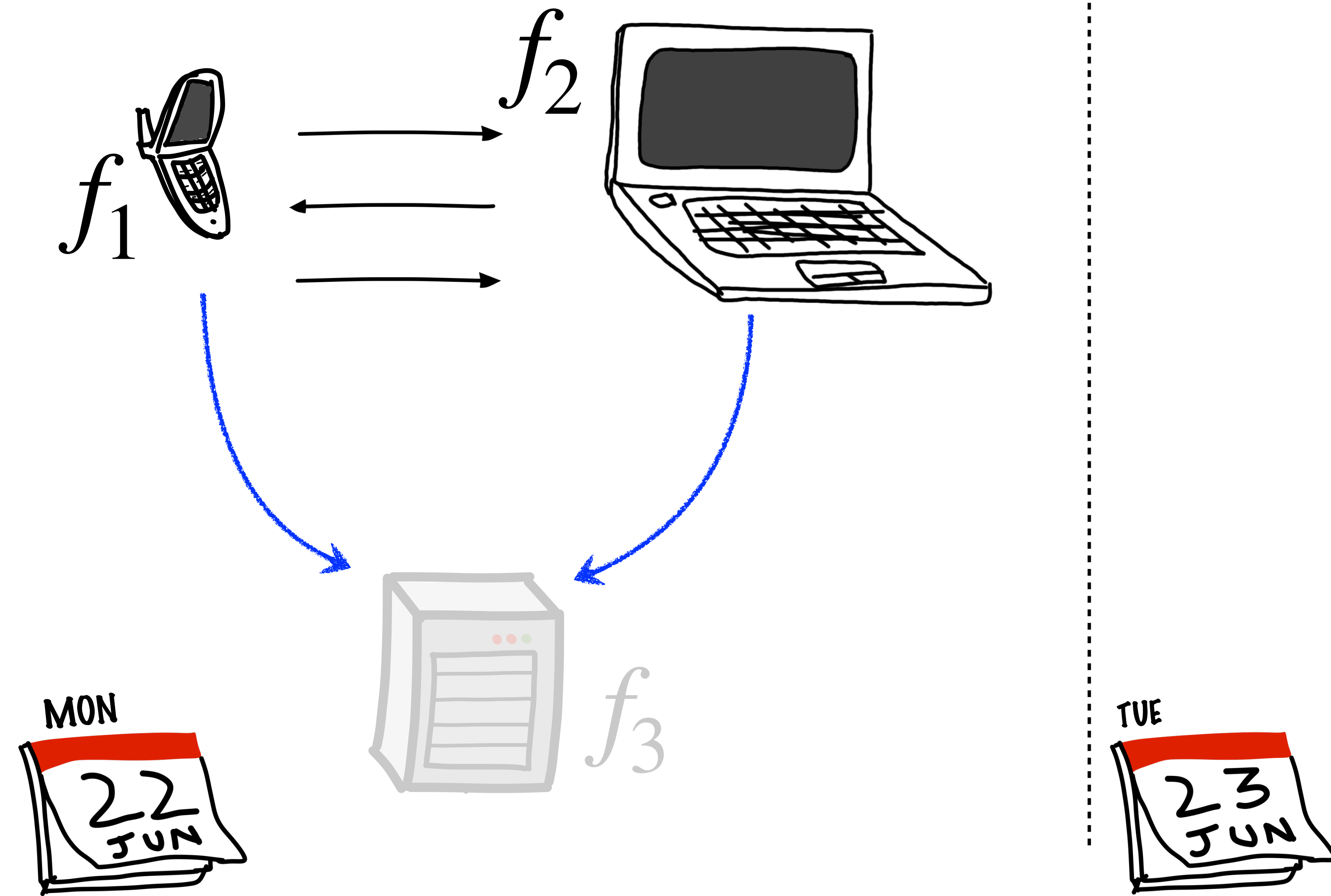
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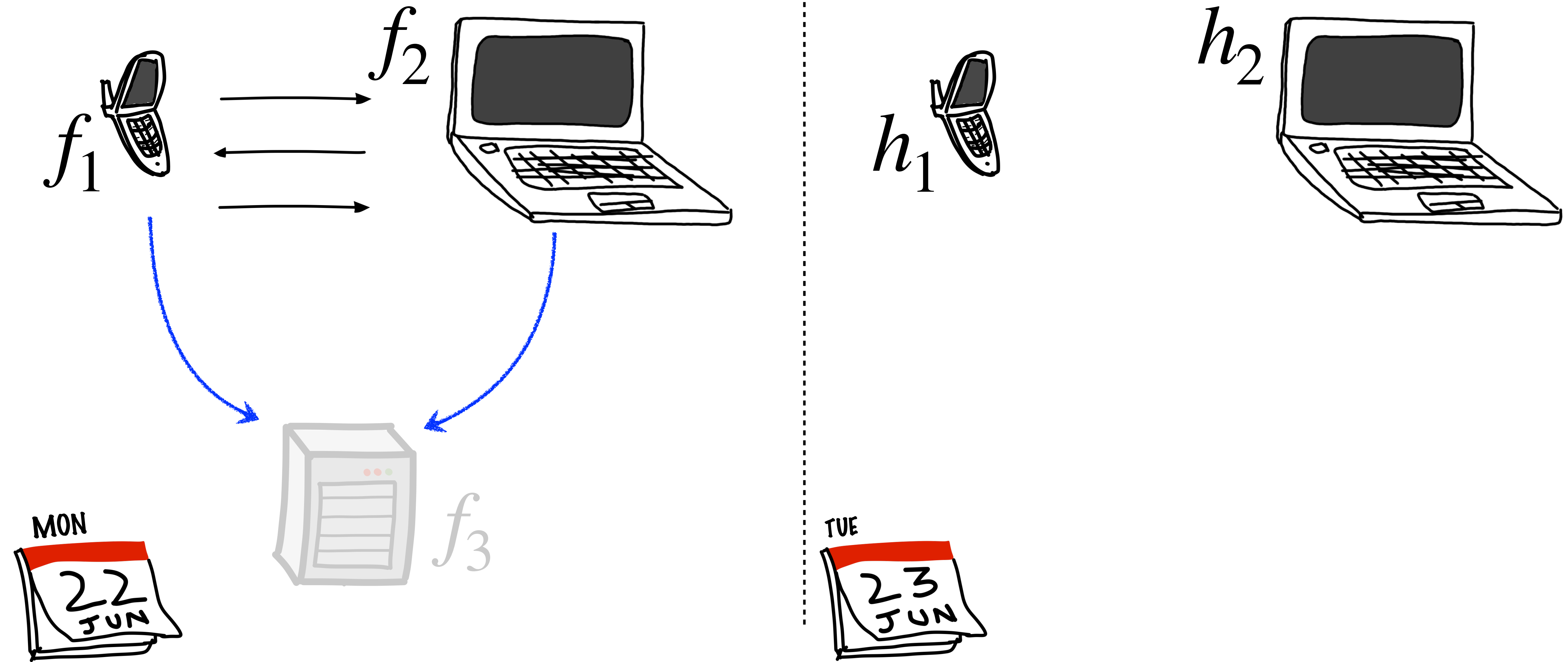
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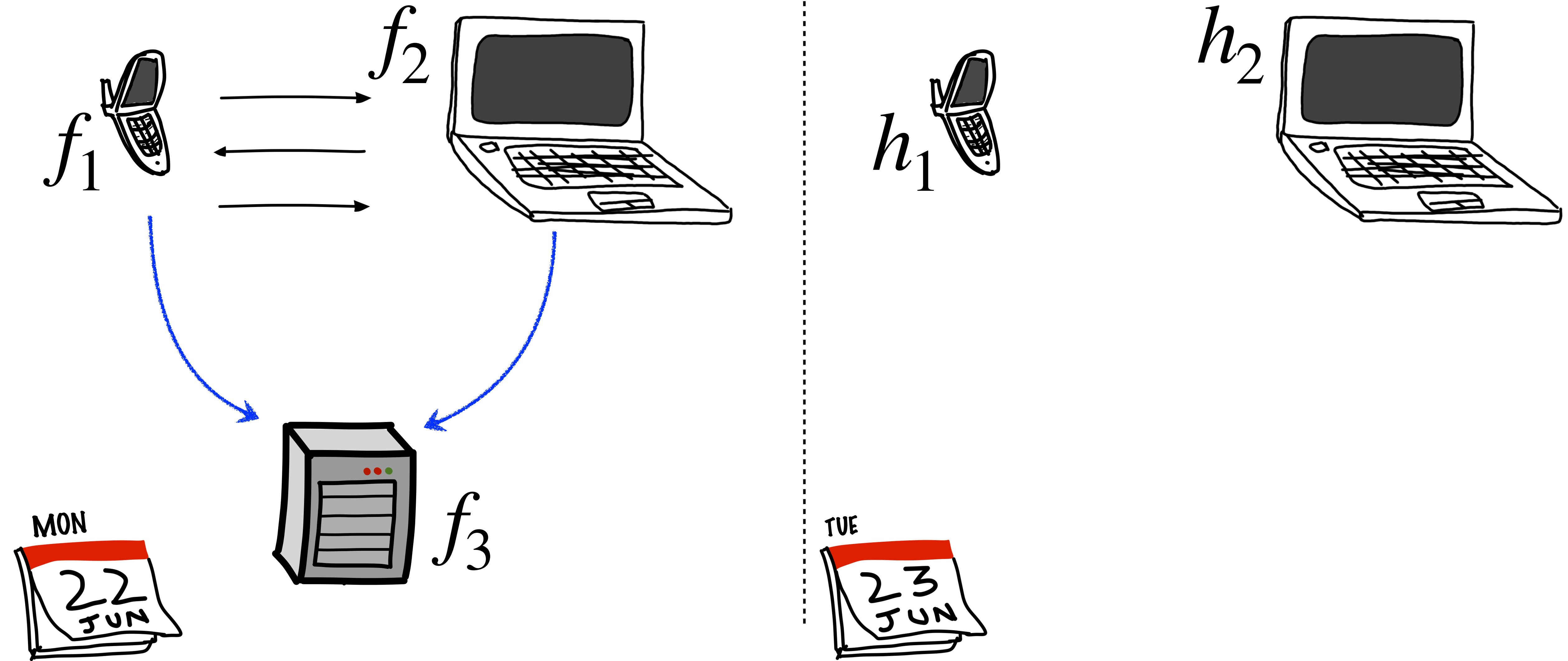
# Defining Offline Refresh



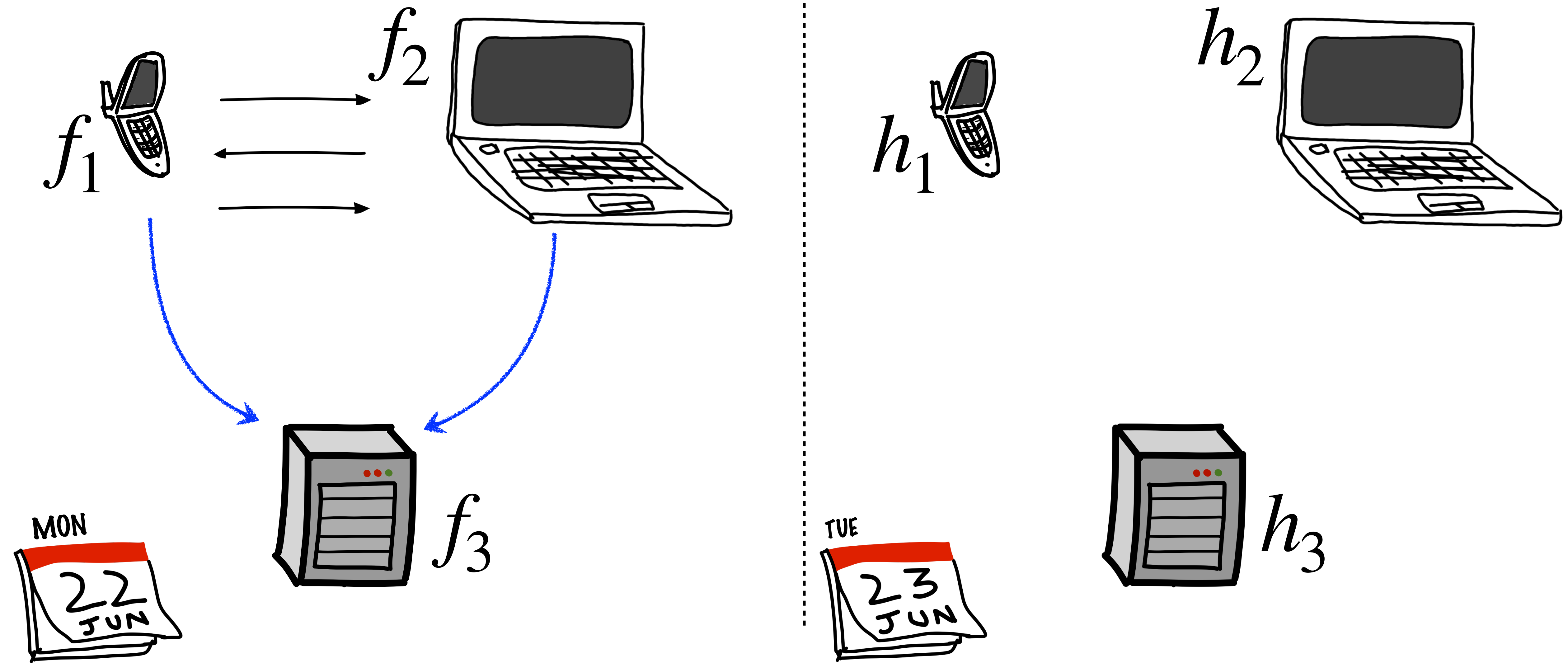
# Defining Offline Refresh



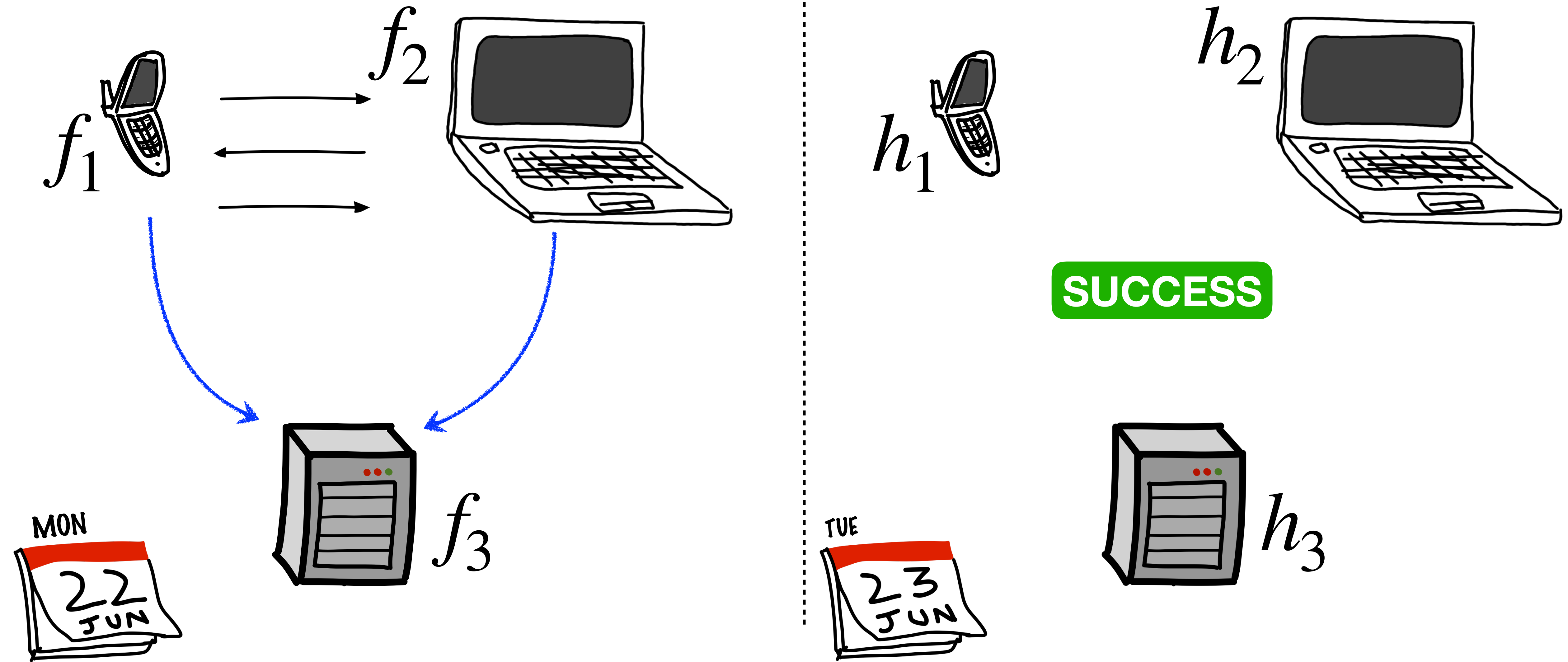
# Defining Offline Refresh



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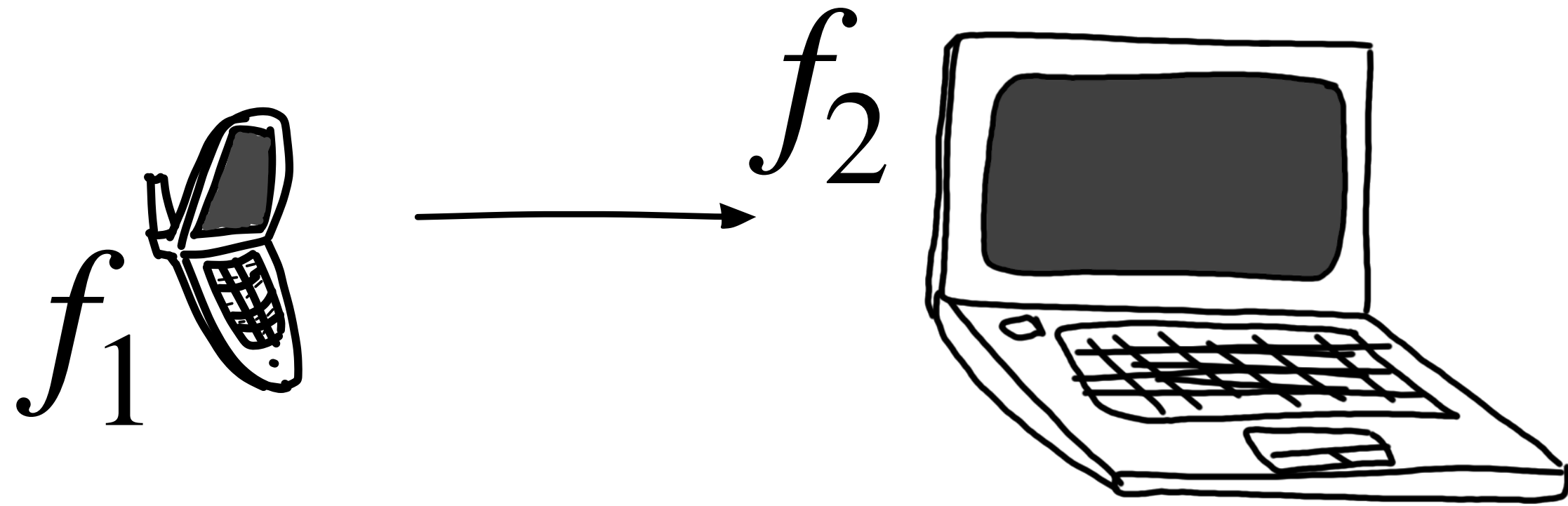
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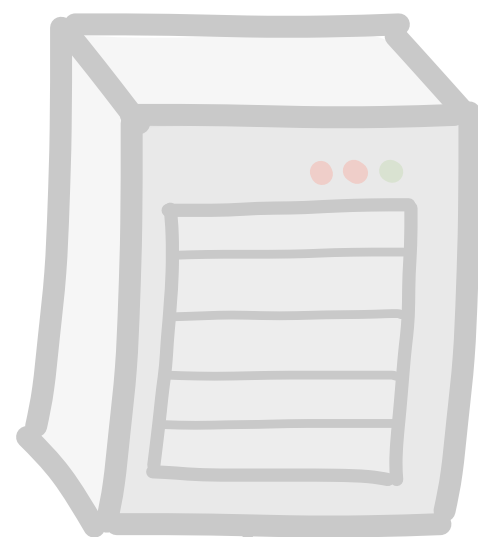
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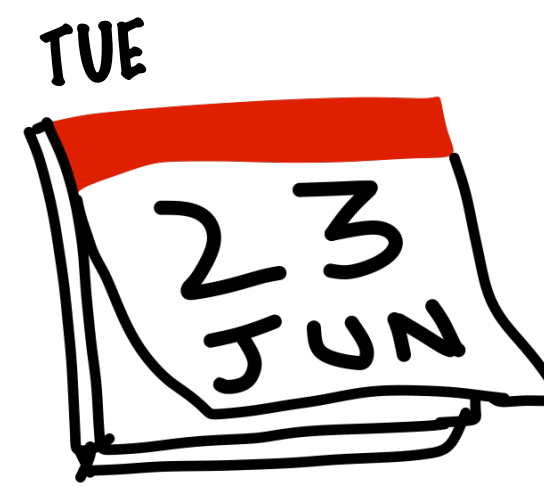
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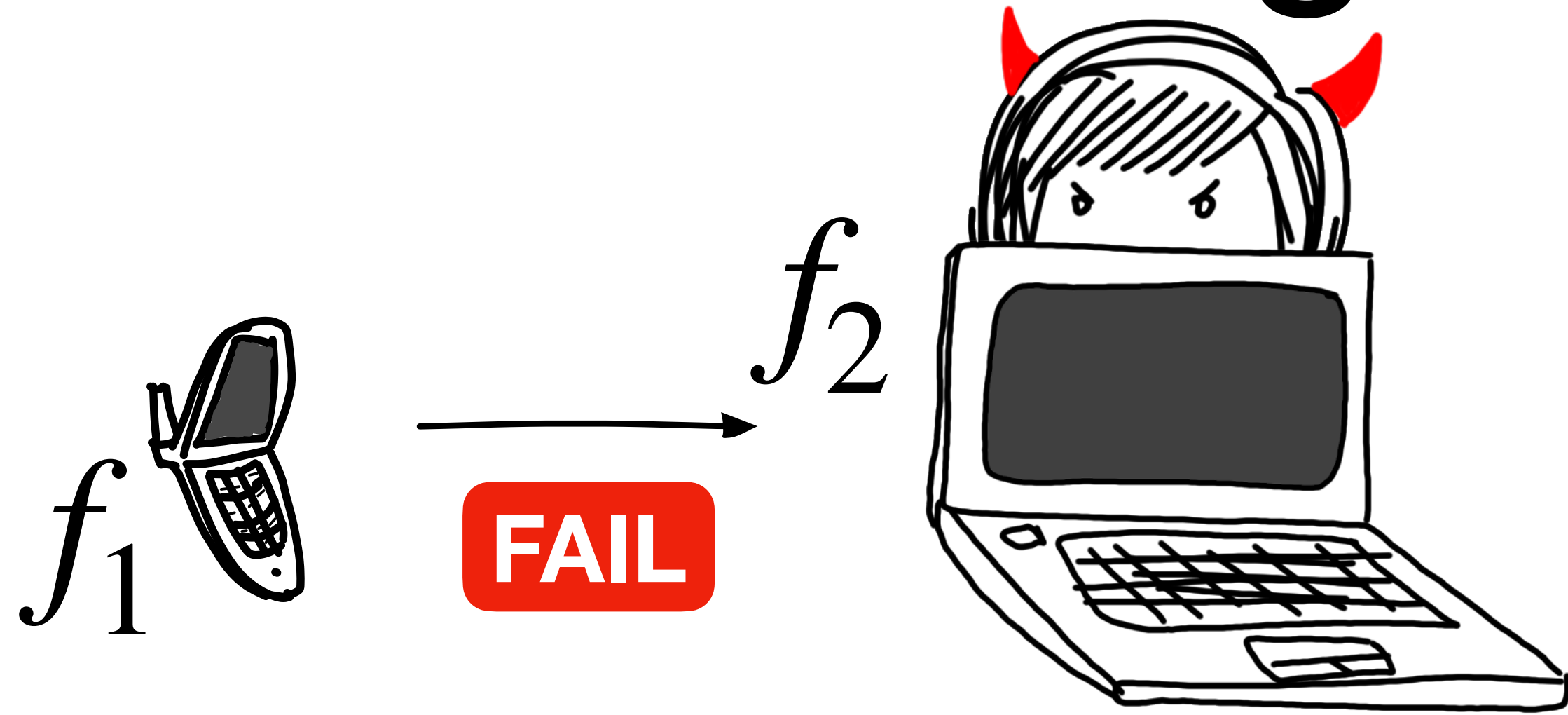
$f_2$



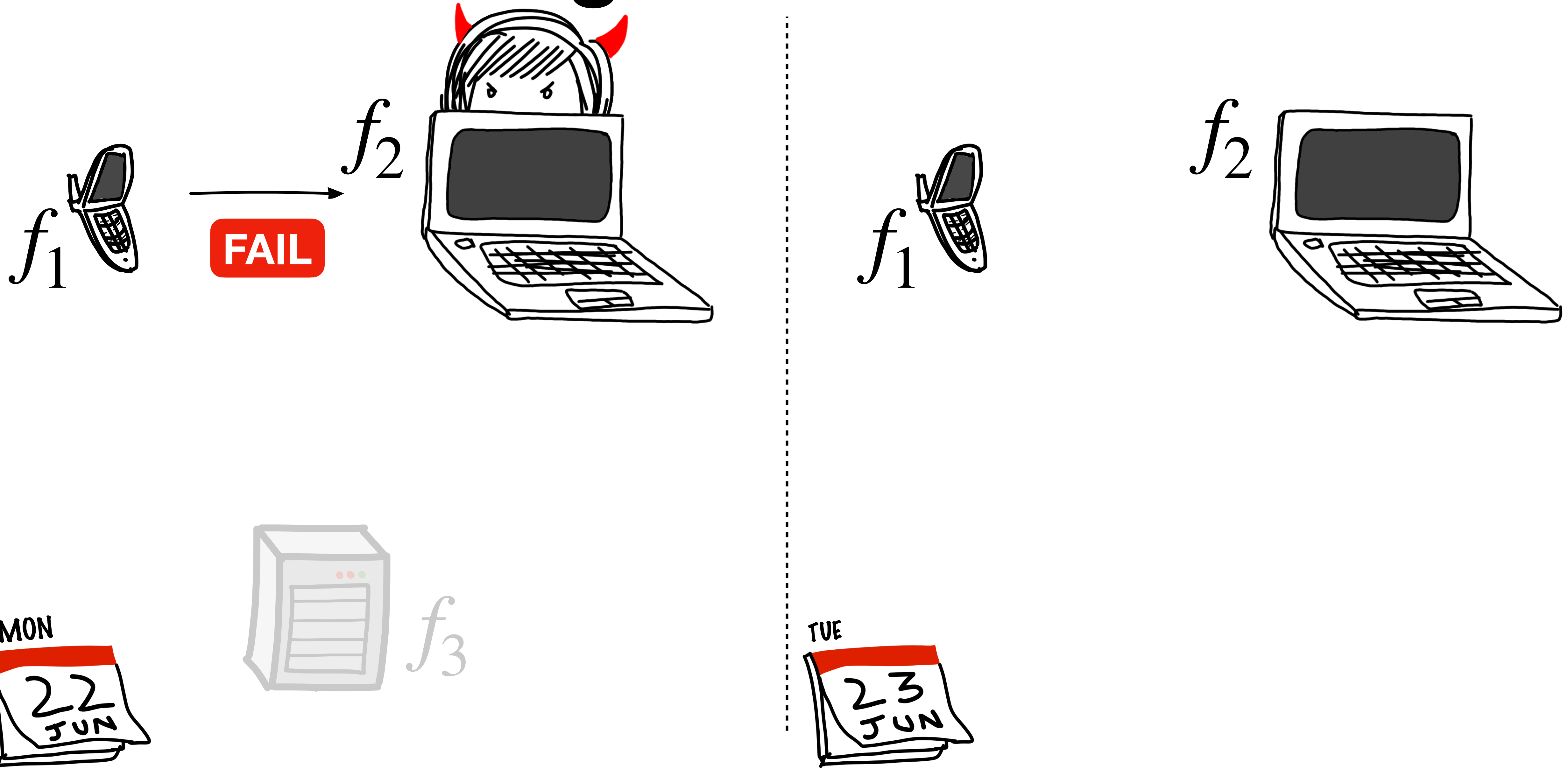
$f_3$



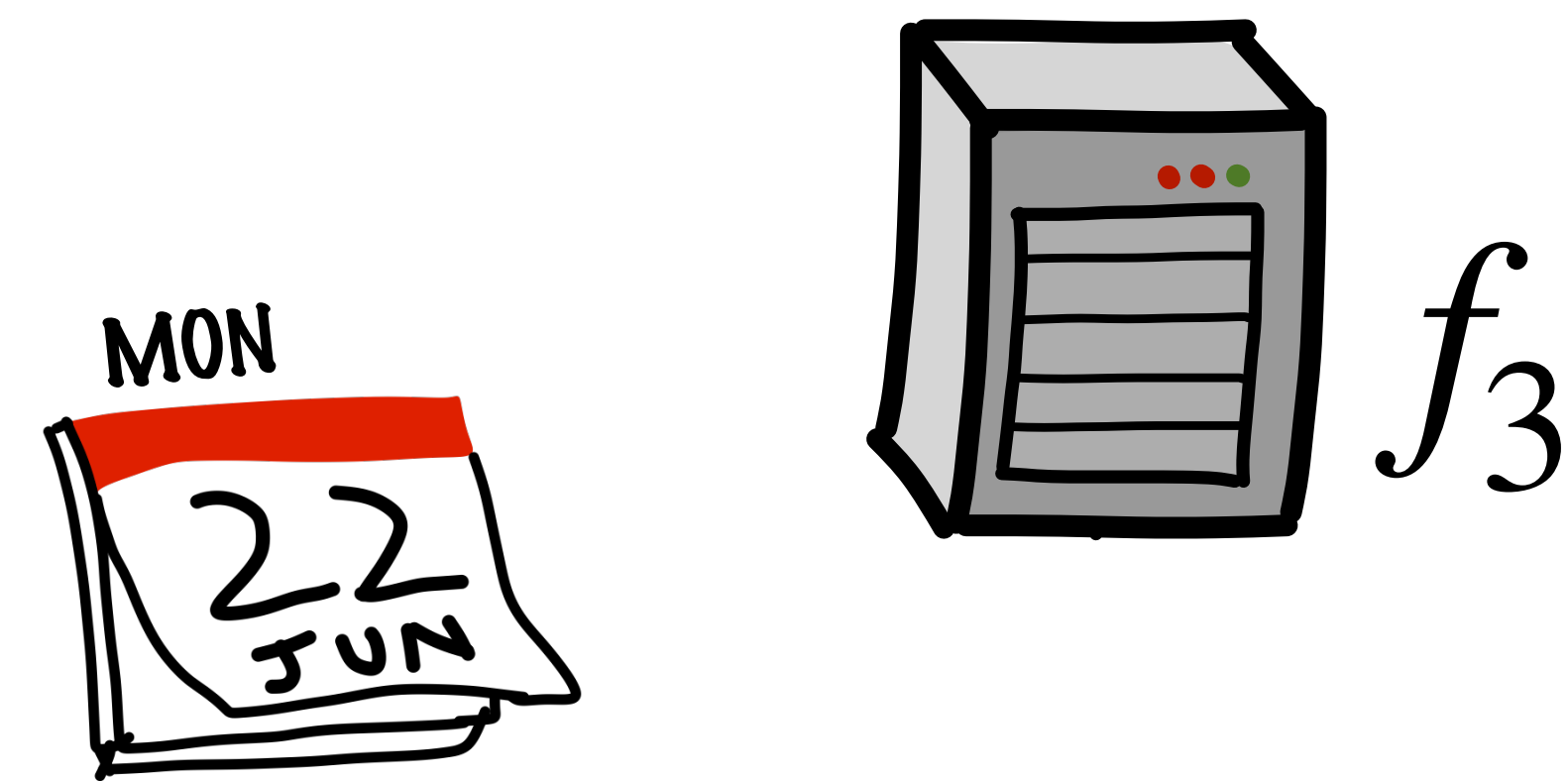
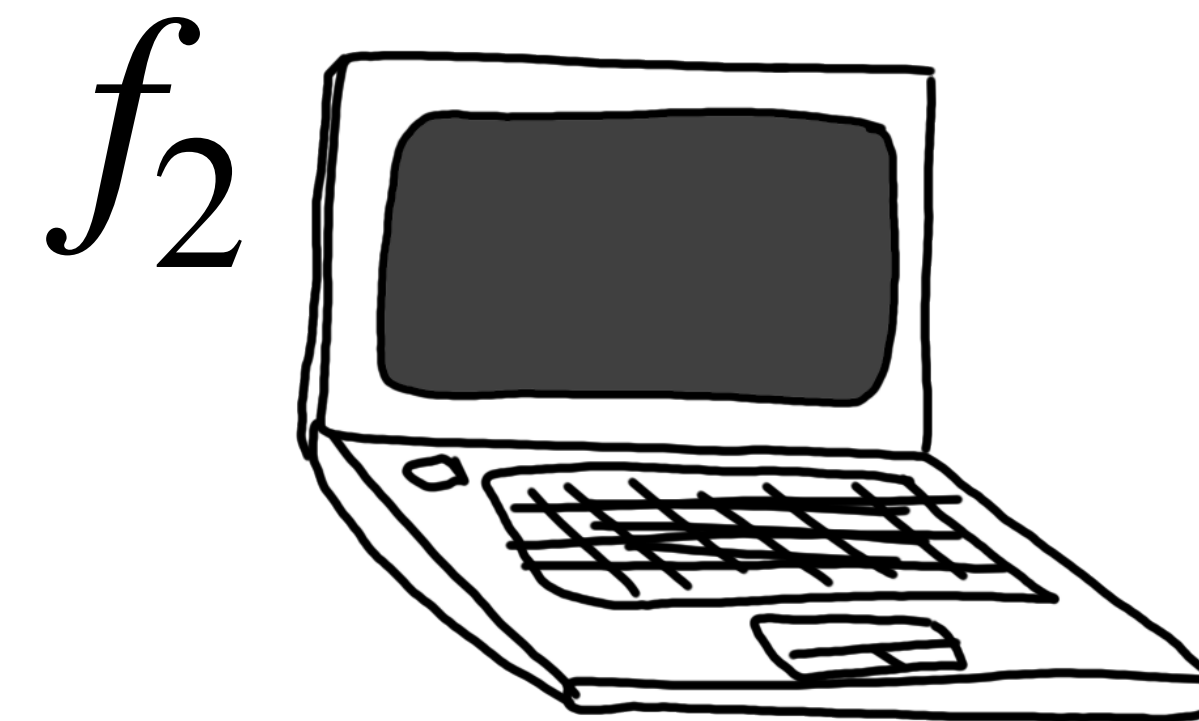
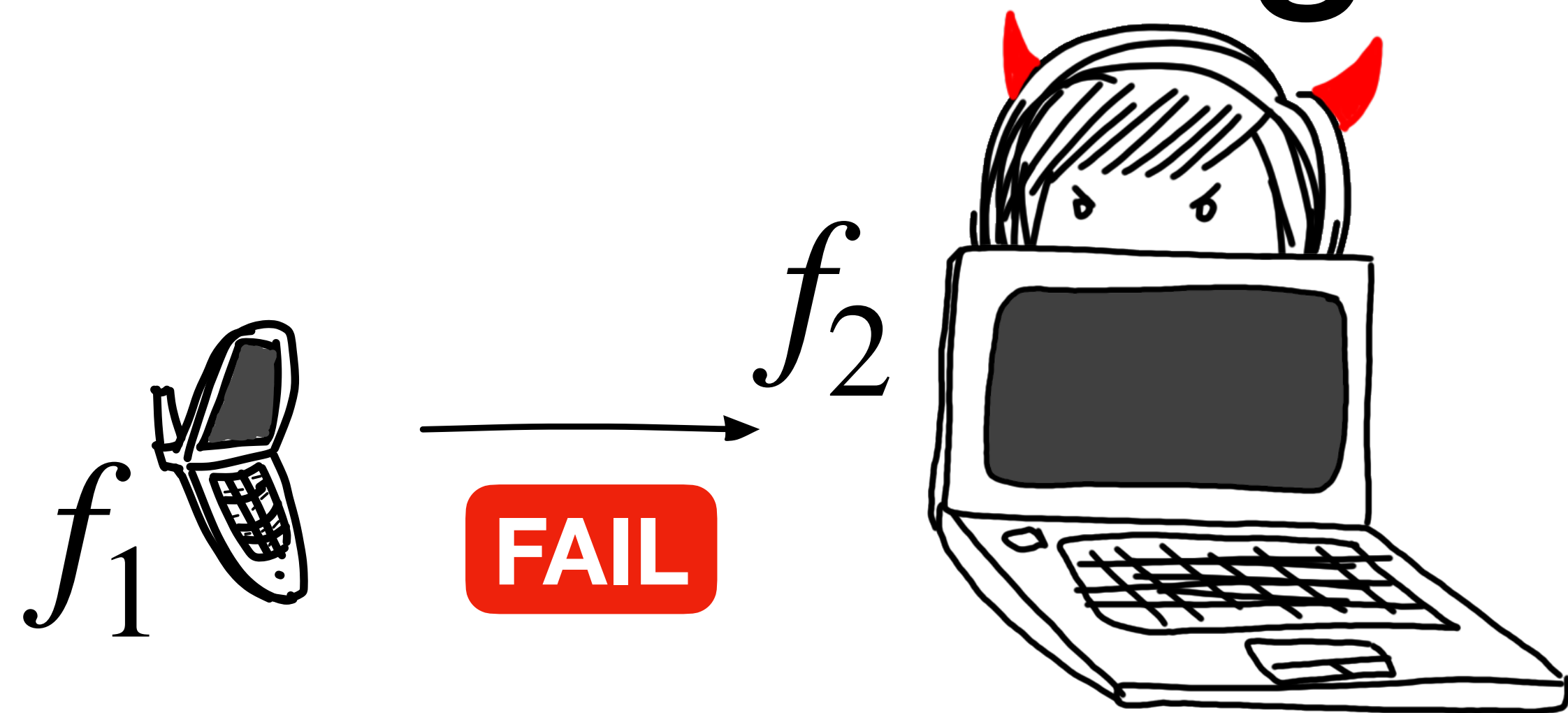
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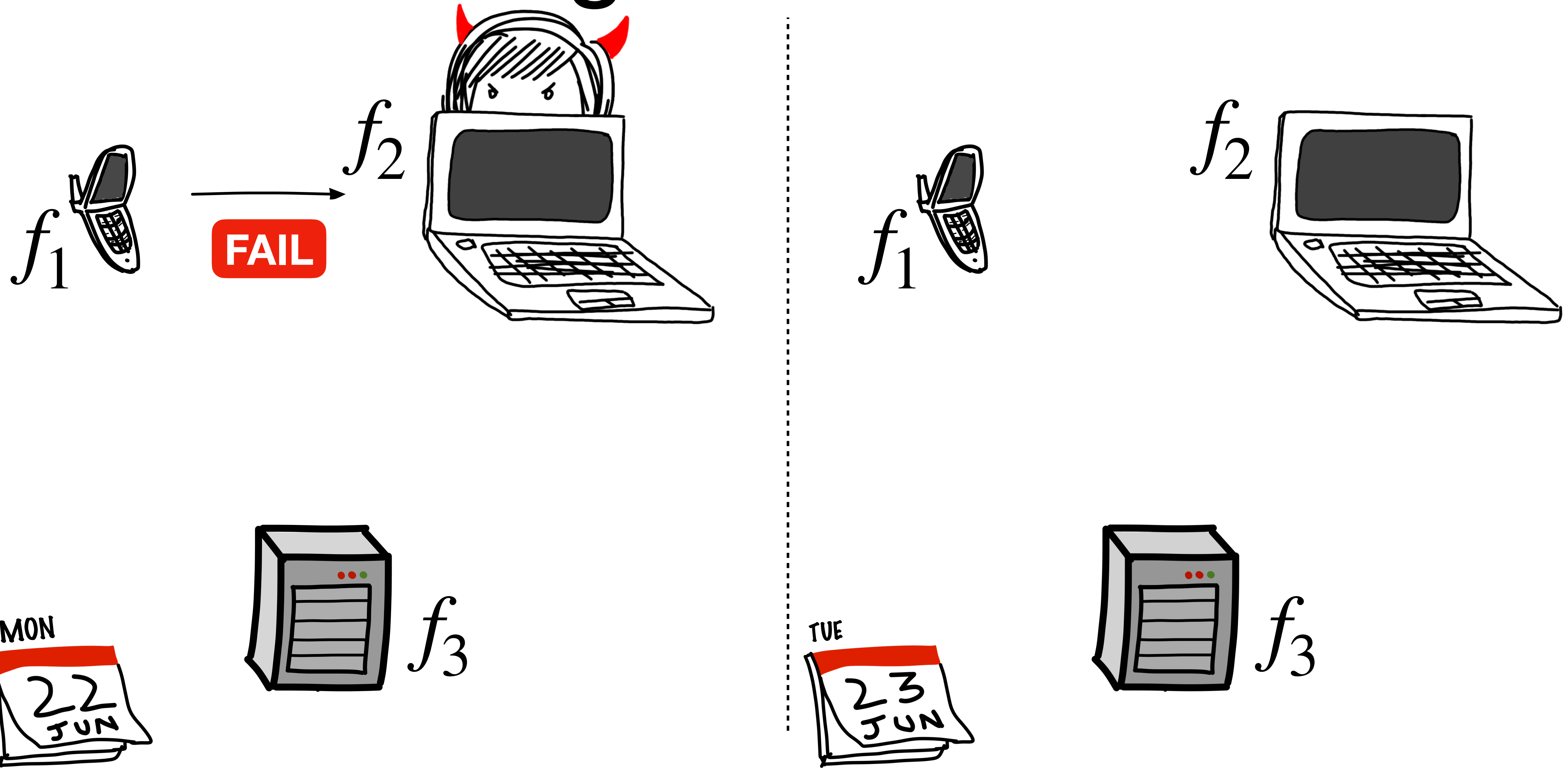
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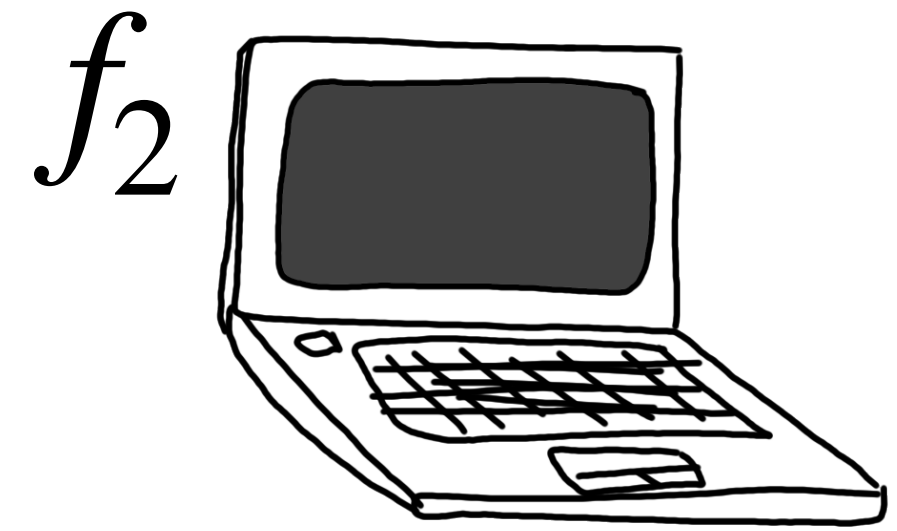
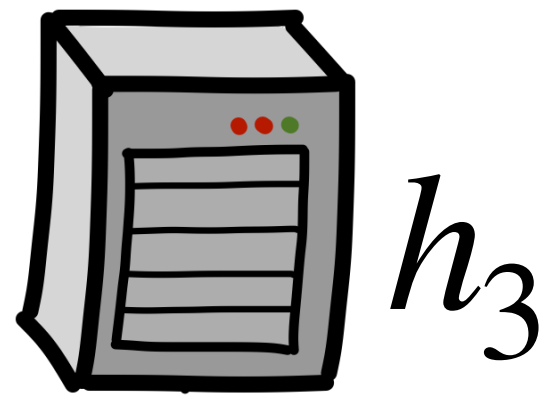
# Defining Offline Refresh



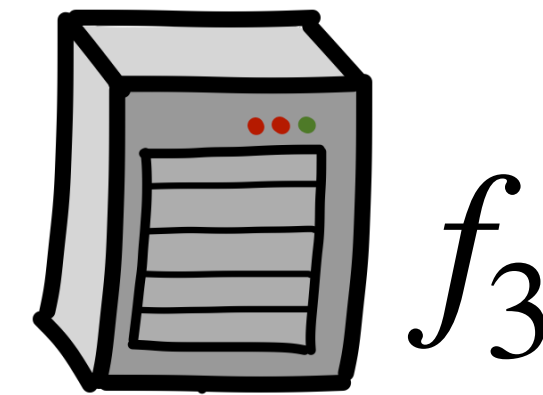
# Defining Offline Refresh



**SUCCESS**



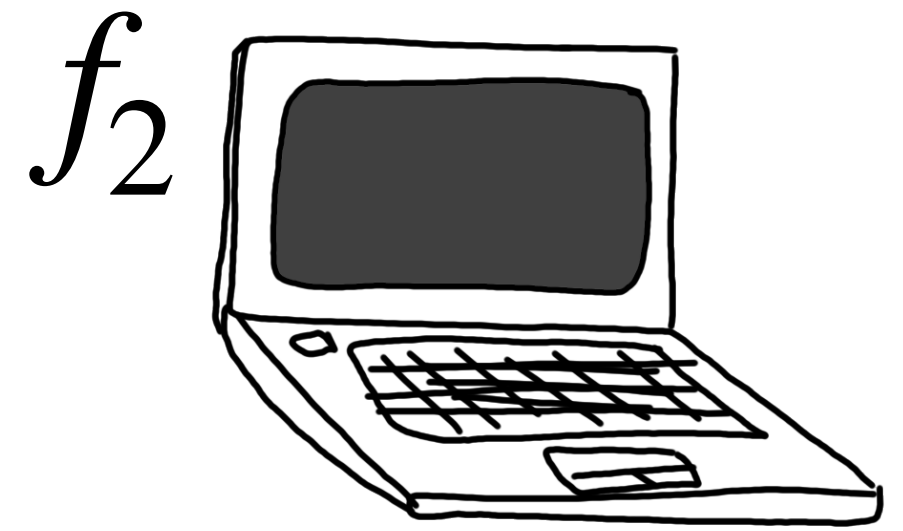
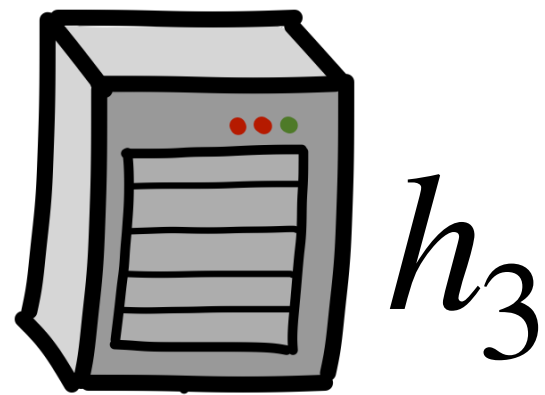
**FAIL**



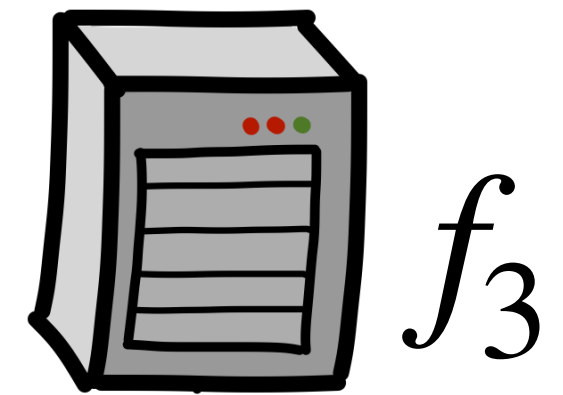
# Defining Offline Refresh



**SUCCESS**



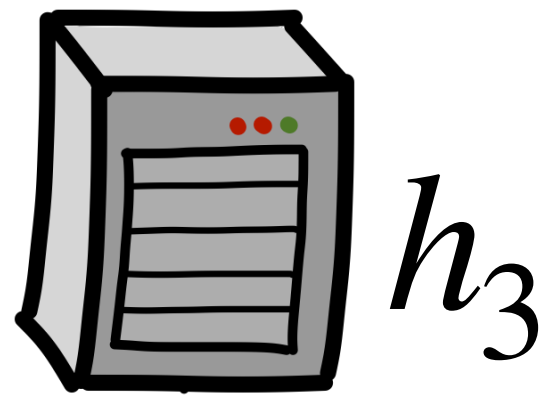
**FAIL**



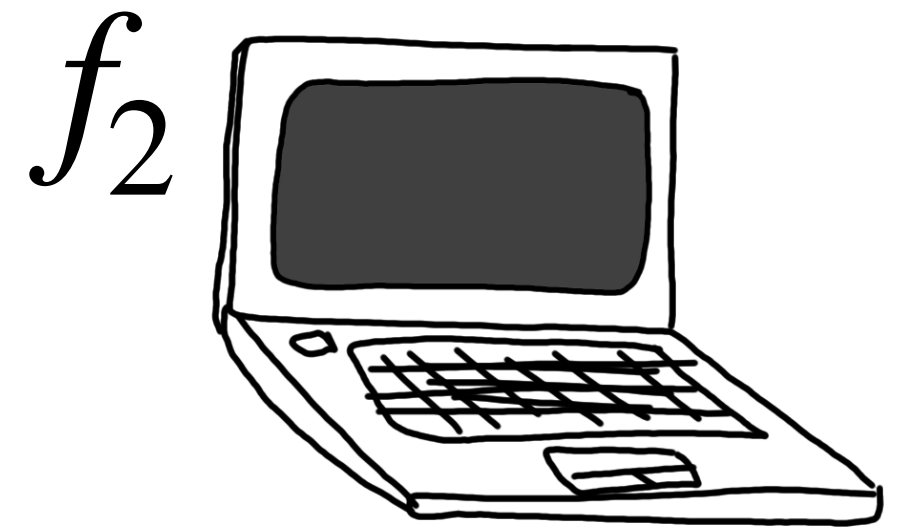
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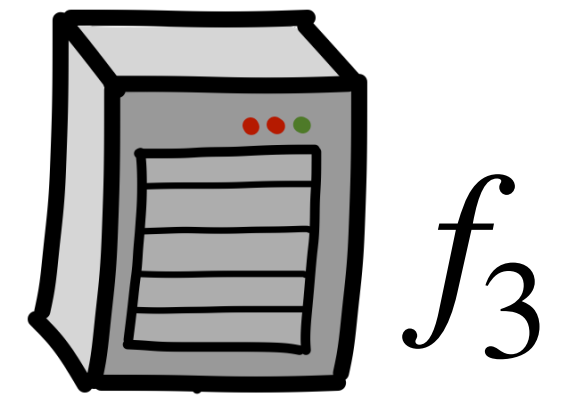
**SUCCESS**



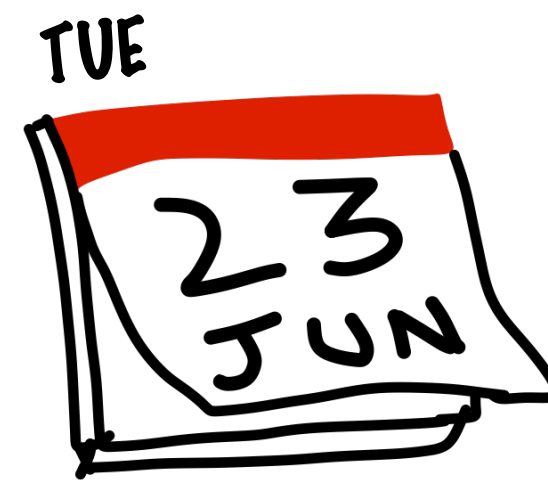
HMMMMMM



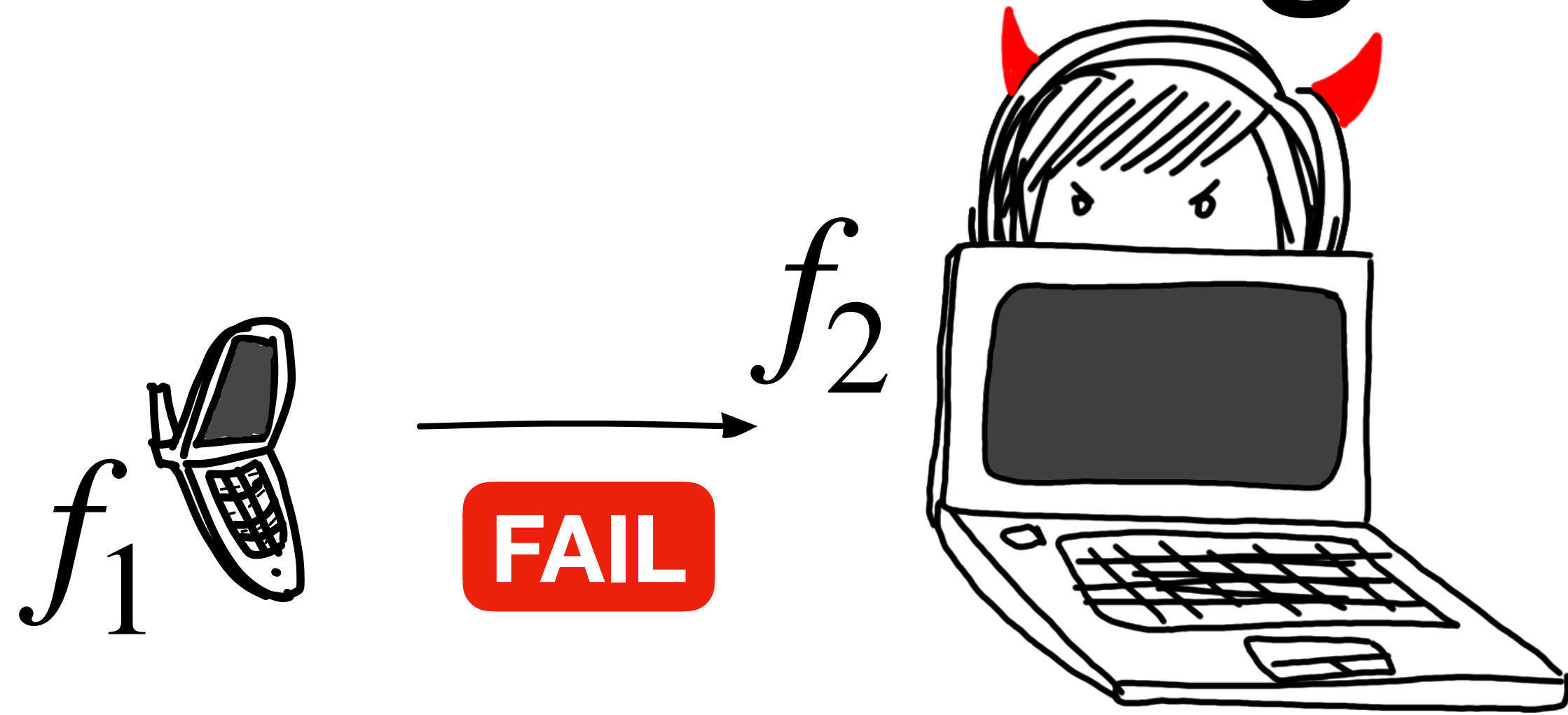
**FAIL**



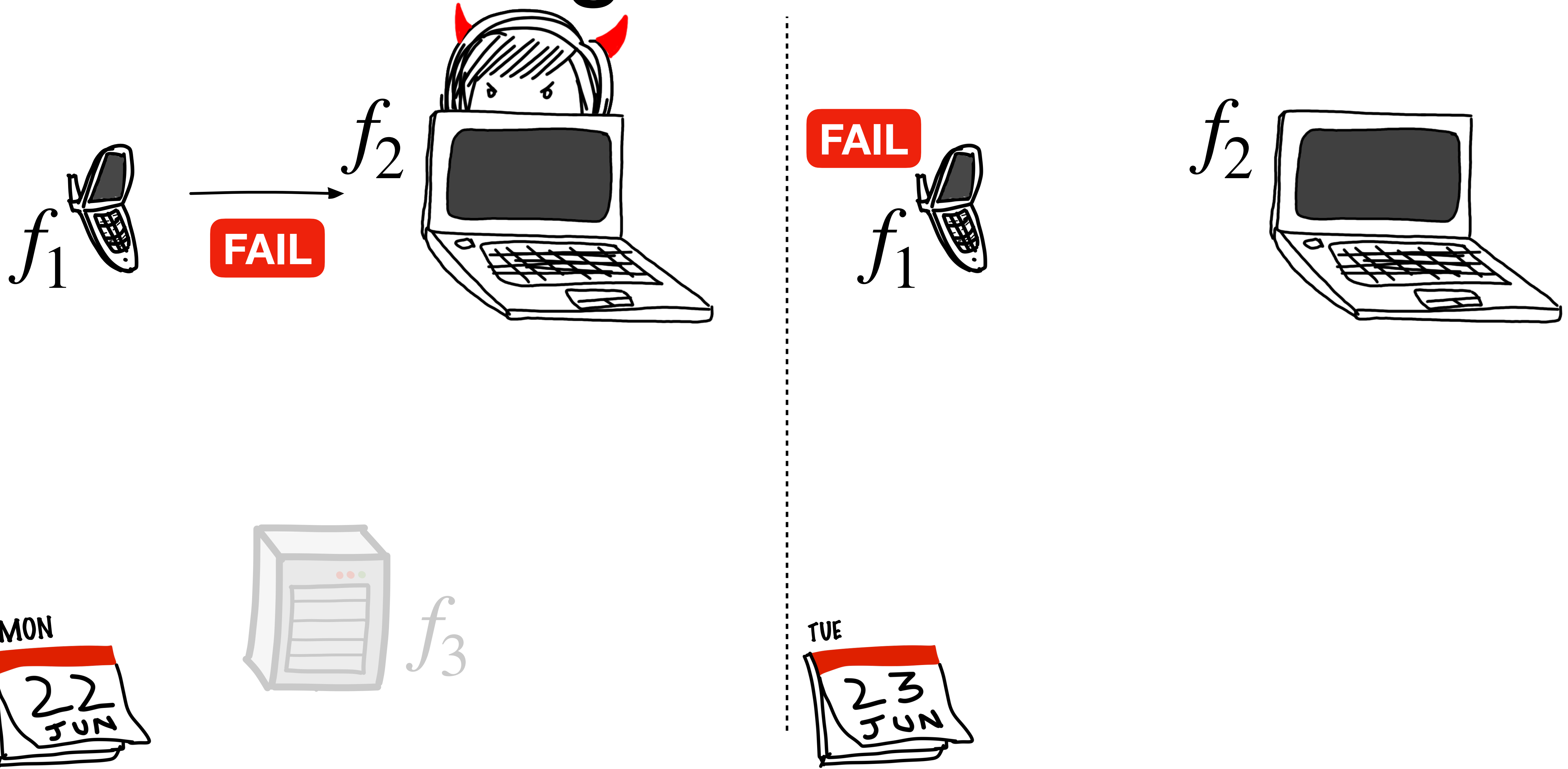
# Defining Offline Refresh



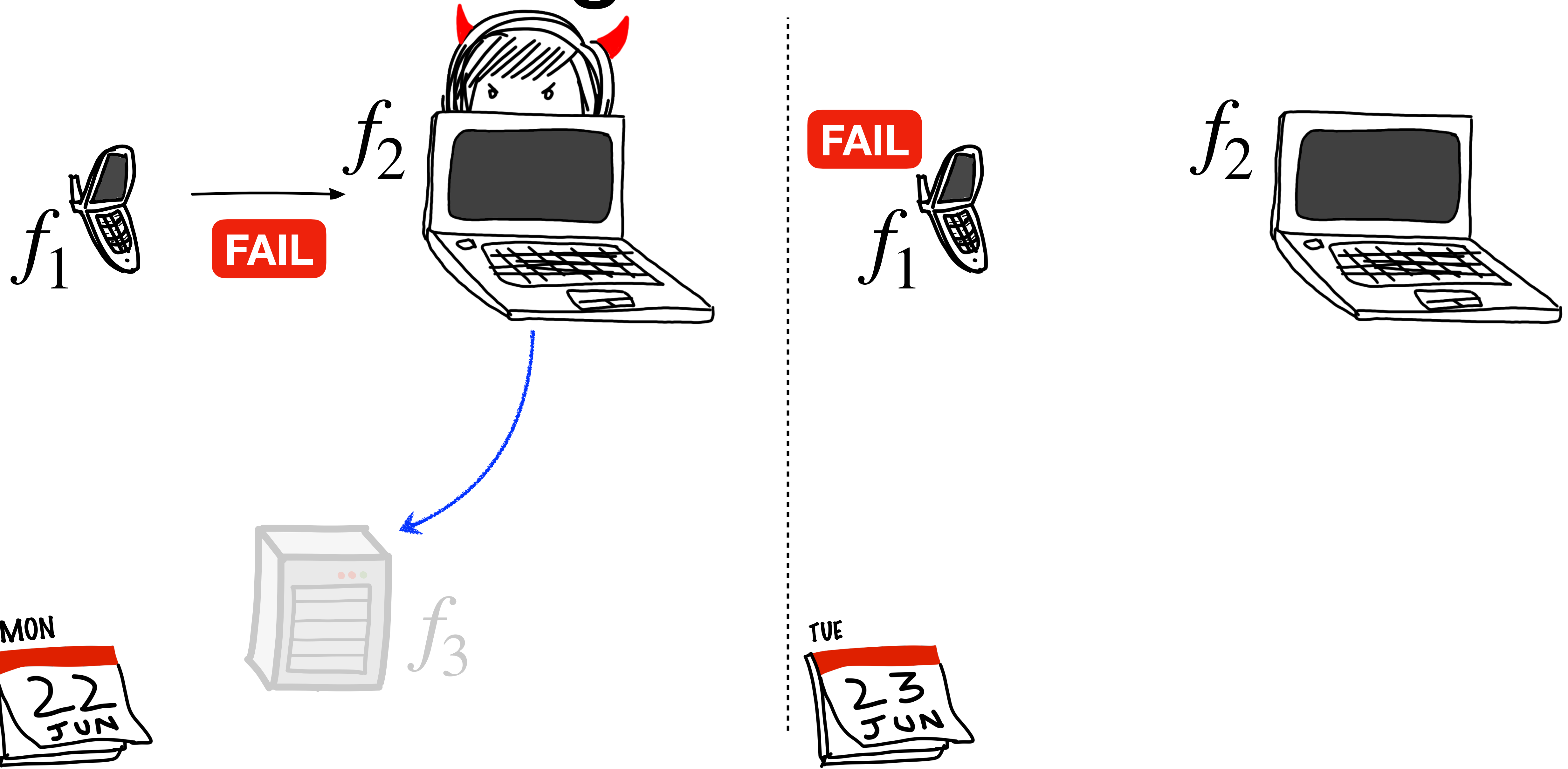
# Defining Offline Refresh



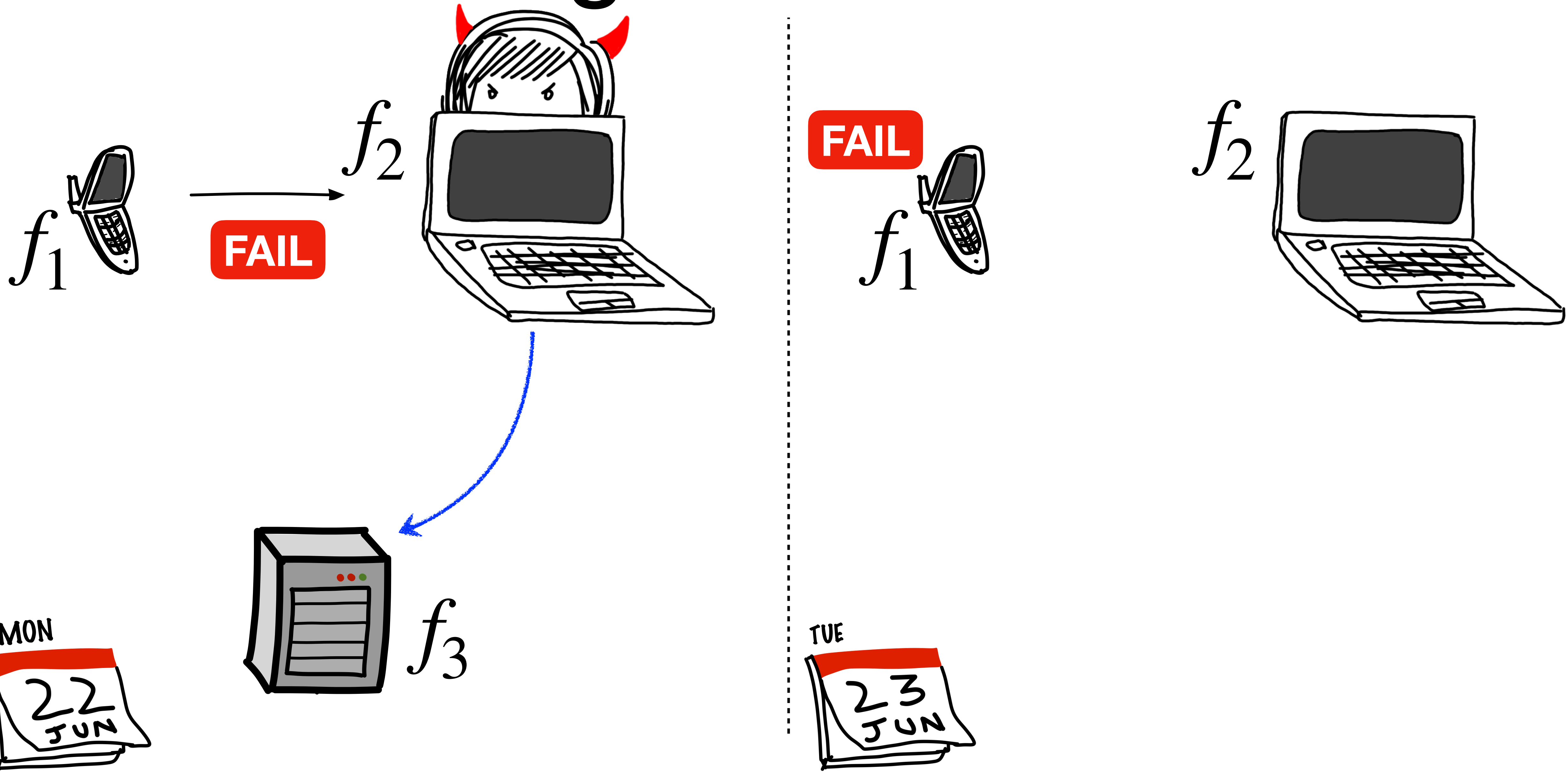
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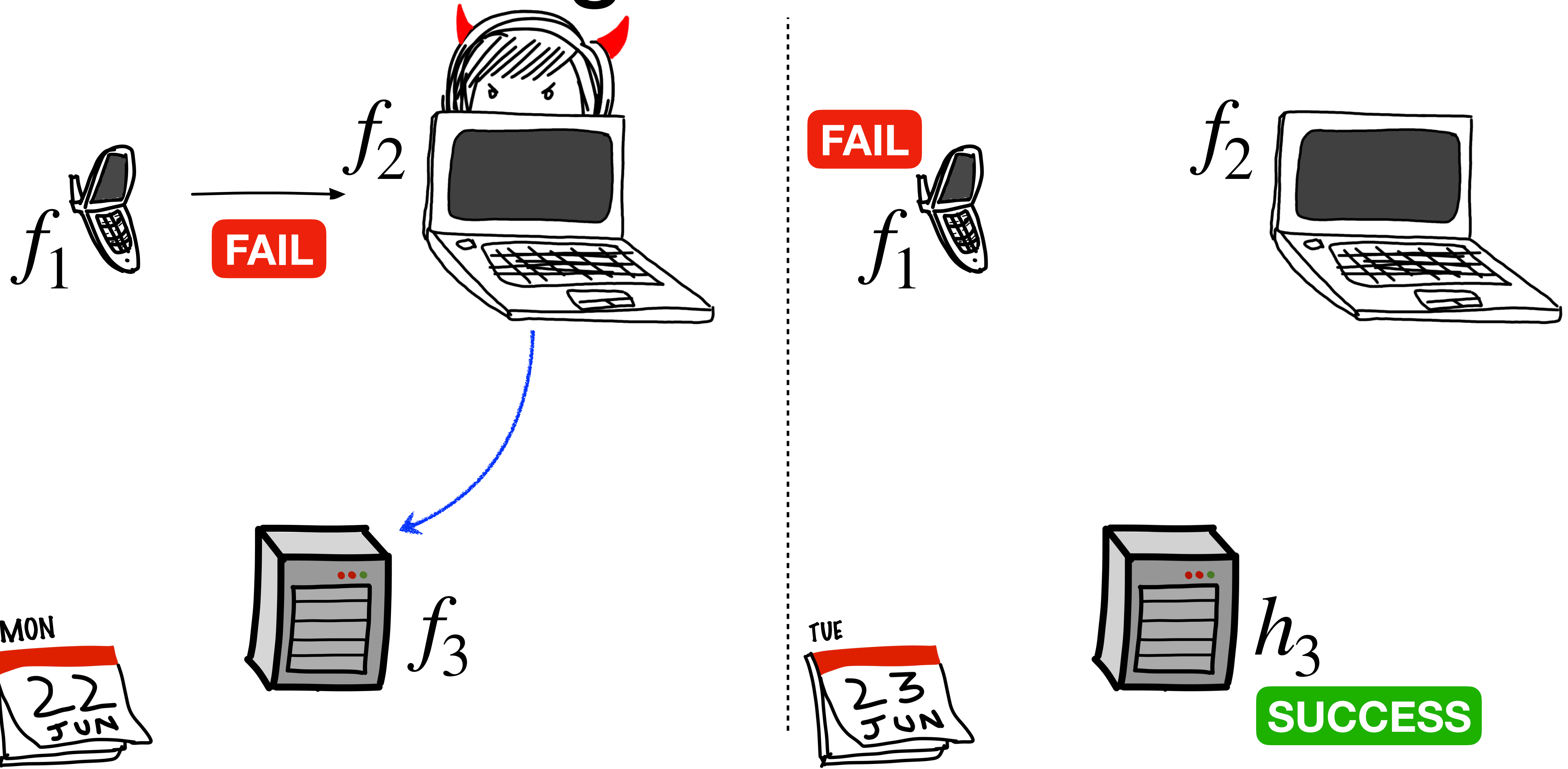
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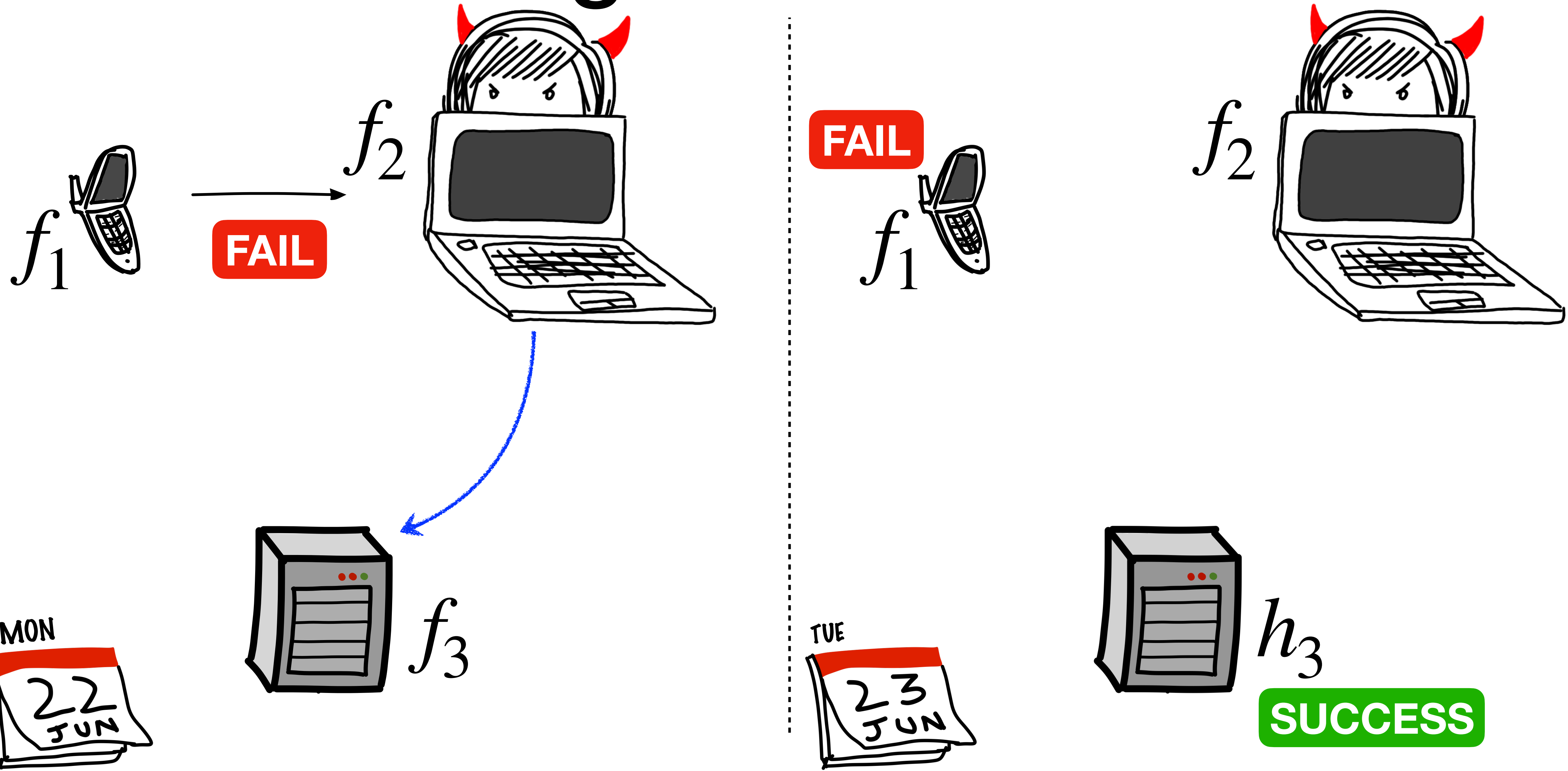
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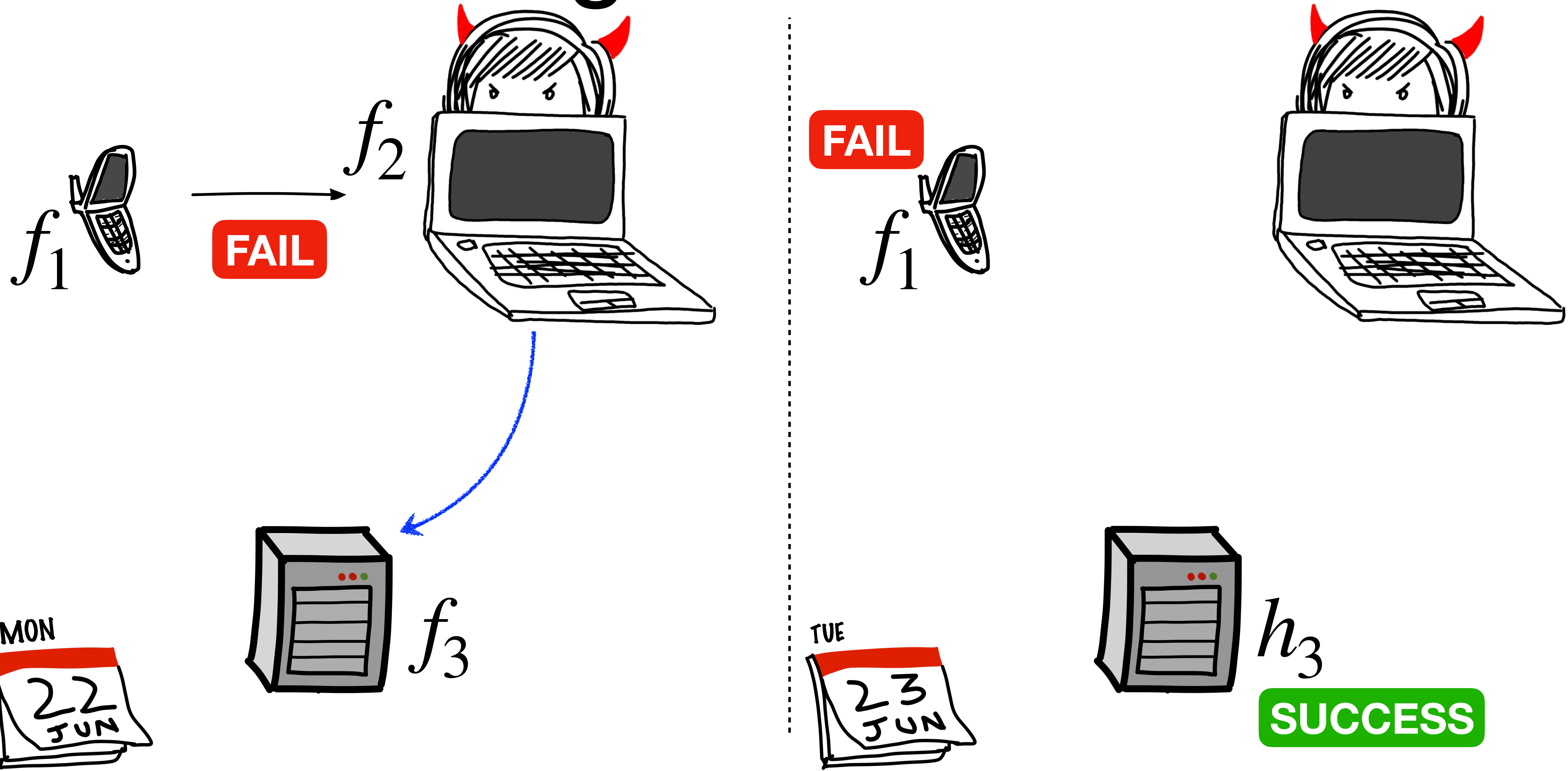
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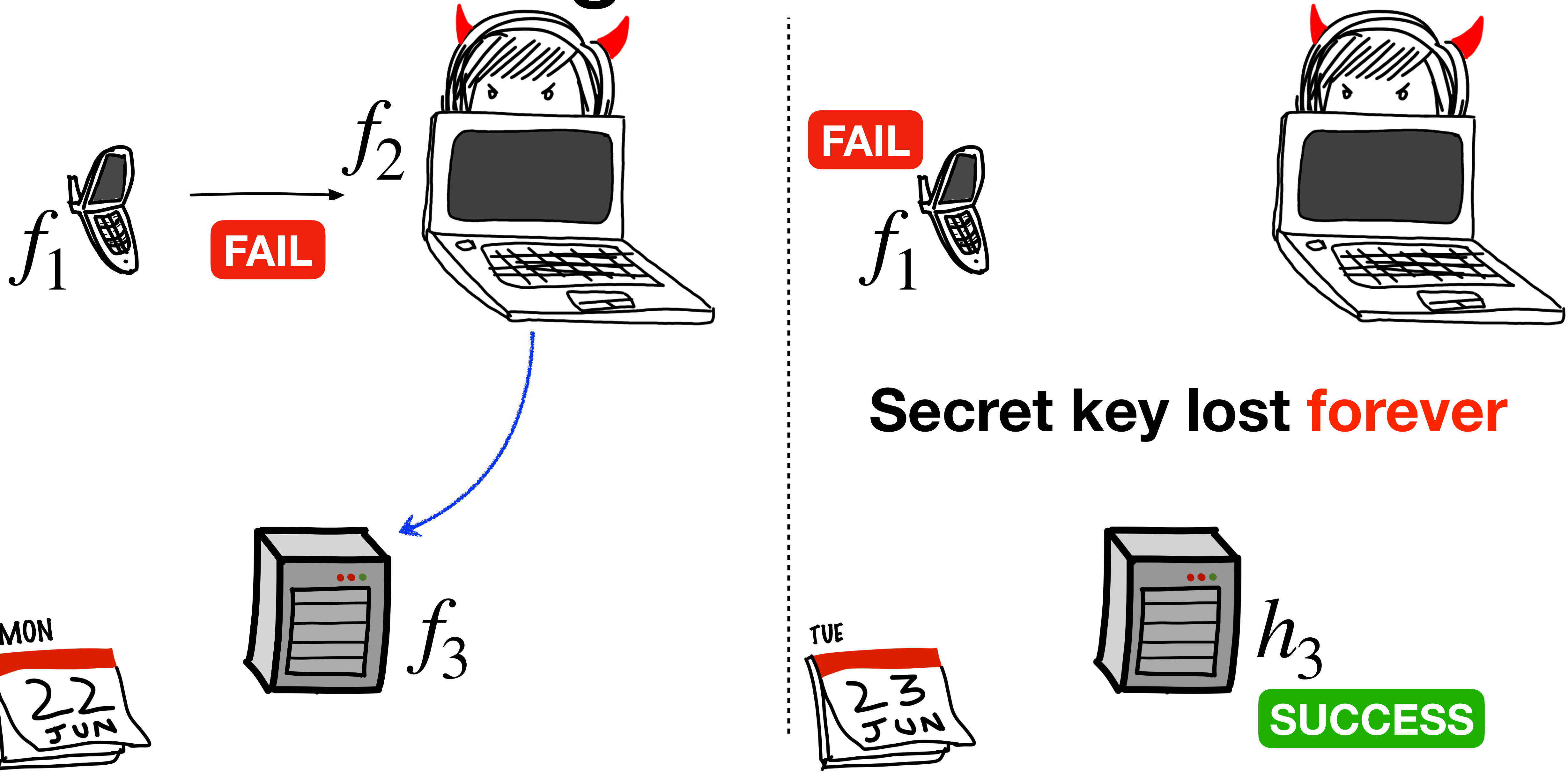
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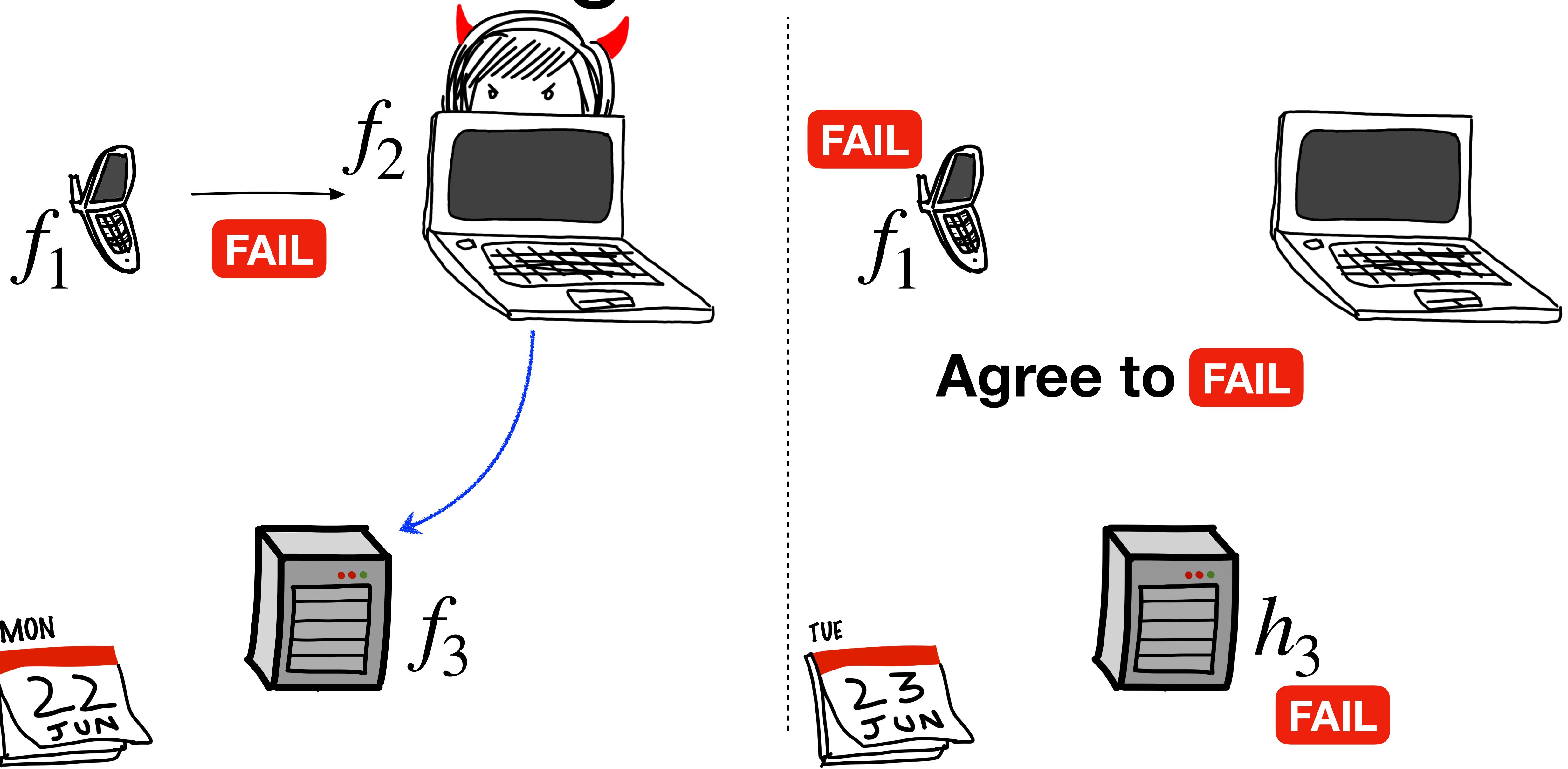
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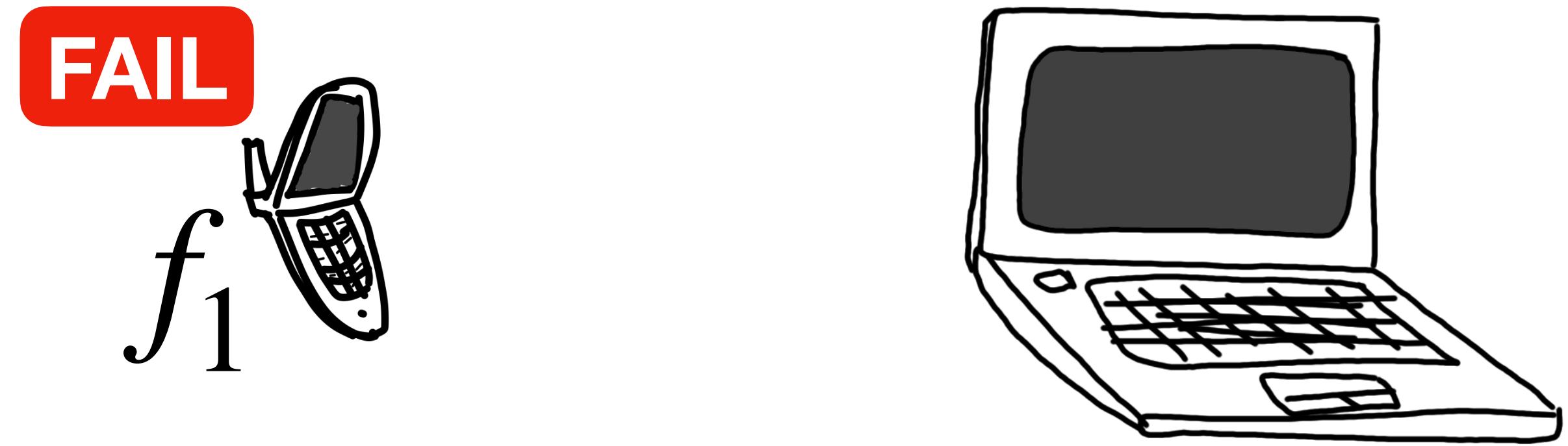
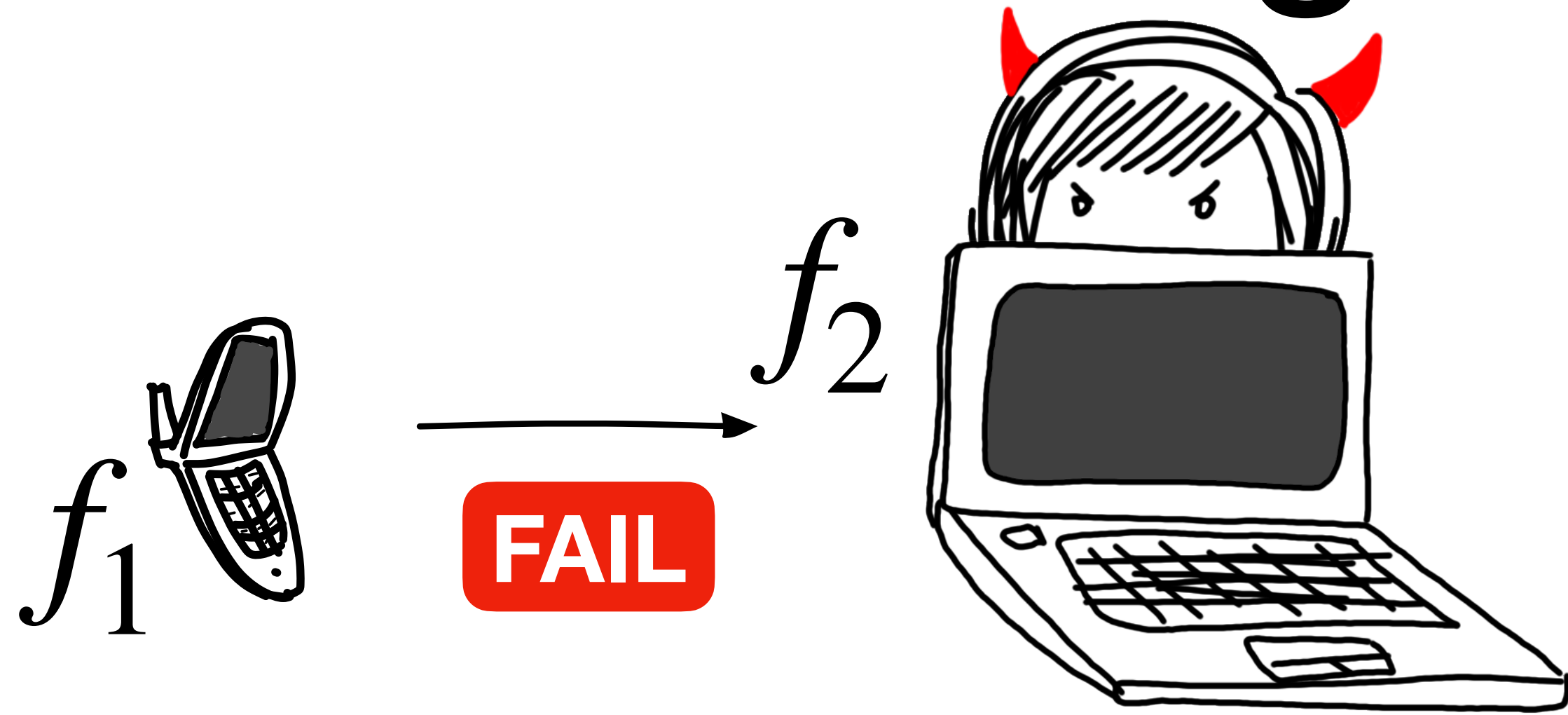
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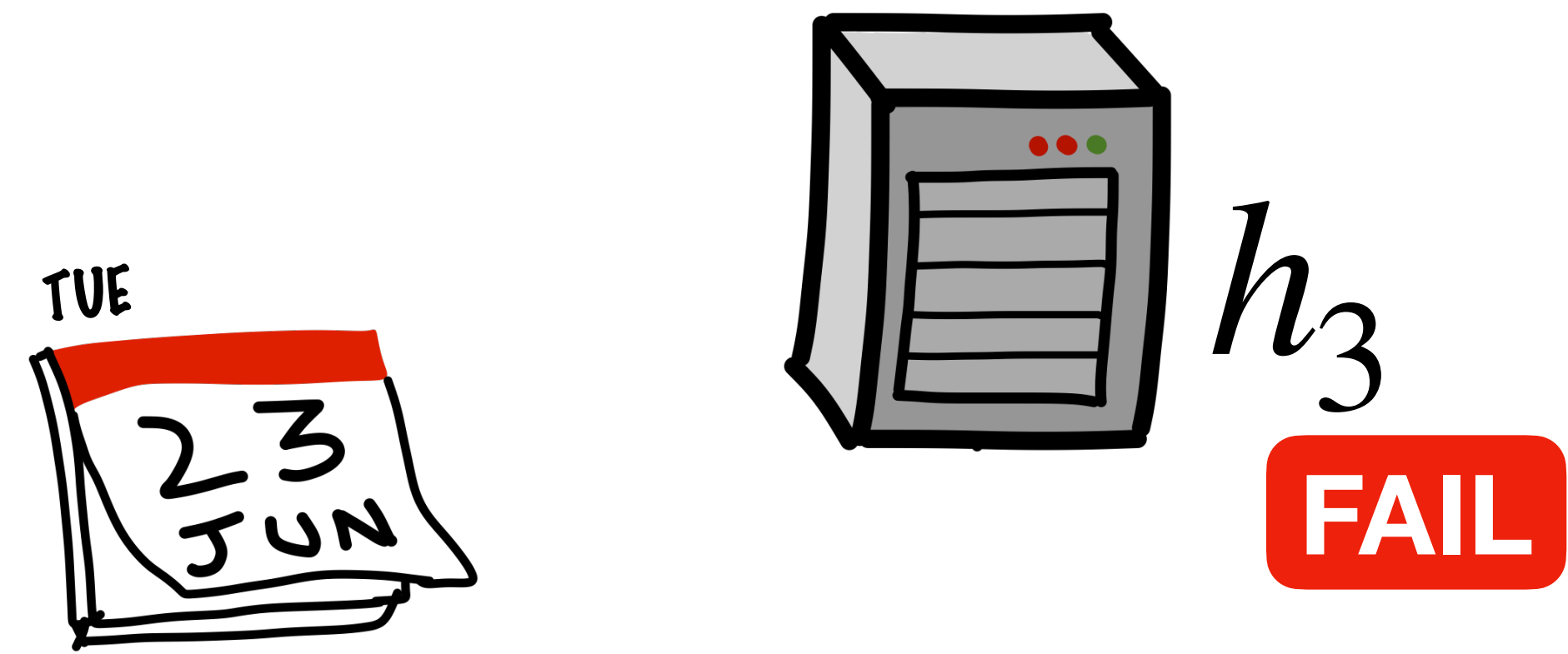
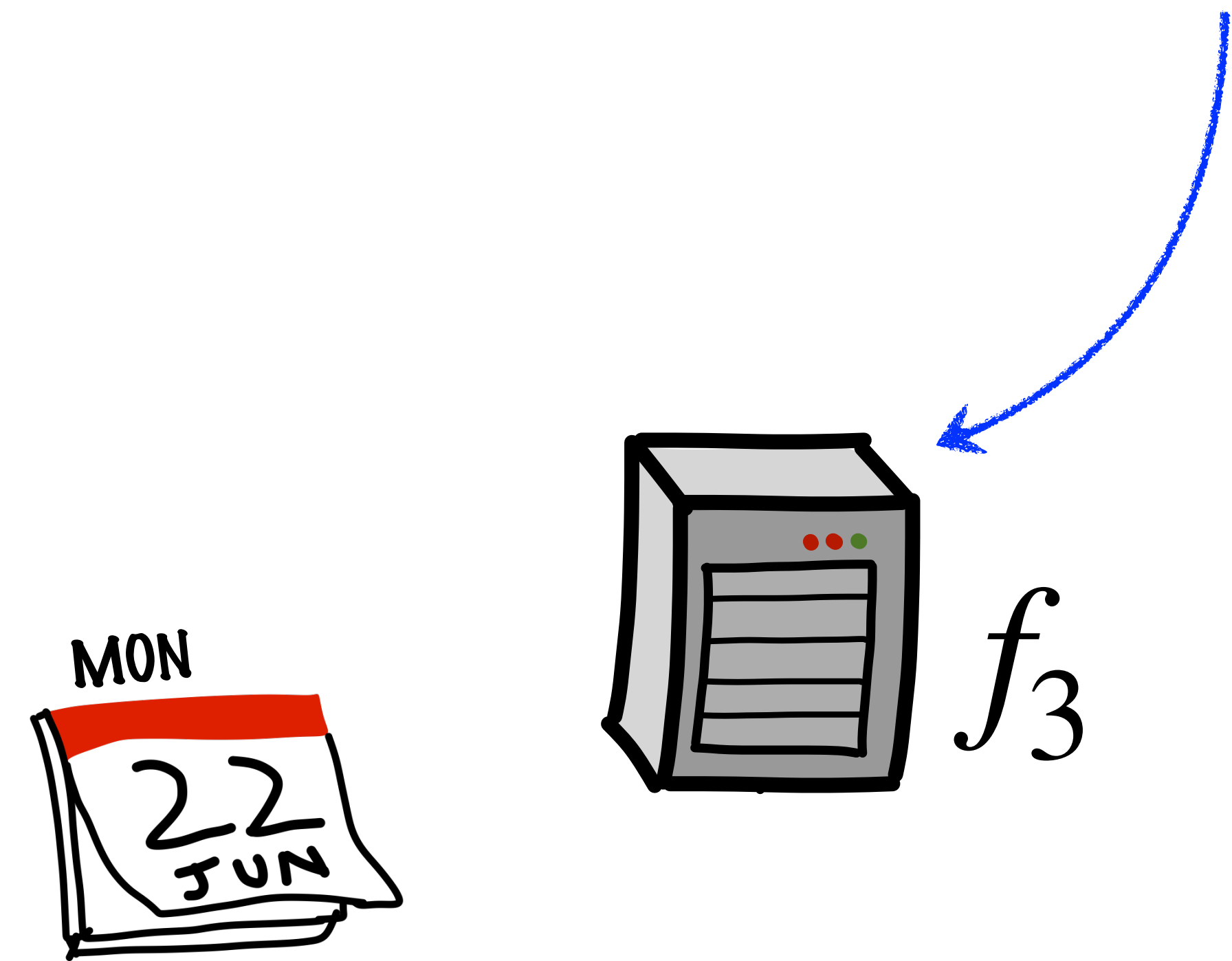
# Defining Offline Refresh



# Defining Offline Refresh



Agree to **FAIL**  
i.e. Unanimous Erasure



# This Work

- Correct definition is subtle
  - Guaranteed progress is impossible
  - We formulate **unanimous erasure**
- $(2,n)$  setting: Efficient new protocol **native** to wallets
- $(t,n)$  setting: **Impossible!**

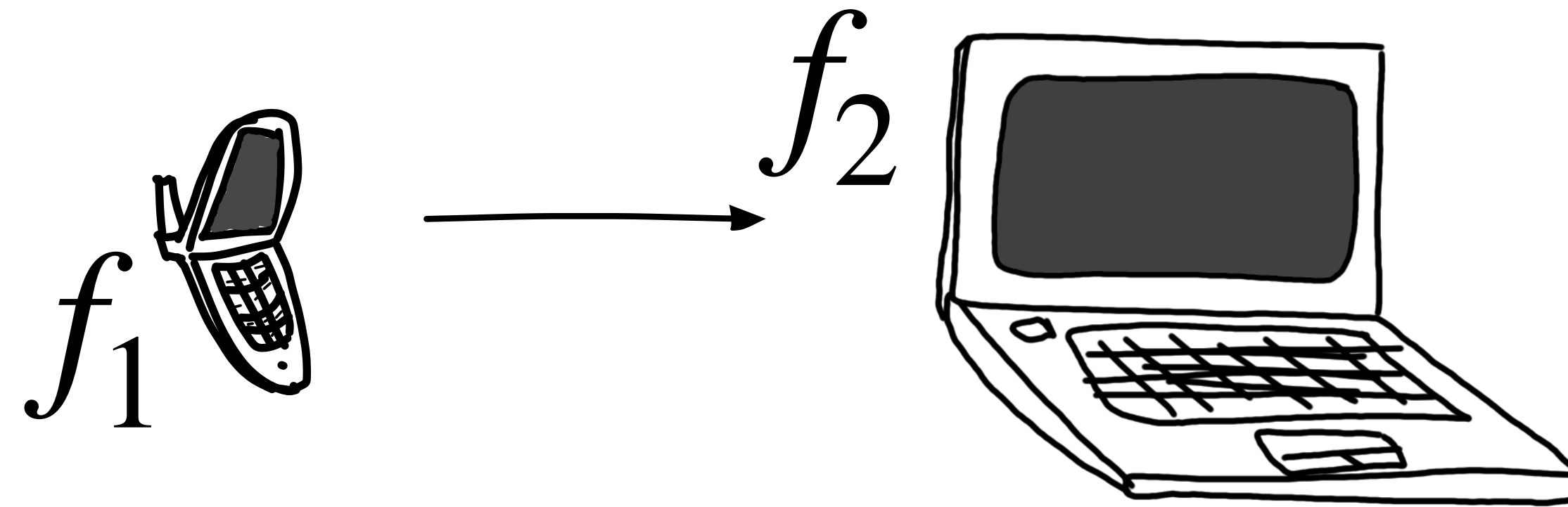
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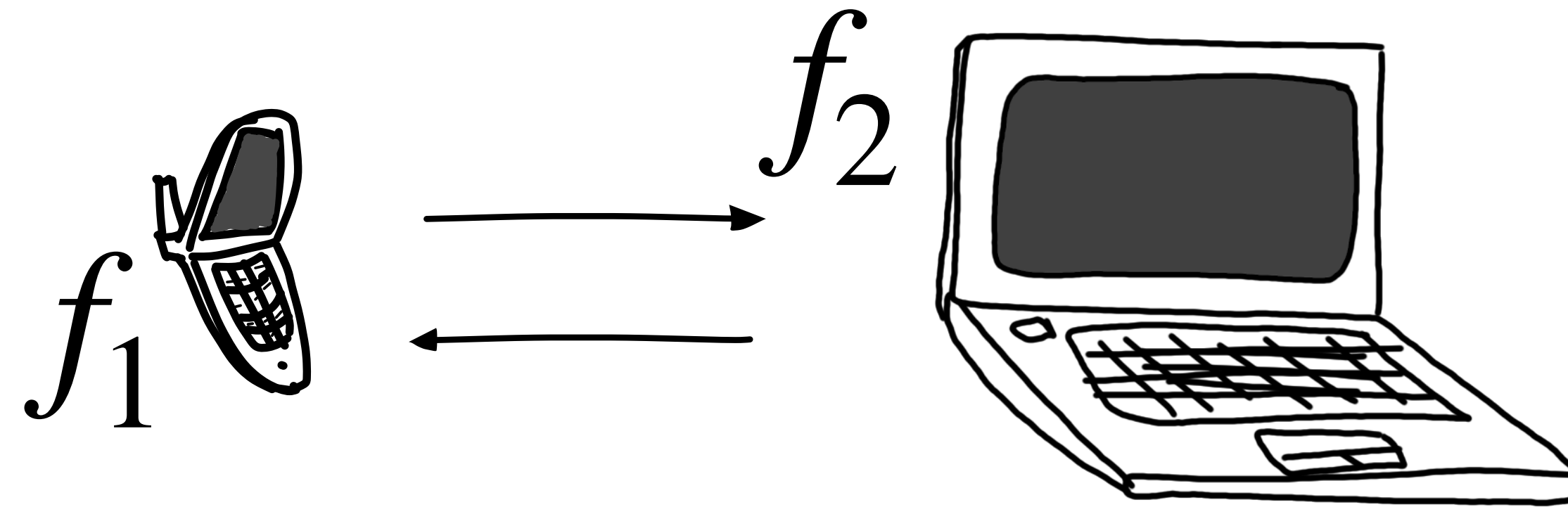
# Challenge: 2PC is Unfair



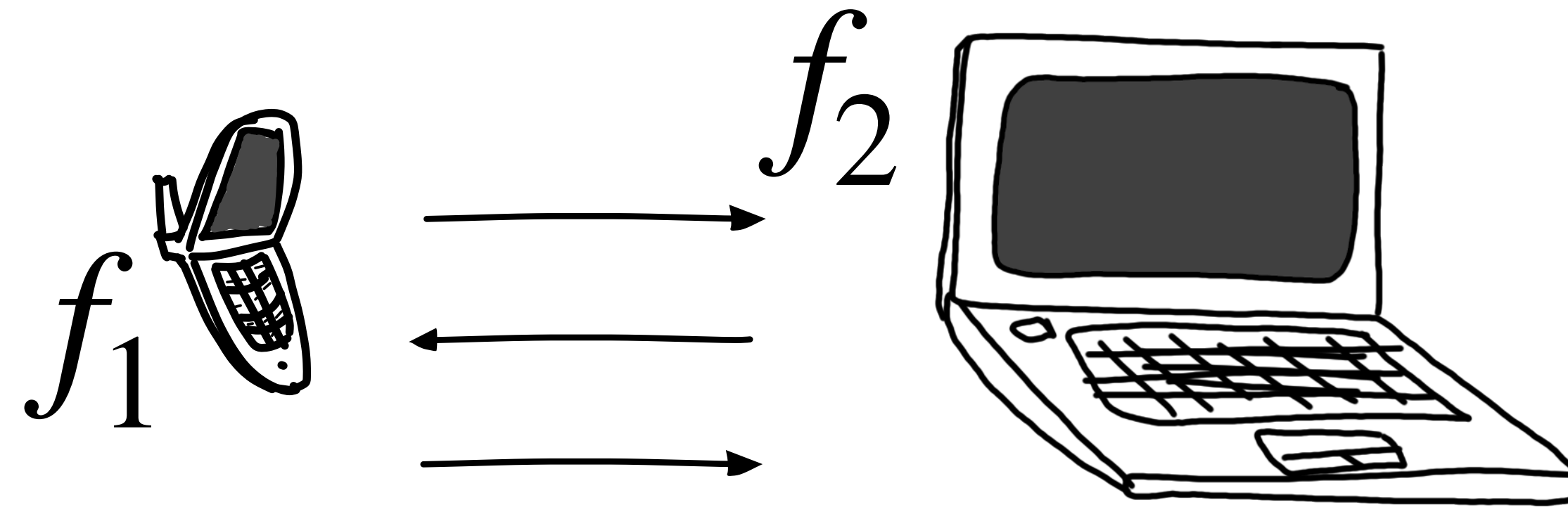
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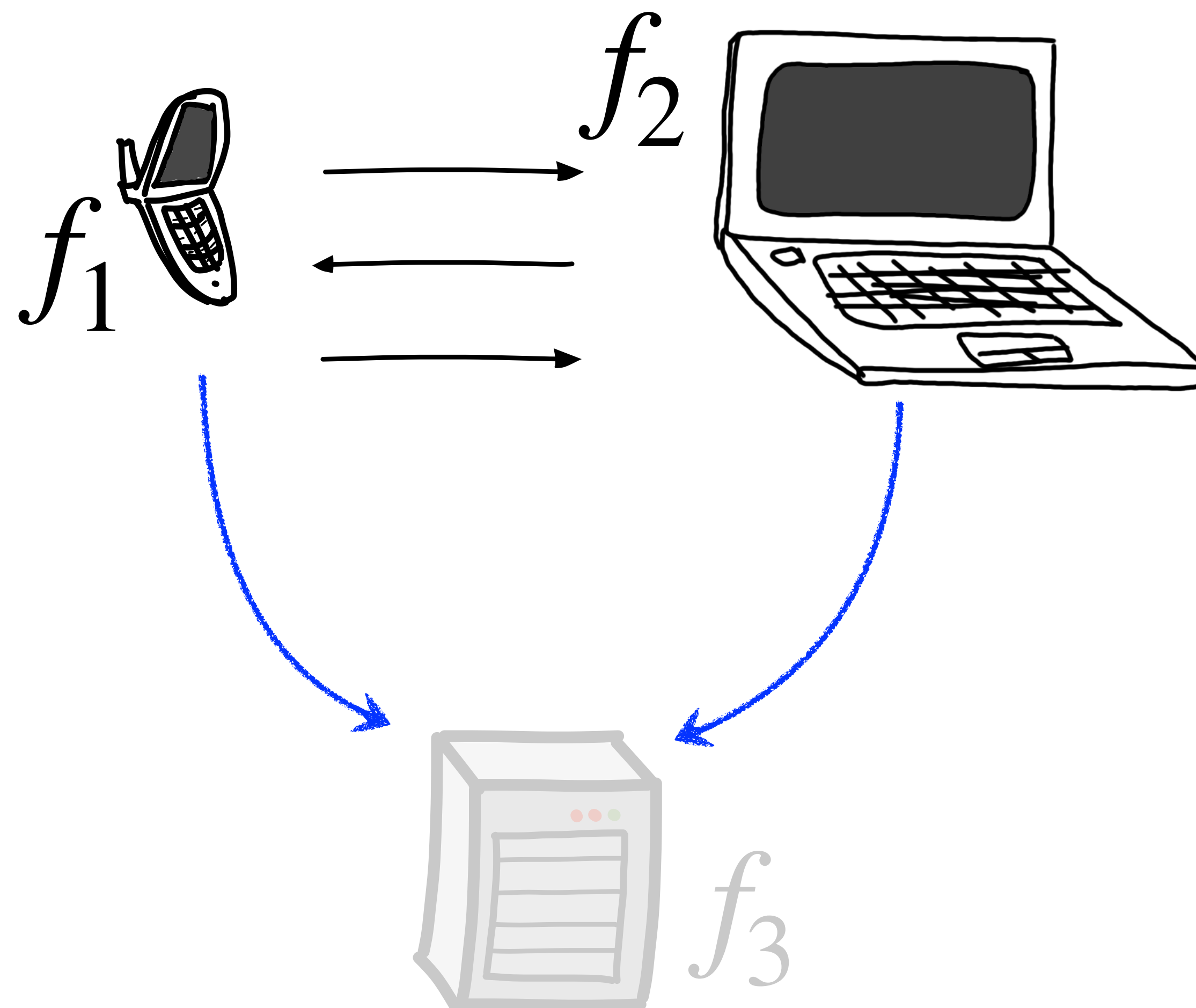
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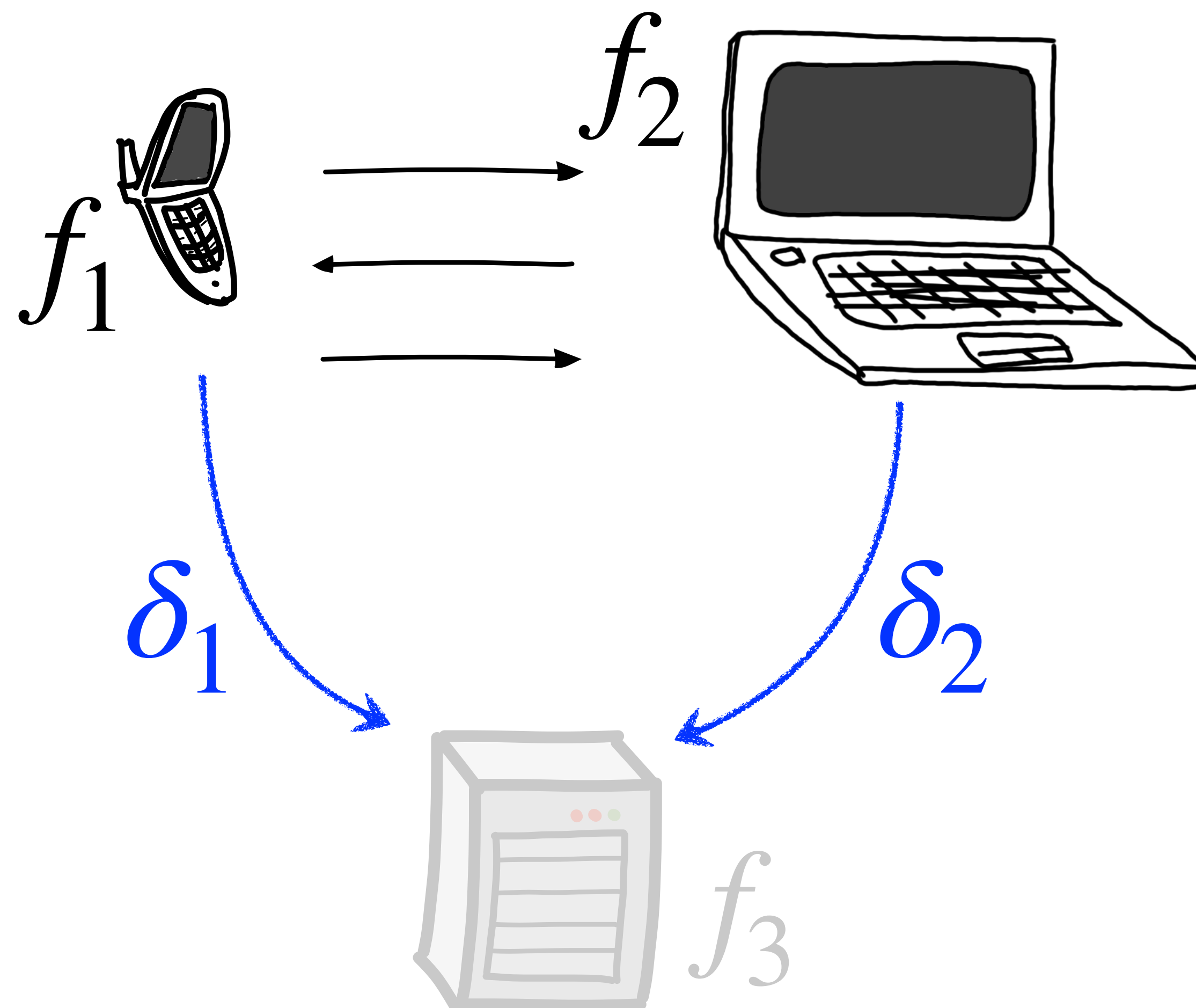
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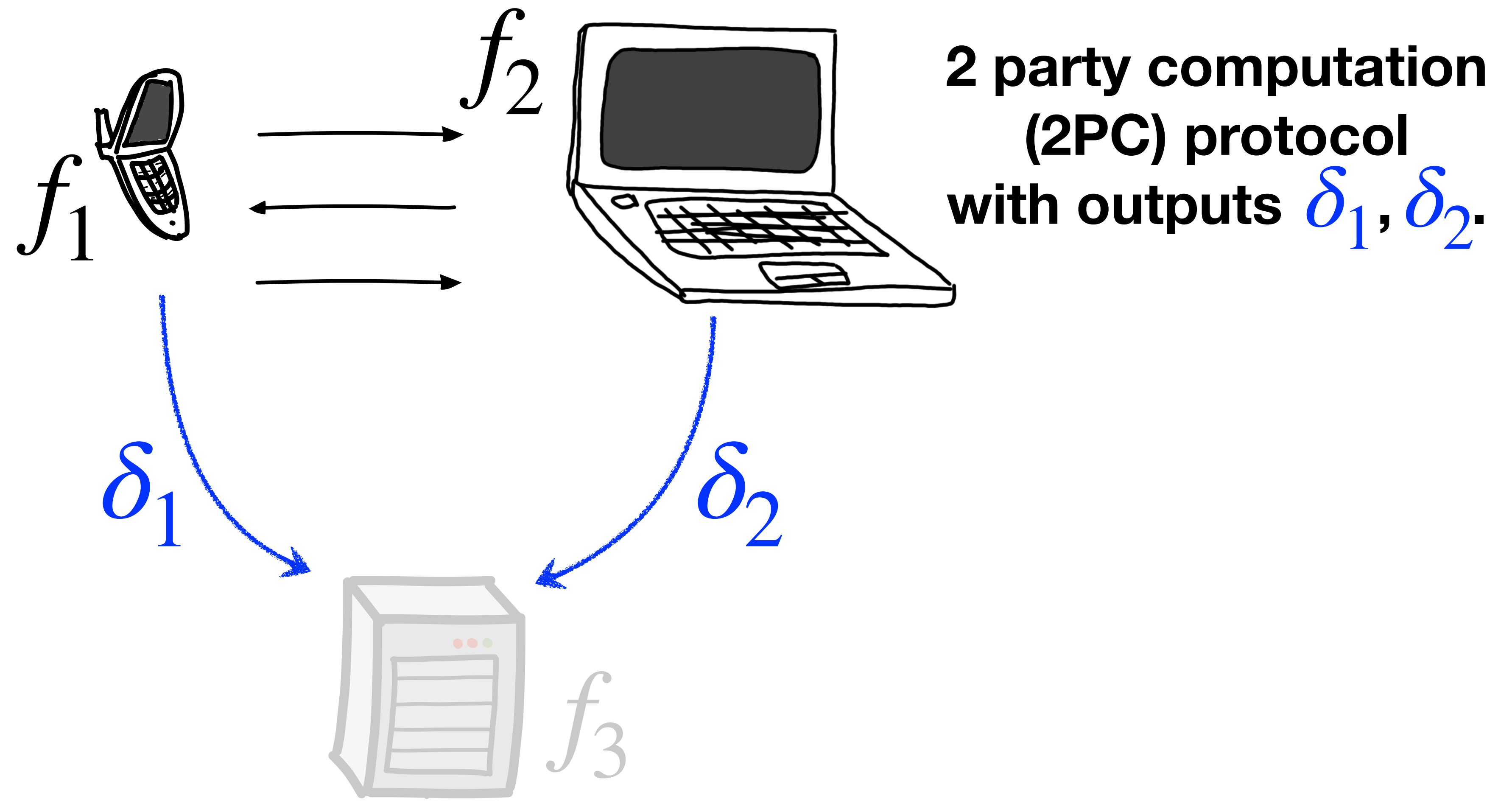
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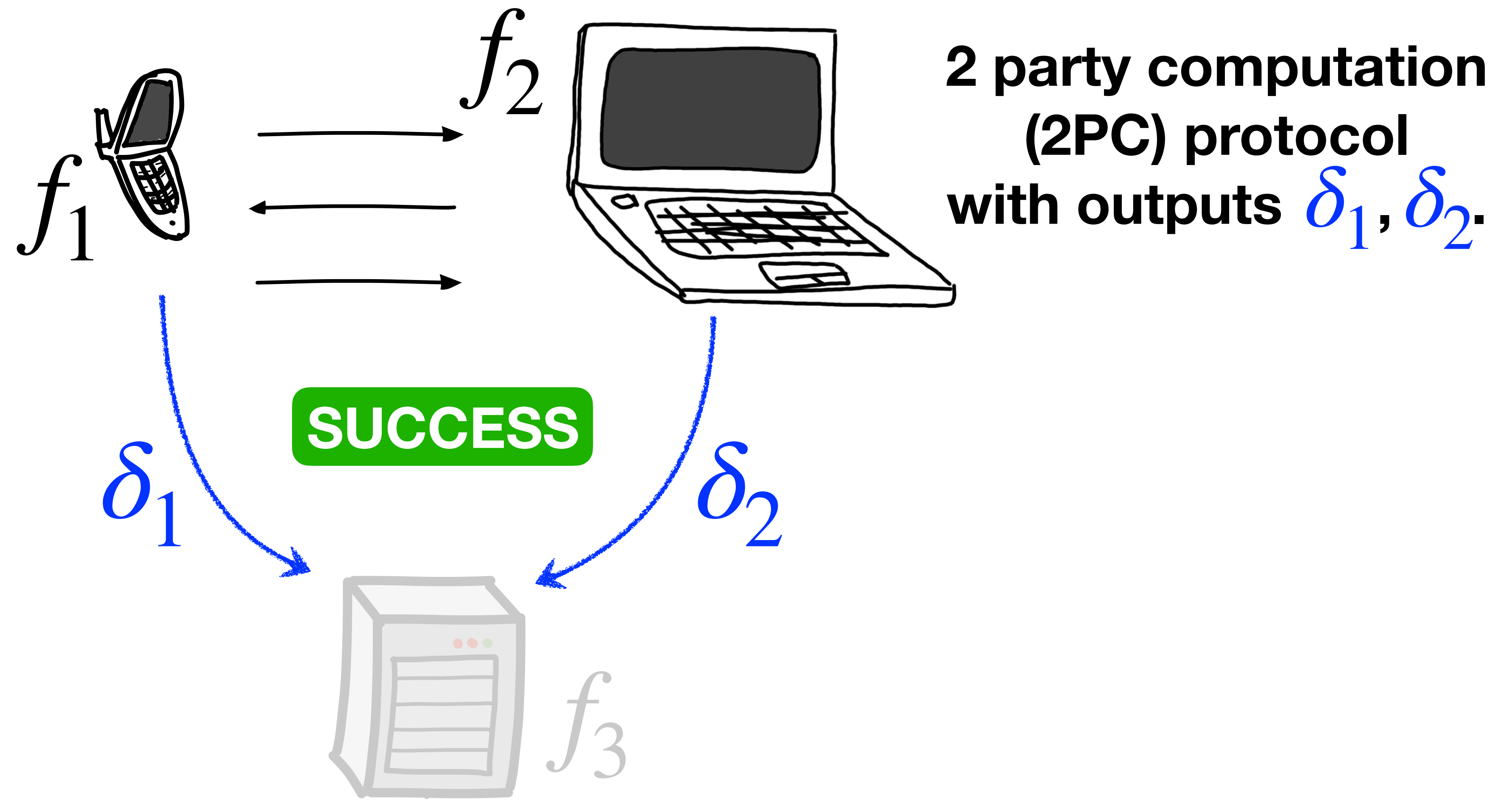
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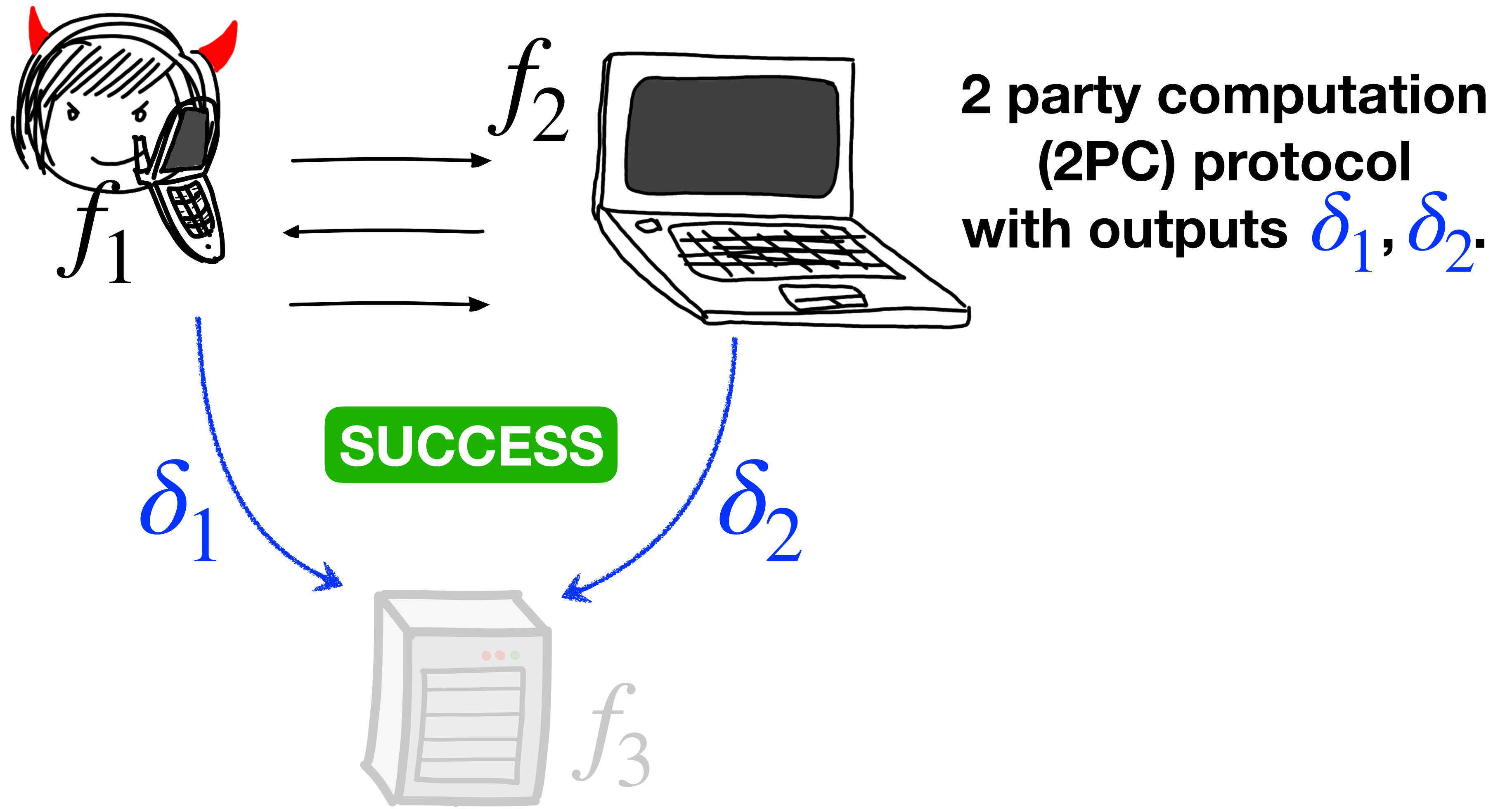
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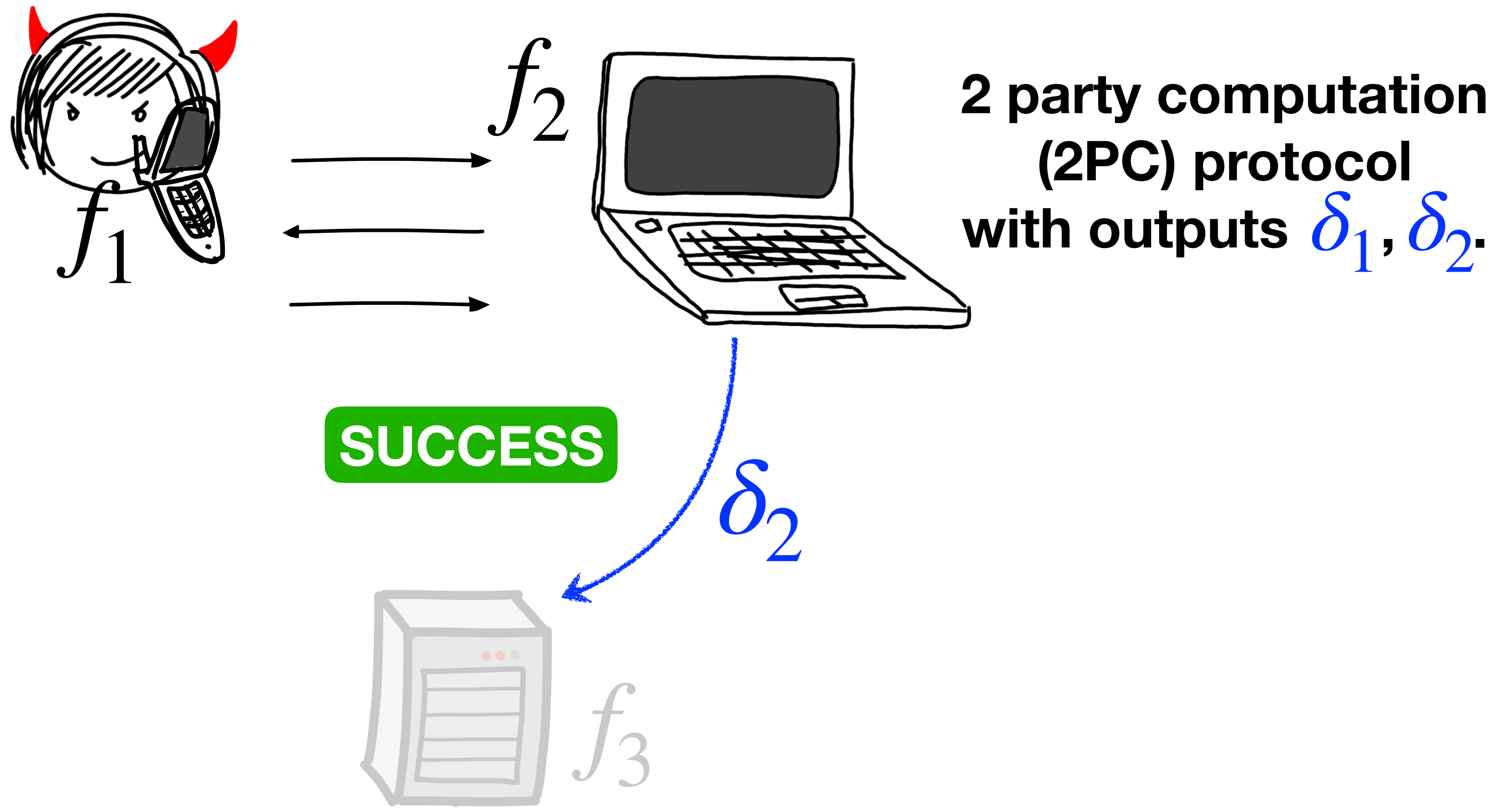
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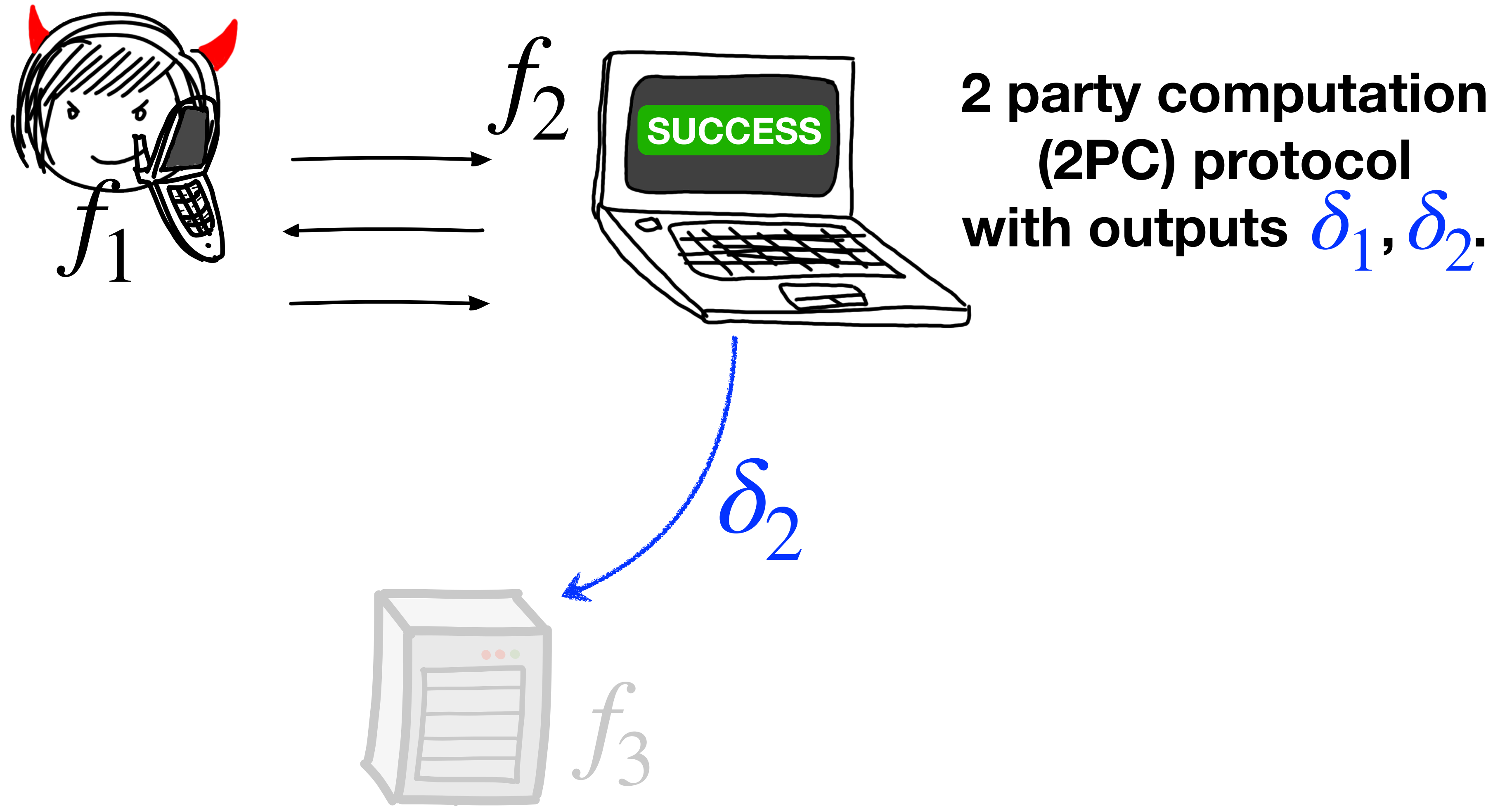
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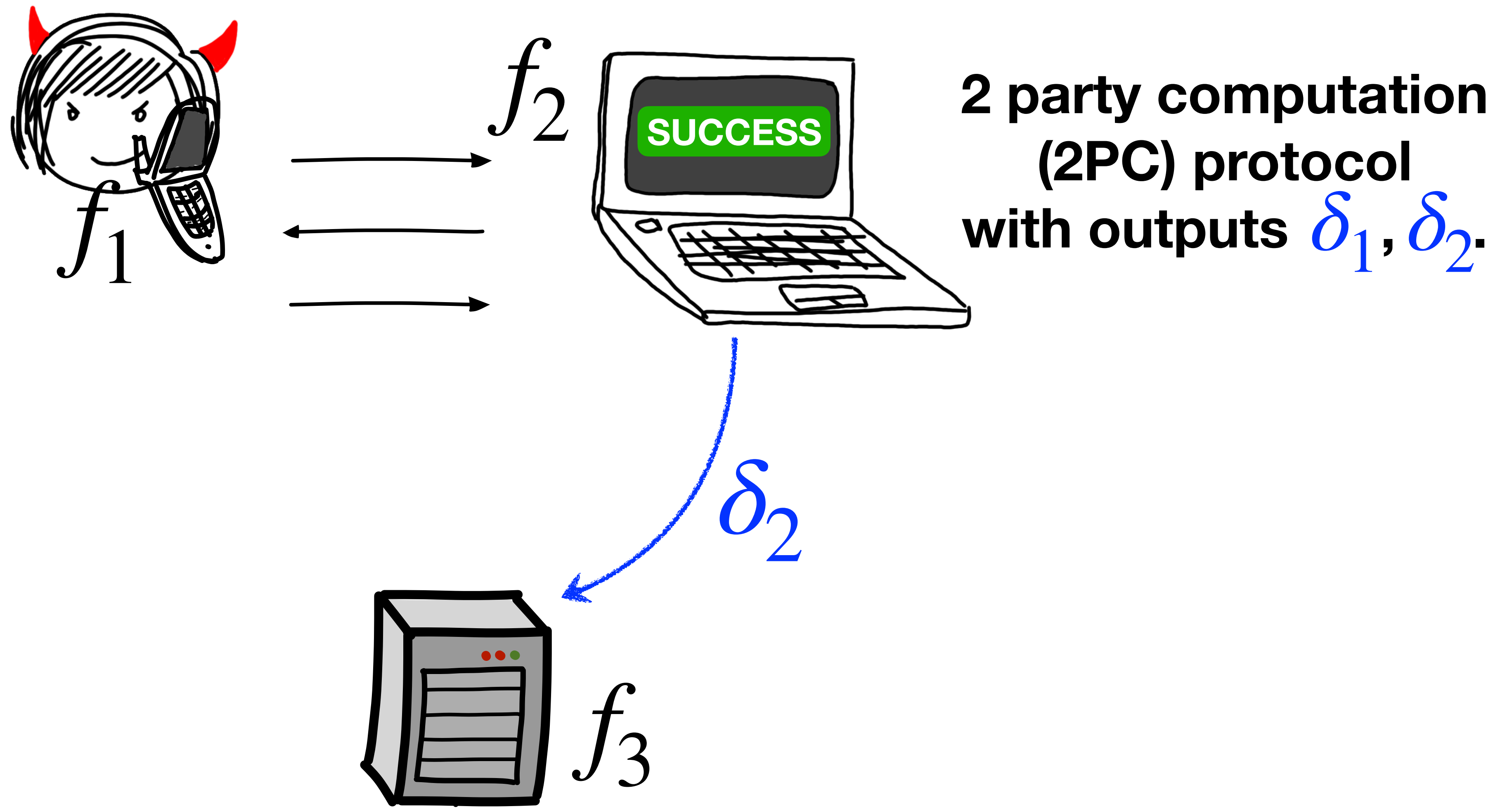
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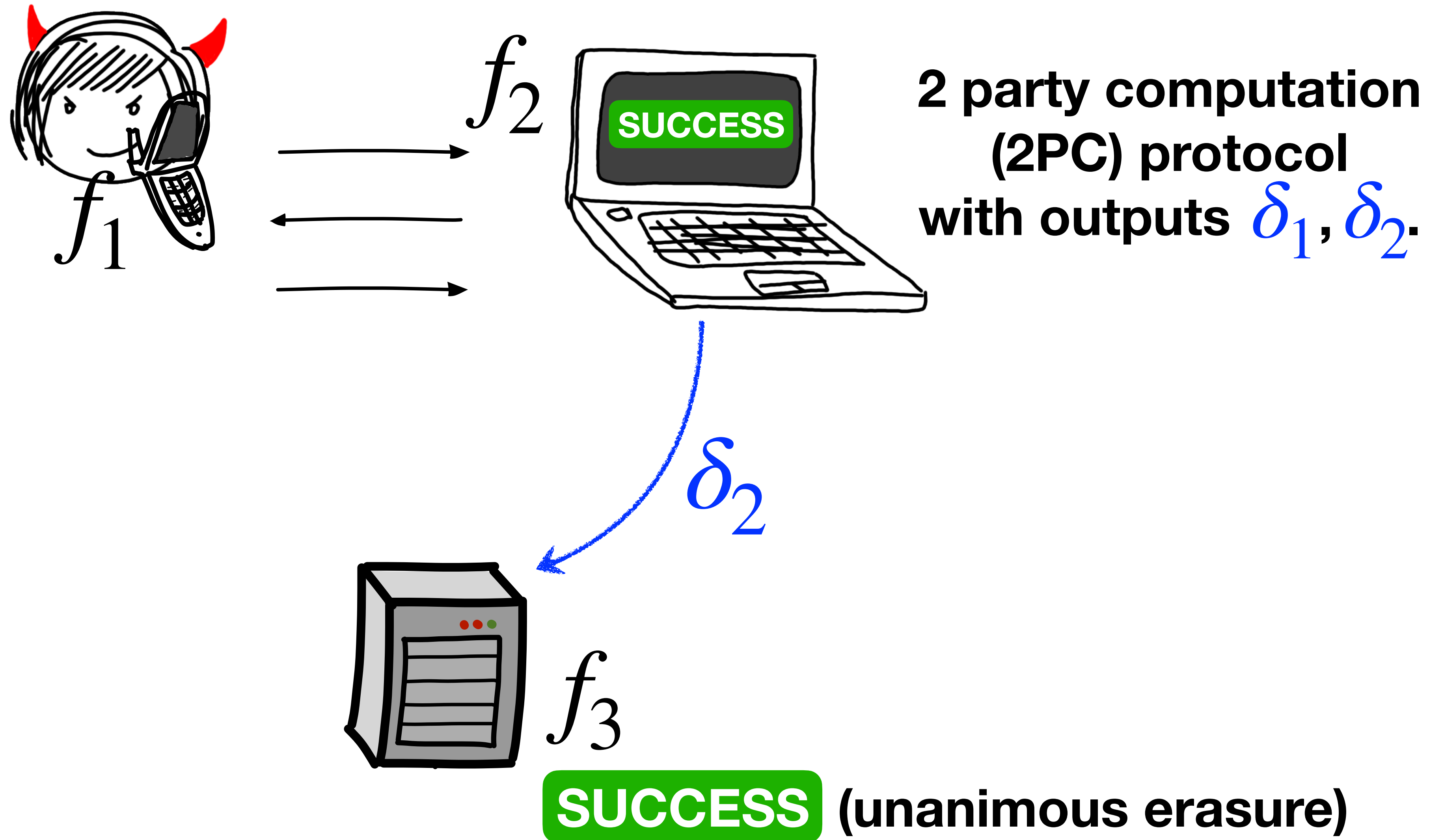
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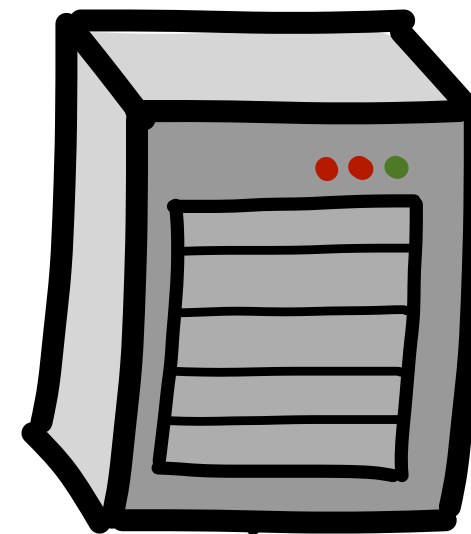
$f_2$



2 party computation  
(2PC) protocol  
with outputs  $\delta_1, \delta_2$ .

Lesson:  $\delta_2$  must be sufficient

$\delta_2$



**SUCCESS** (unanimous erasure)

# Challenge: 2PC is Unfair



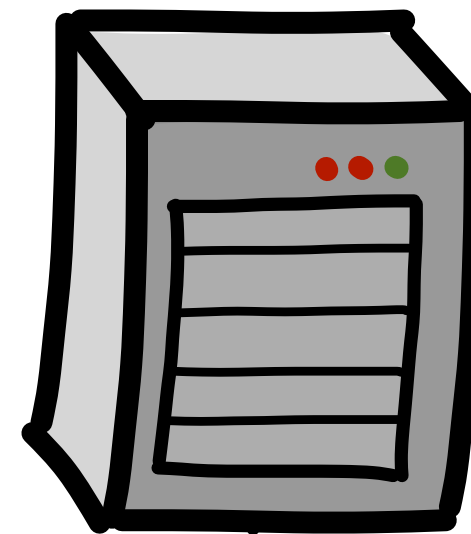
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Lesson:  $\delta_2$  must be sufficient  
(Equivalently  $\delta_1$ )

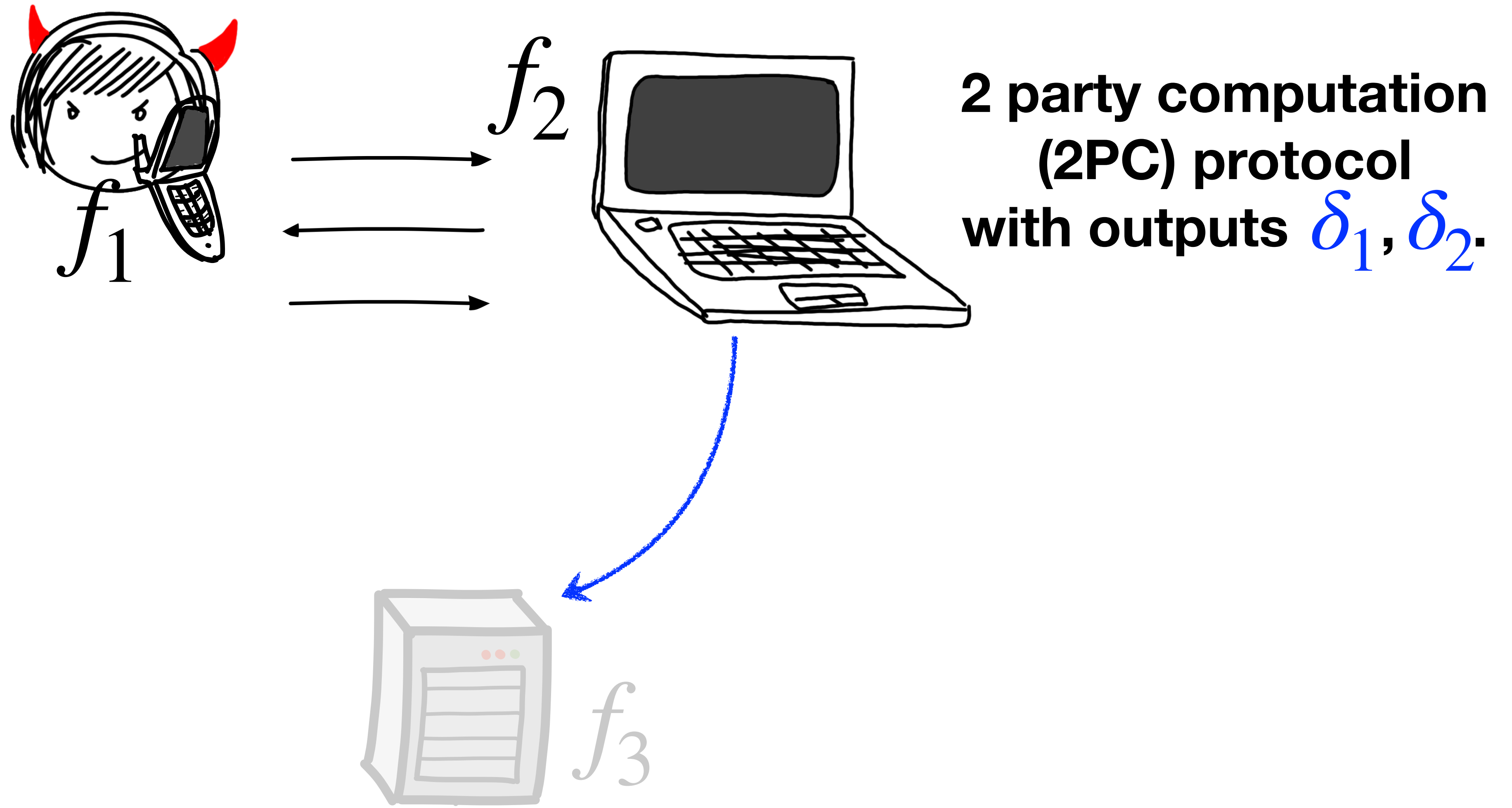
$\delta_2$



**SUCCESS**

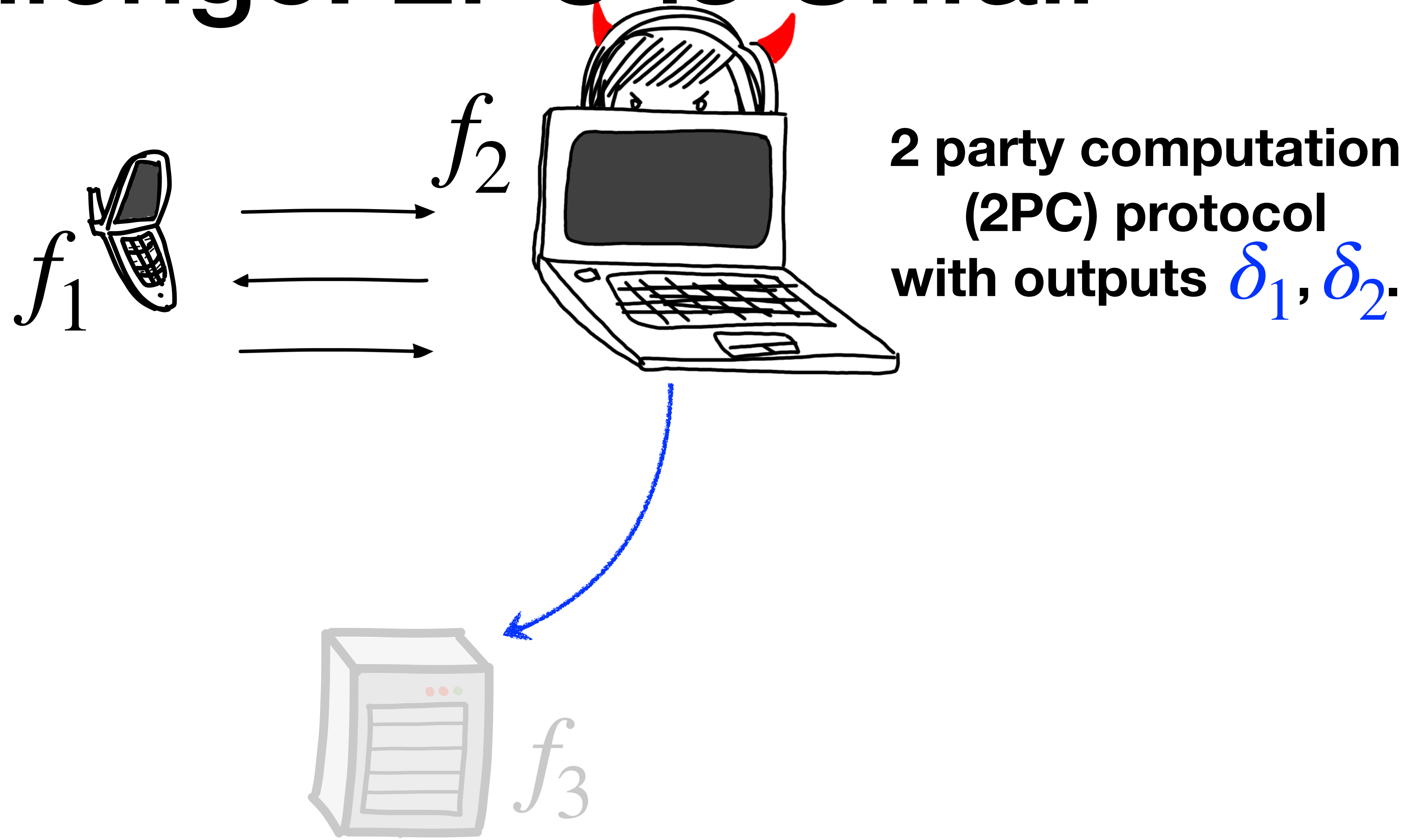
(unanimous erasure)

# Challenge: 2PC is Unfair



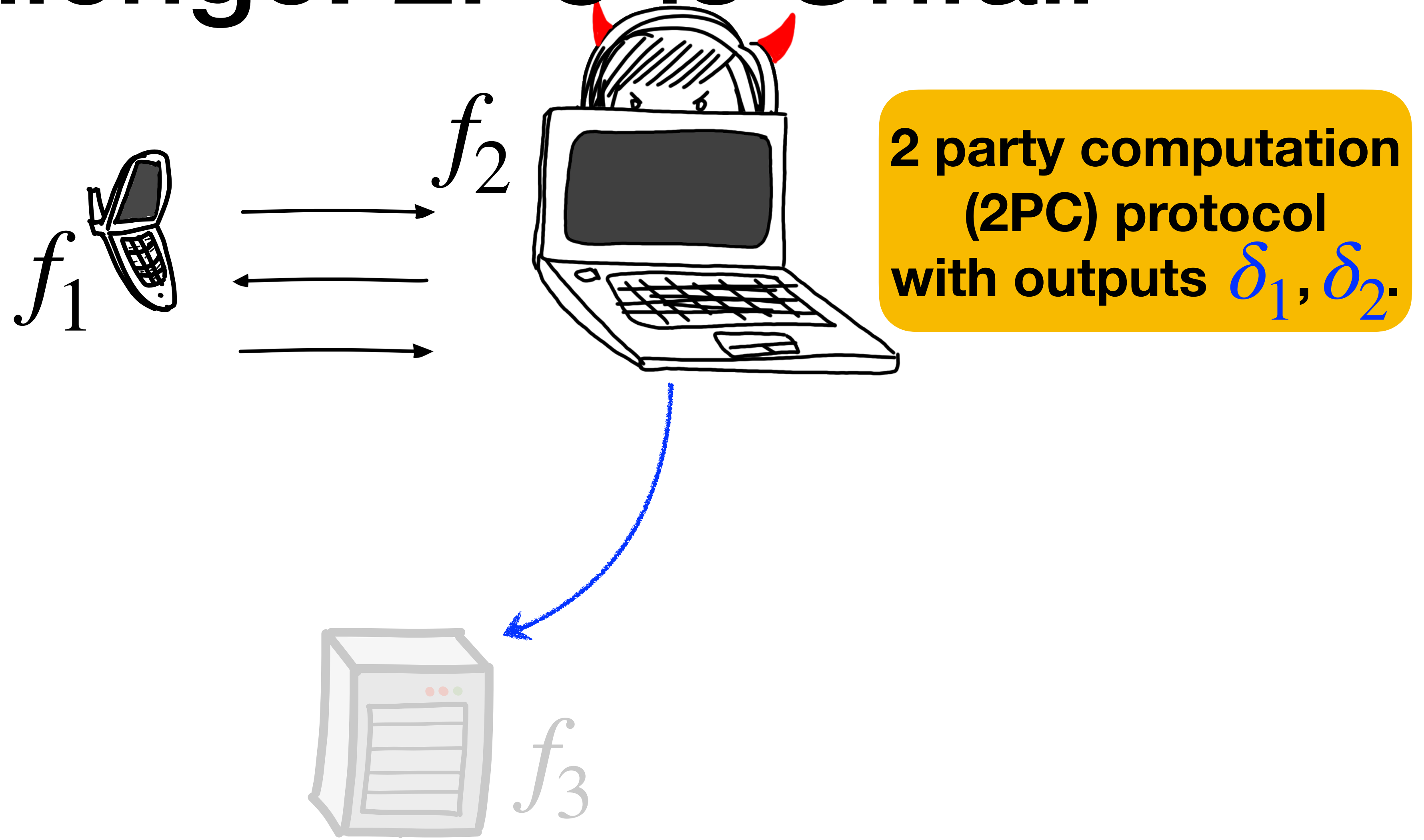
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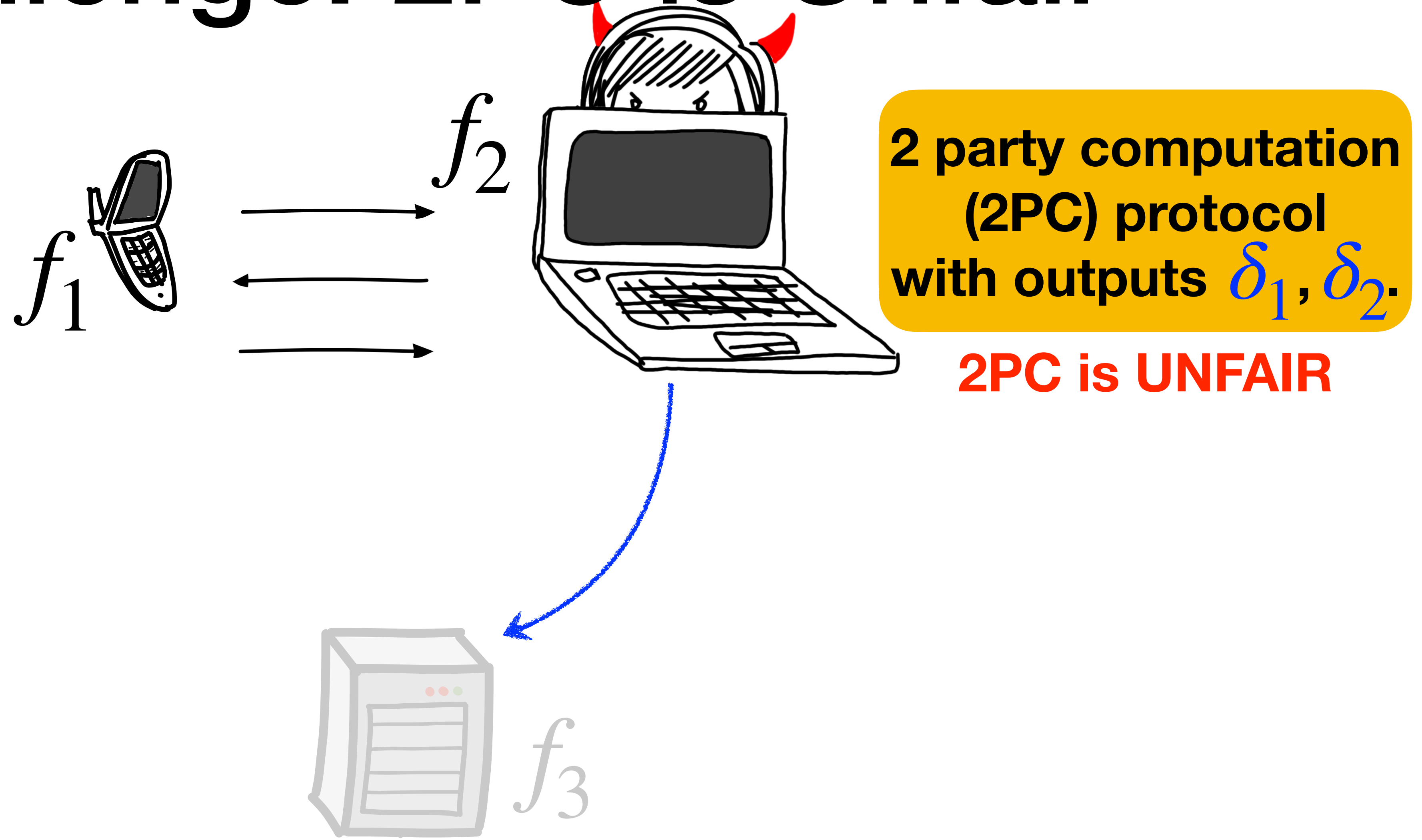
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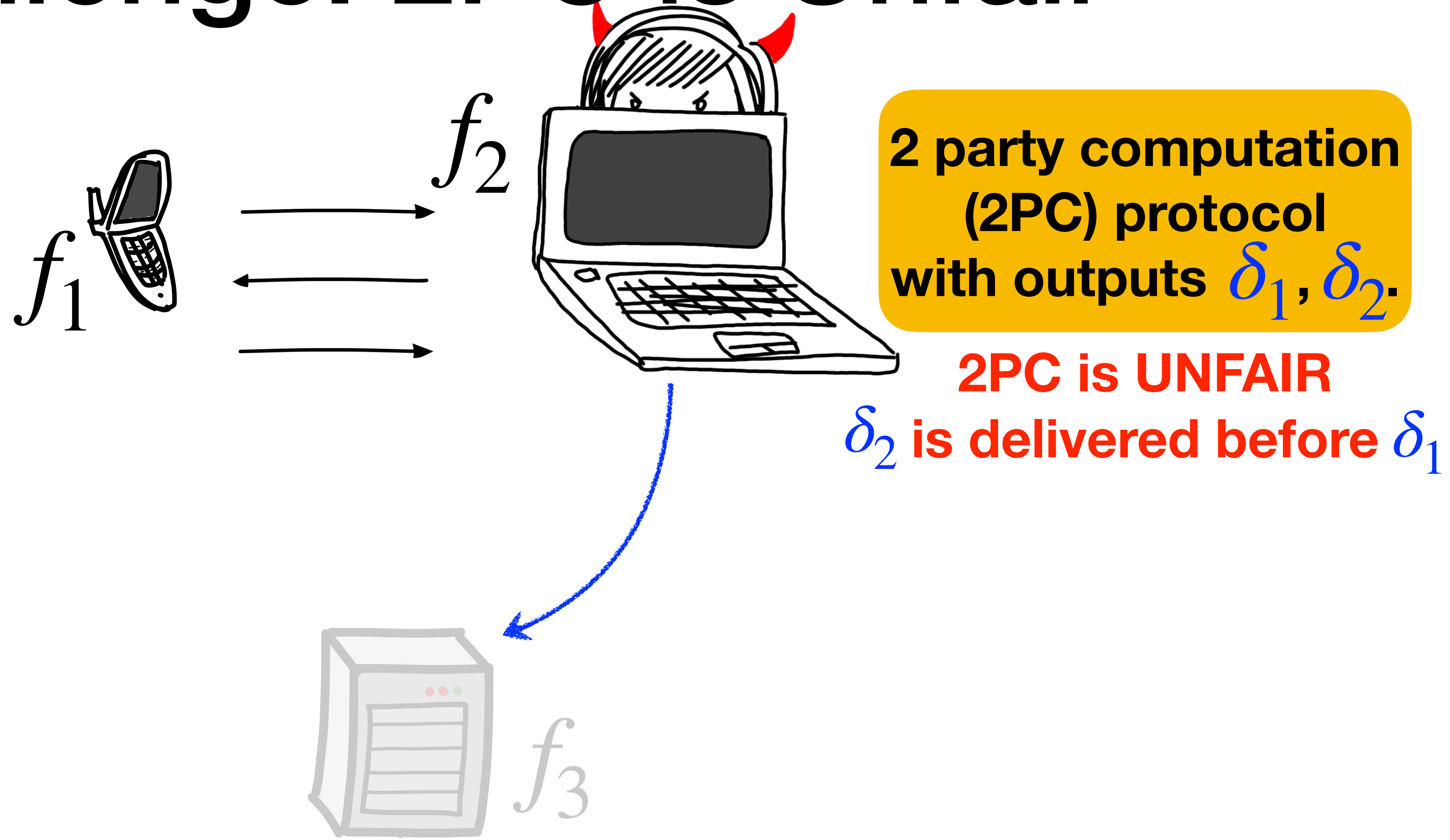
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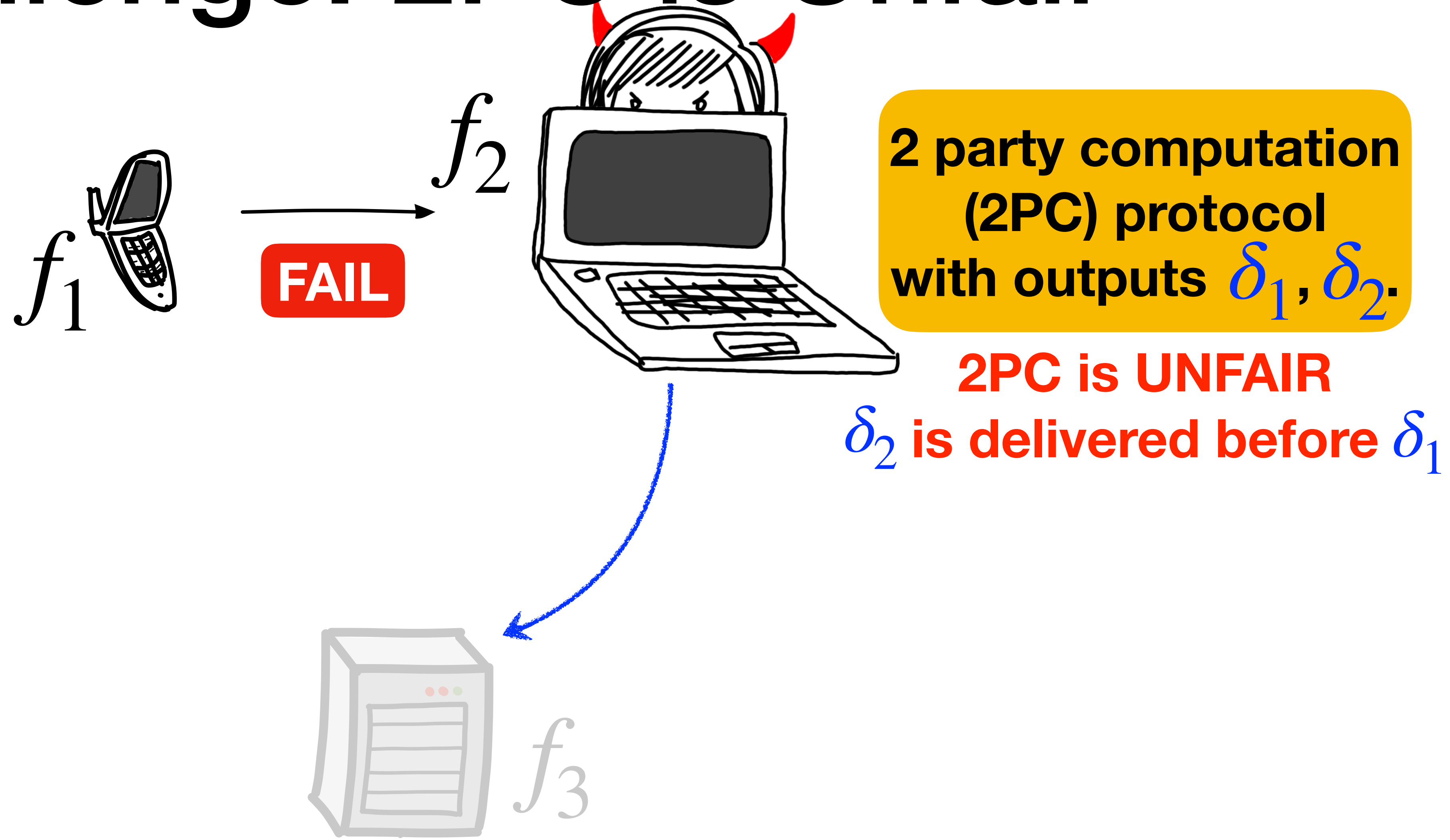
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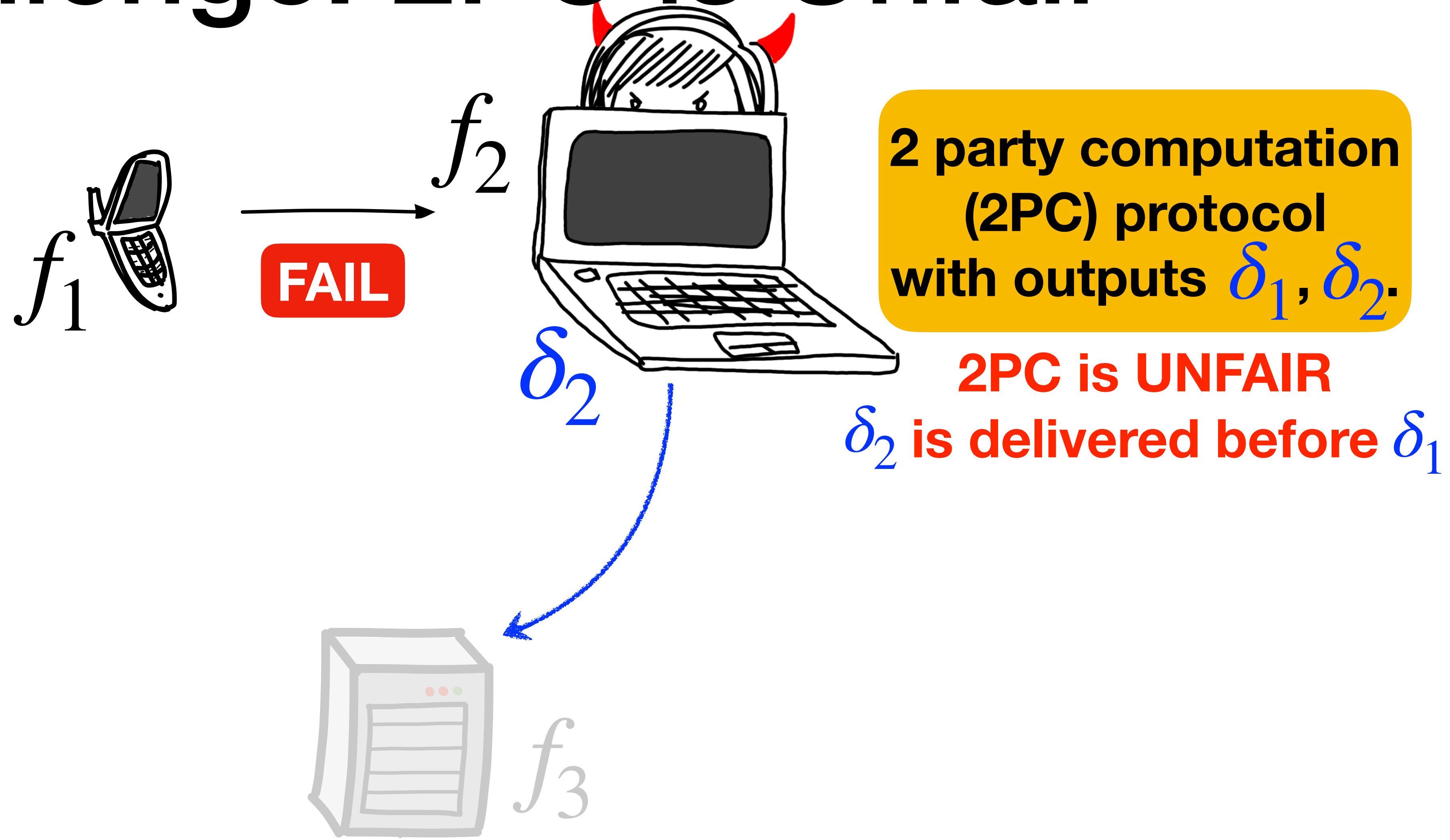
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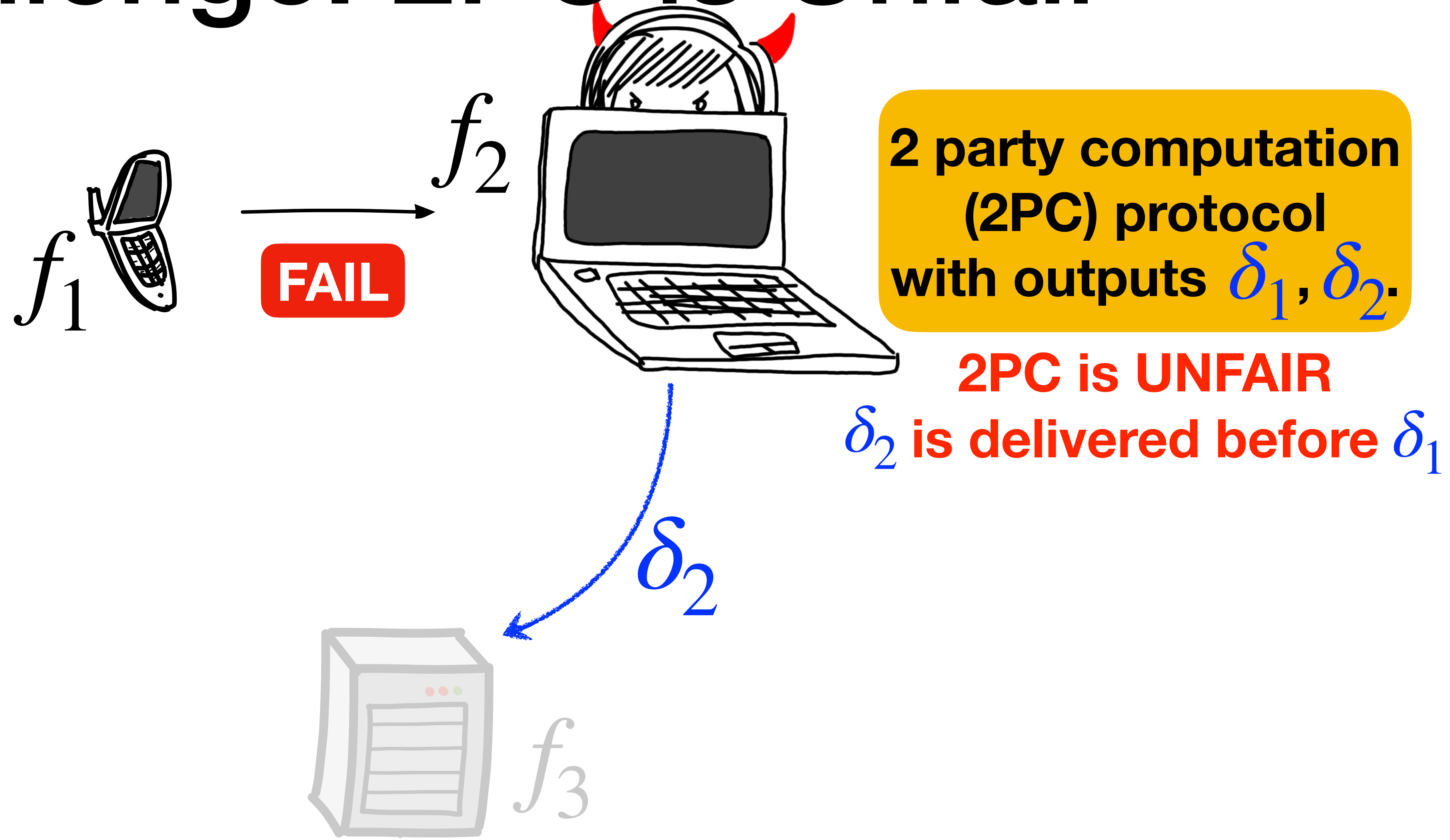
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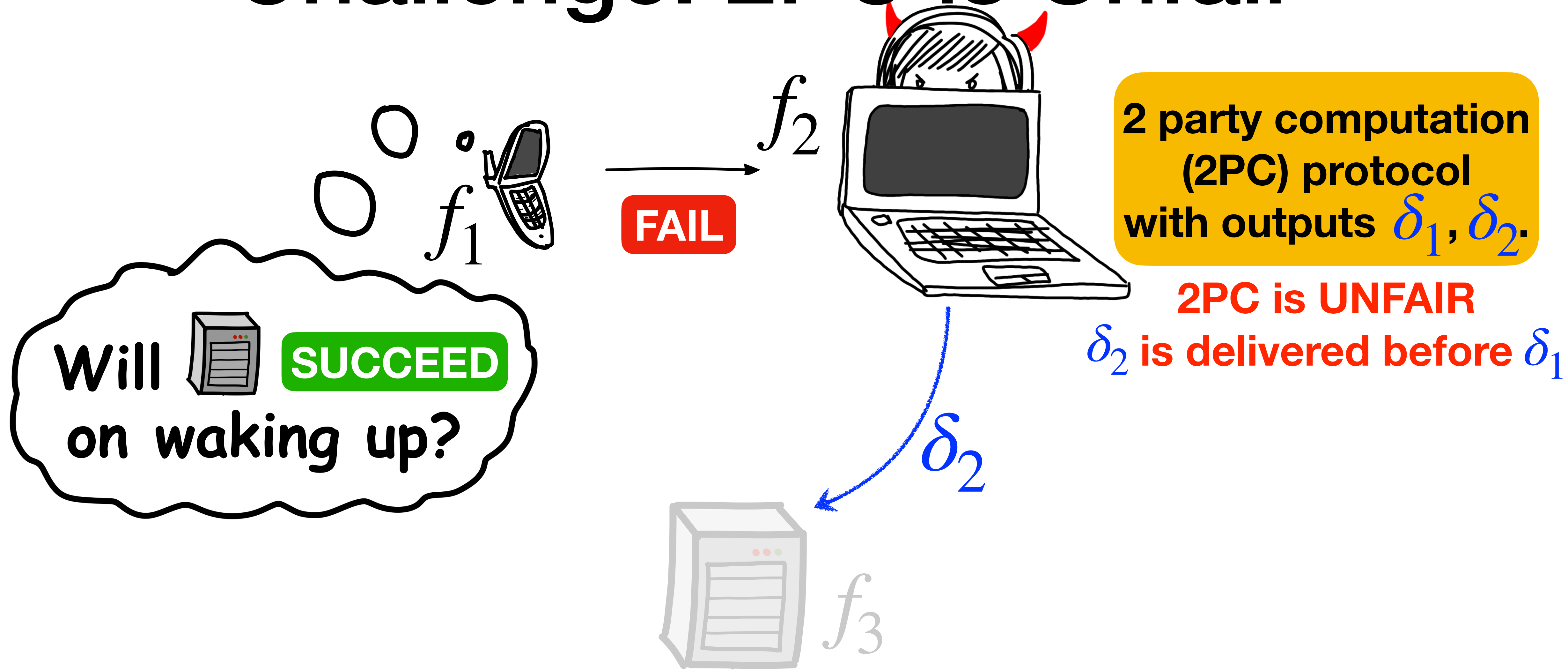
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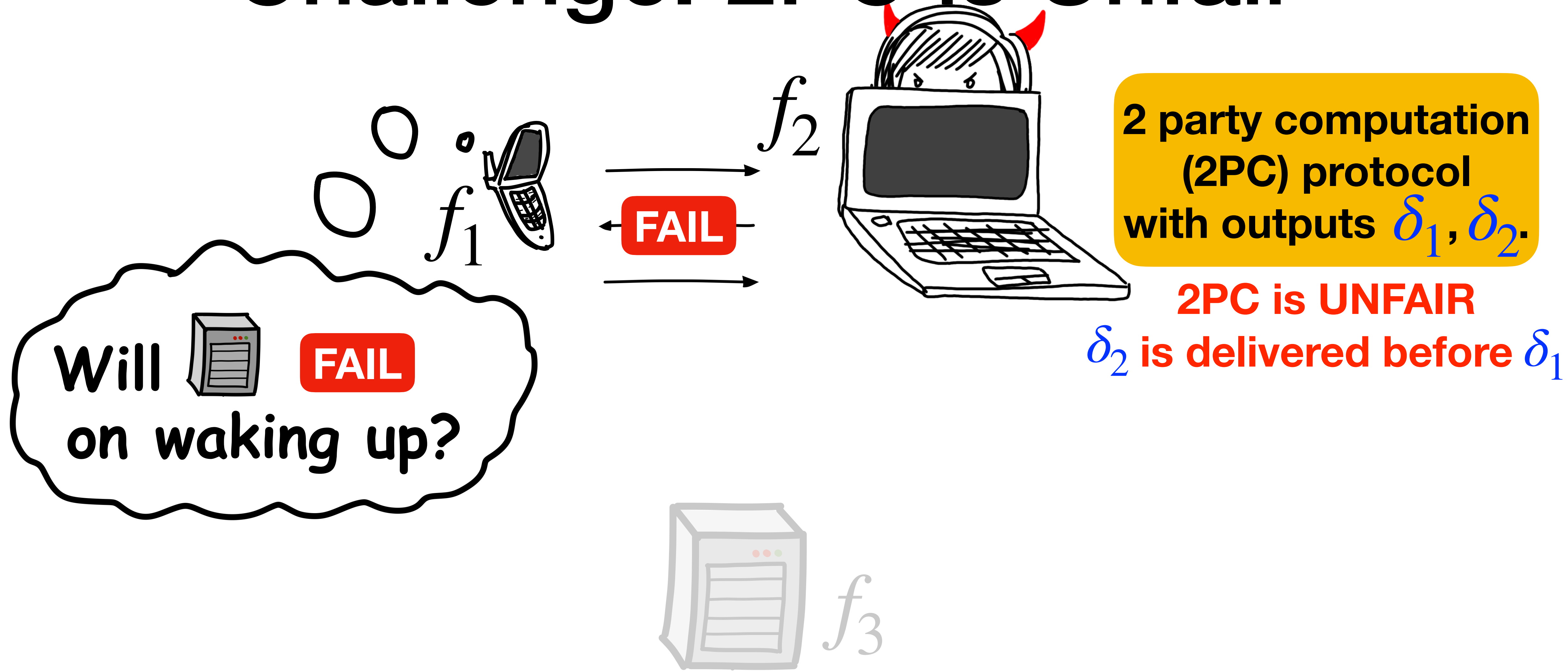
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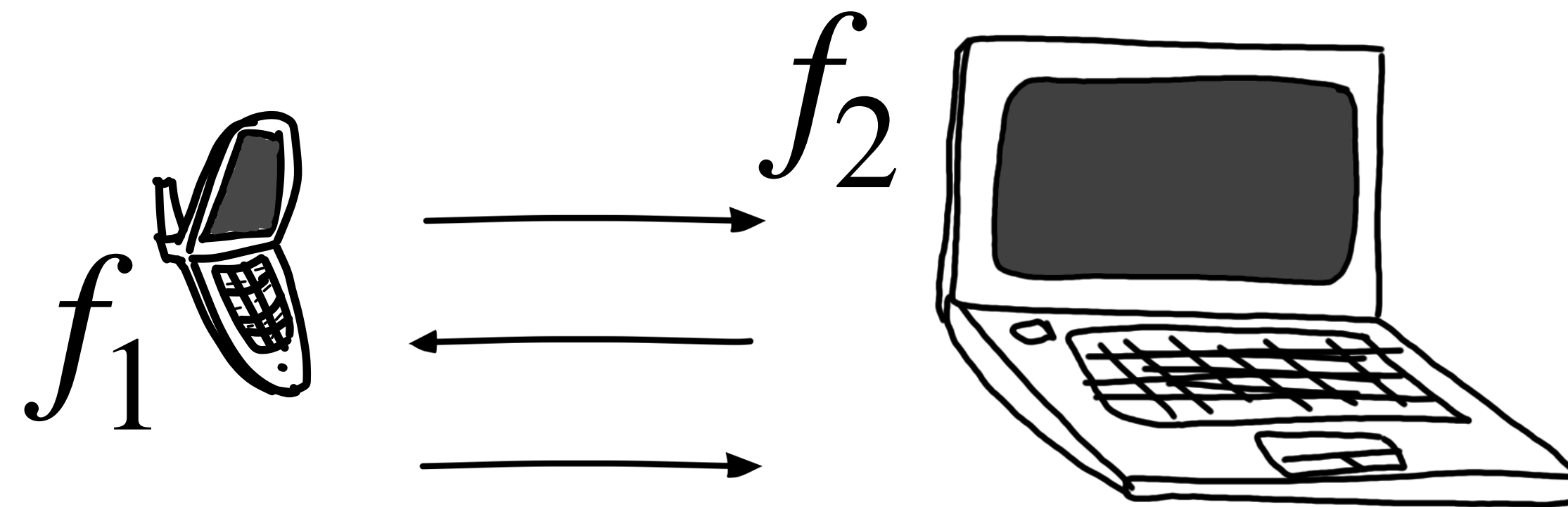
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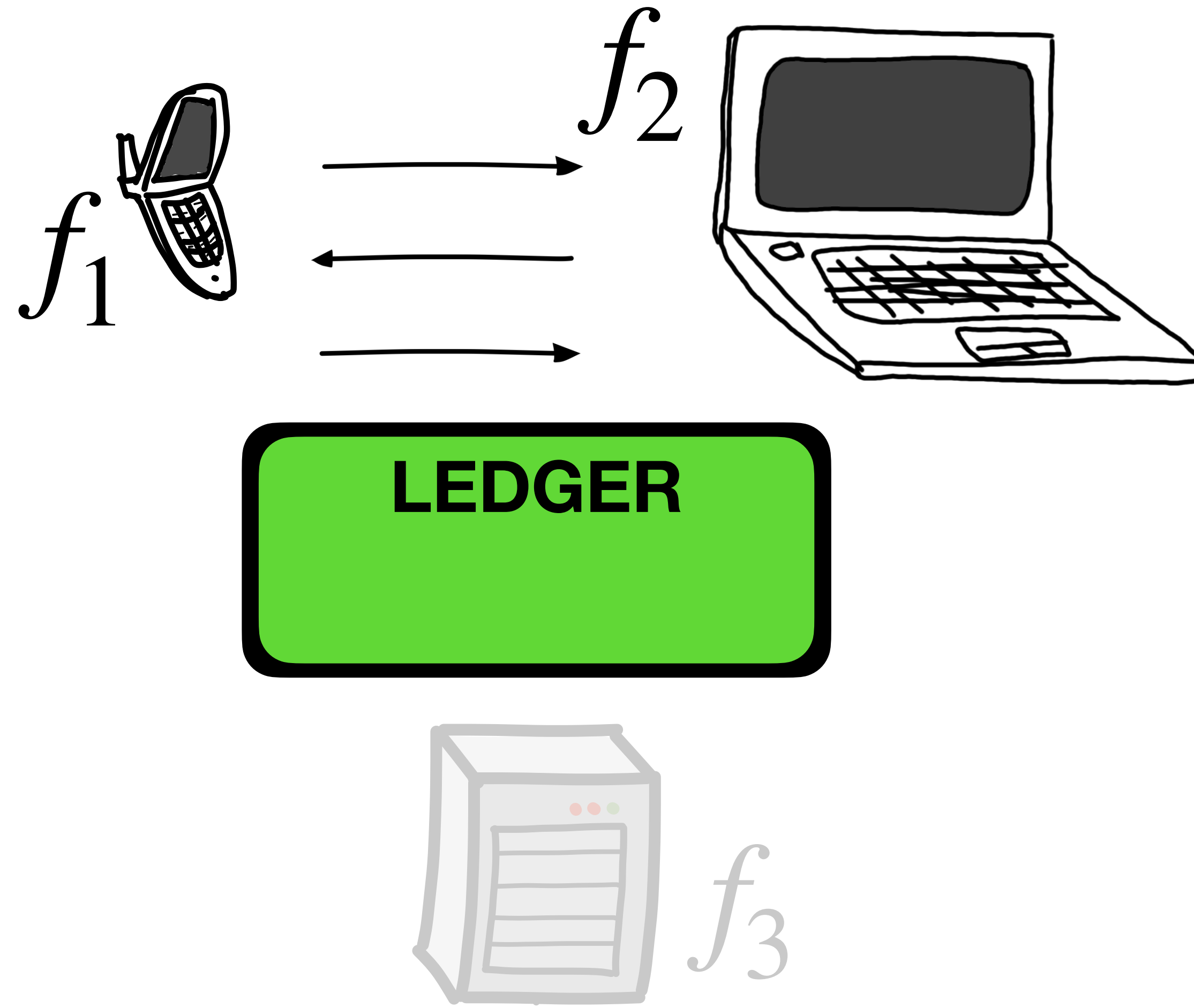


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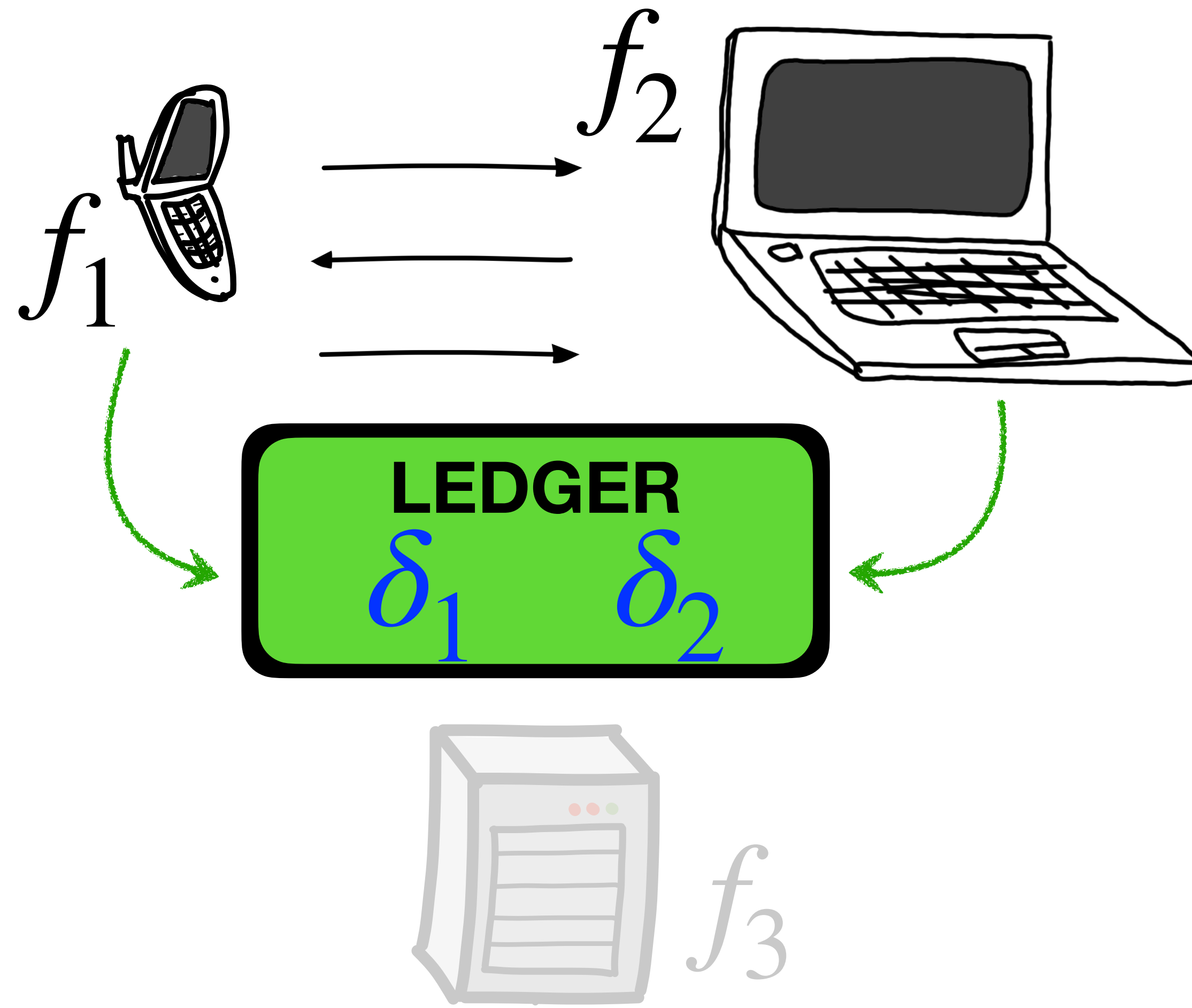
# Towards a Solution



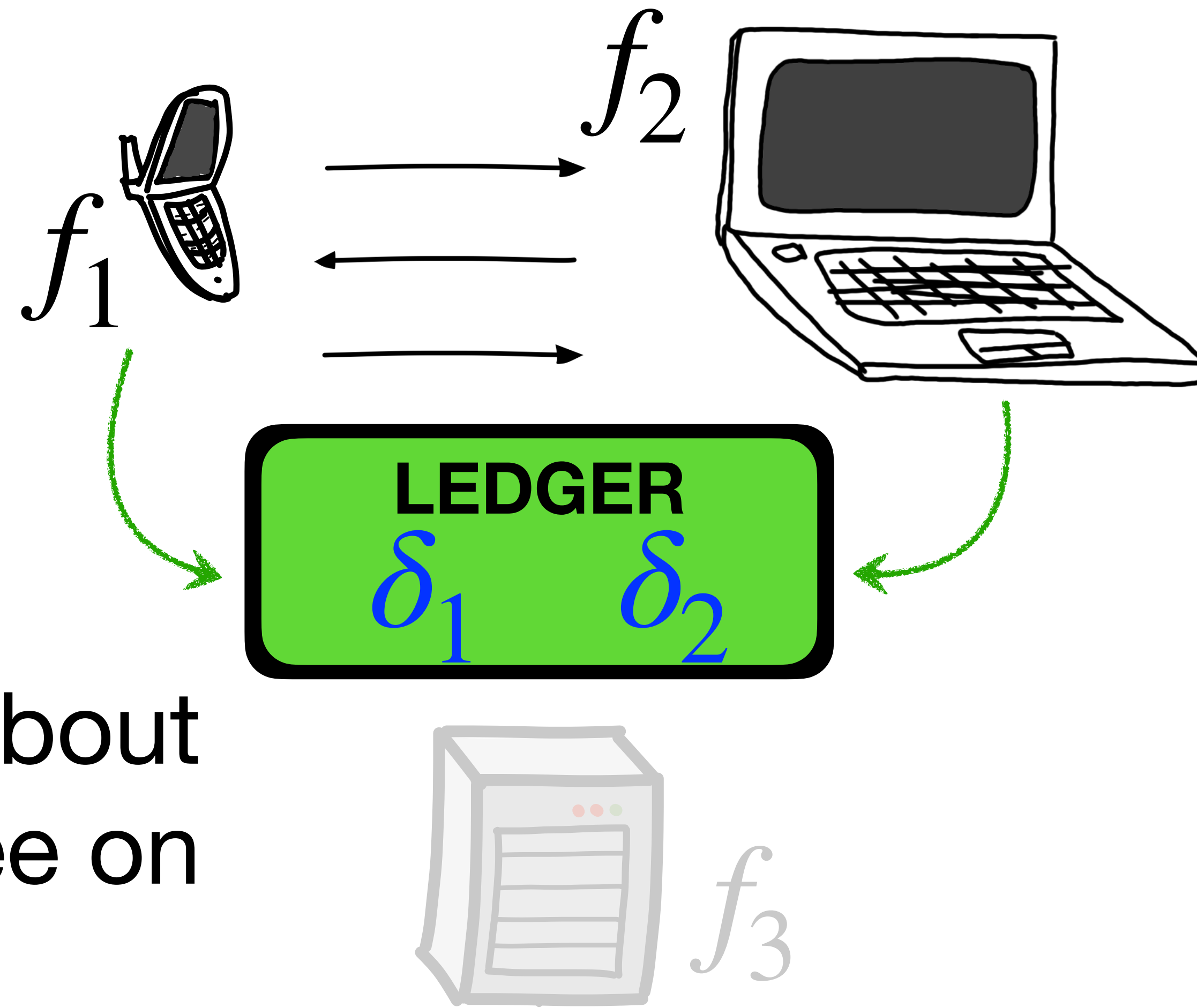
# Towards a Solution

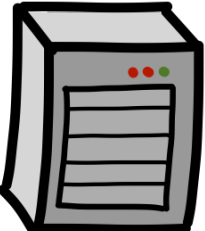


# Towards a Solution

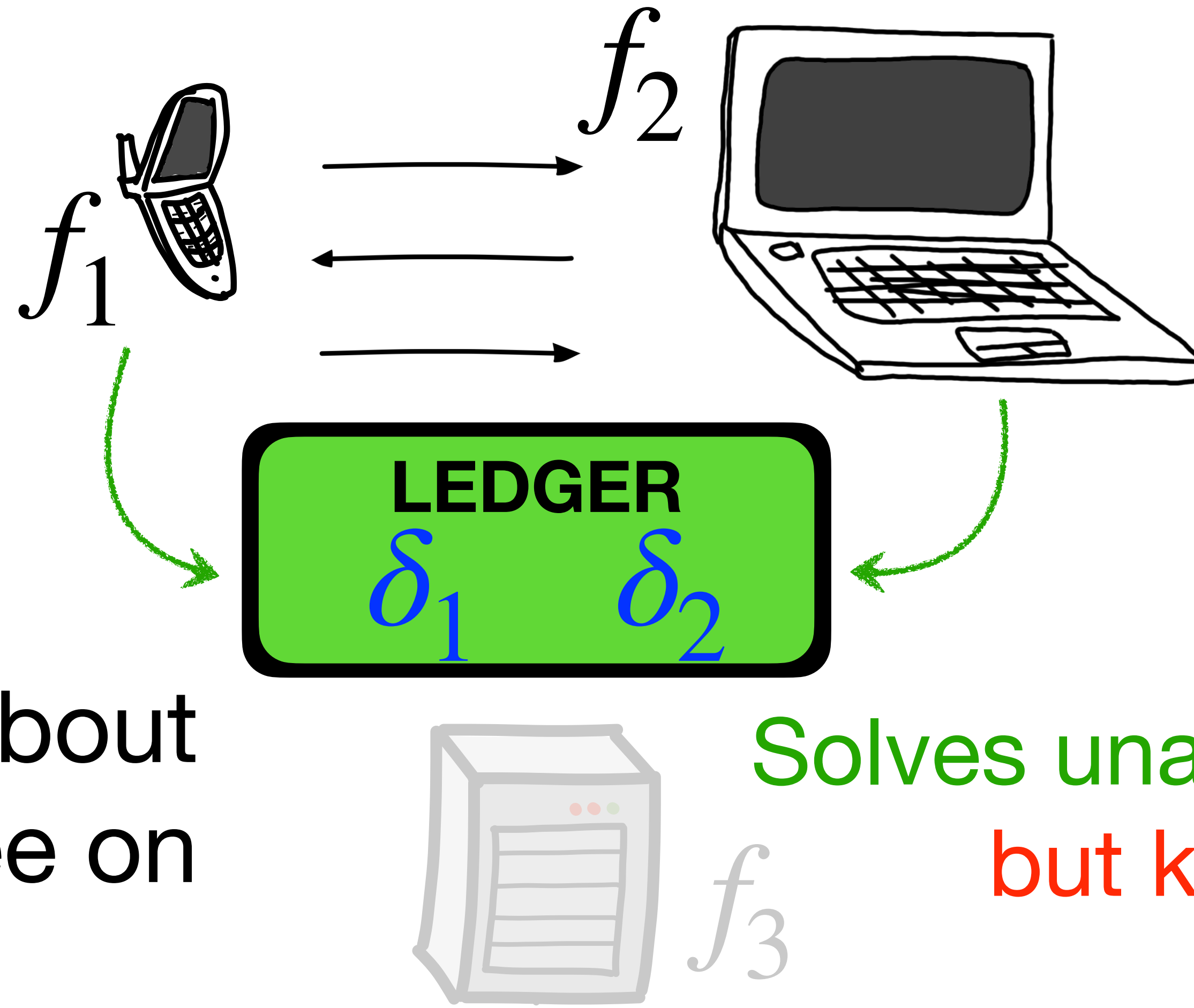


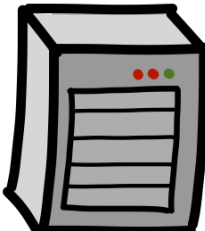
# Towards a Solution



No ambiguity about  
what  will see on  
waking up

# Towards a Solution



No ambiguity about  
what  will see on  
waking up

Solves unanimous erasure,  
but kills privacy

# General Problem Flavour

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- Public channels can be verified but can't convey private information
- **Our approach:** use P2P channels to convey  $\delta_1, \delta_2$  and ledger to achieve consensus on whether or not to use them.
- Public and private values are linked via nonces of sigs created by *interleaved threshold signing*

# ECDSA / Schnorr

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Discrete logarithm based signatures

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Public key:  $X = x \cdot G$

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$\downarrow$

$\mathbb{G}$

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$\downarrow$   $\downarrow$

$\mathbb{G}$   $\mathbb{Z}_q$

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Public key:  $X = x \cdot G$

$\downarrow$   $\downarrow$

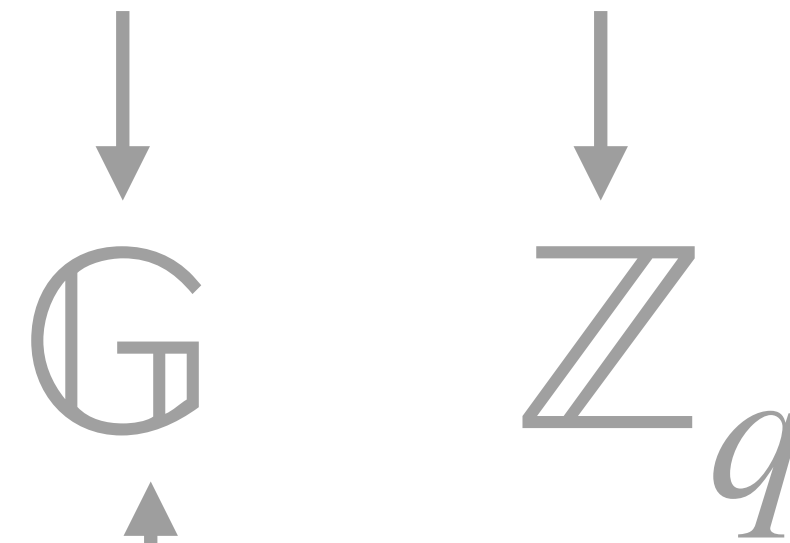
$\mathbb{G}$   $\mathbb{Z}_q$

Signatures:  $(R, \sigma)$

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Public key:  $X = x \cdot G$

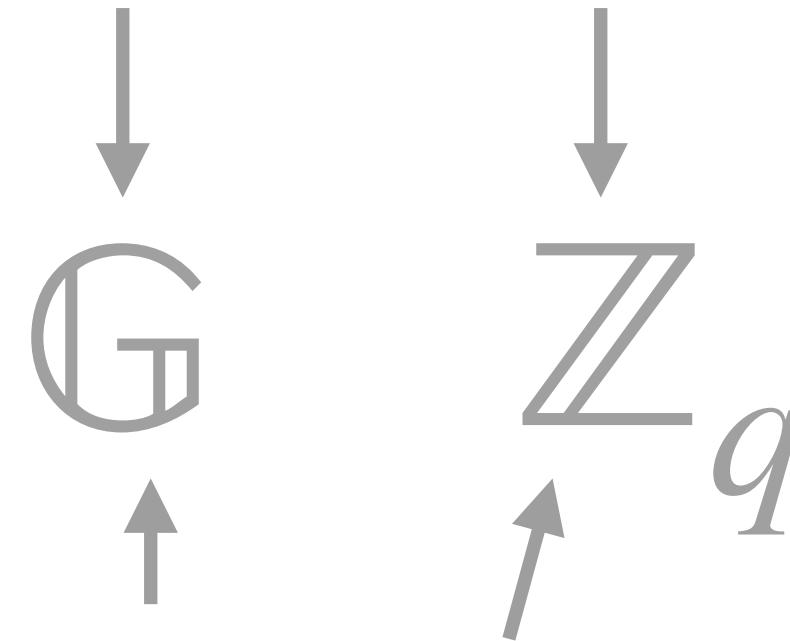


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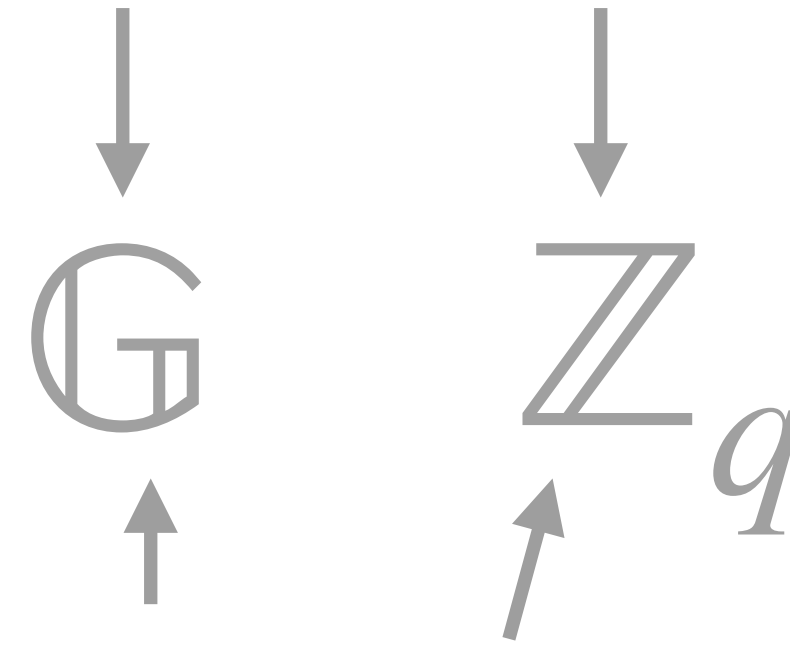


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Discrete logarithm based signatures

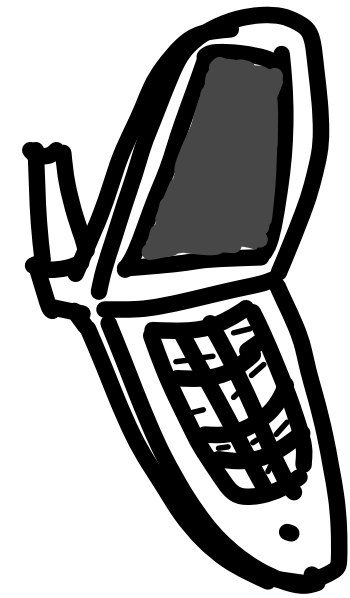
Public key:  $X = x \cdot G$



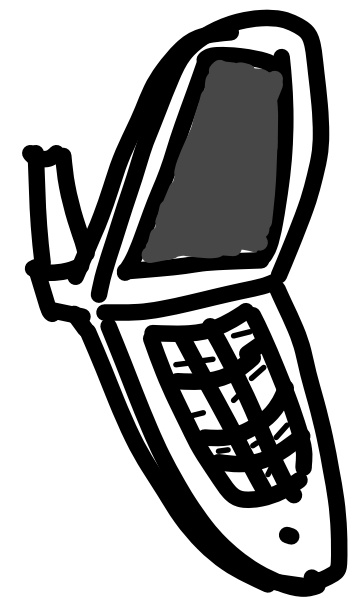
Signatures:  $(R, \sigma)$

**Random**

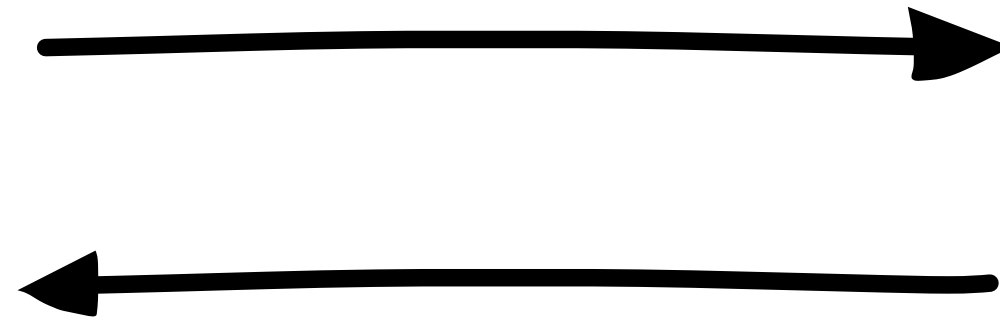
# Threshold ECDSA/Schnorr



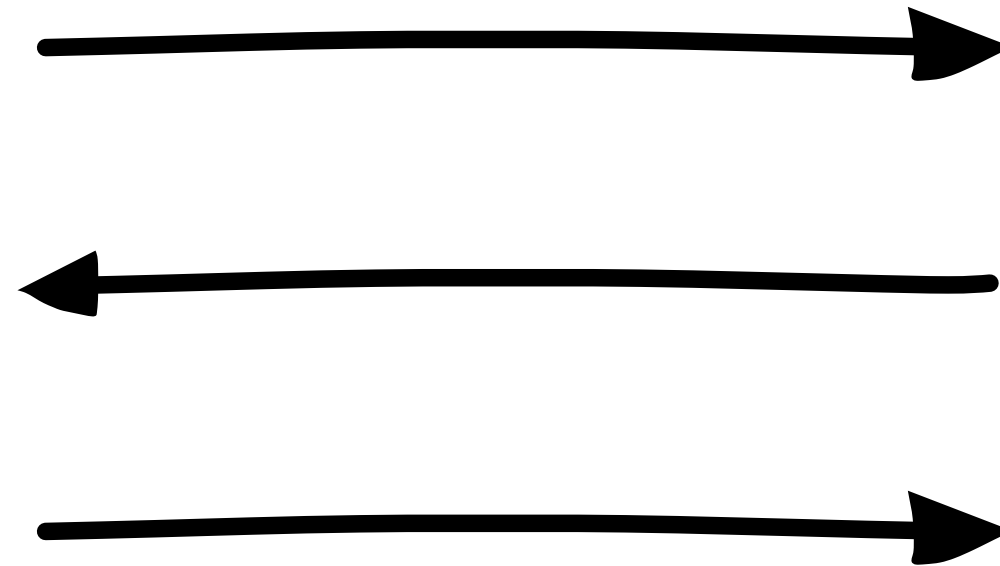
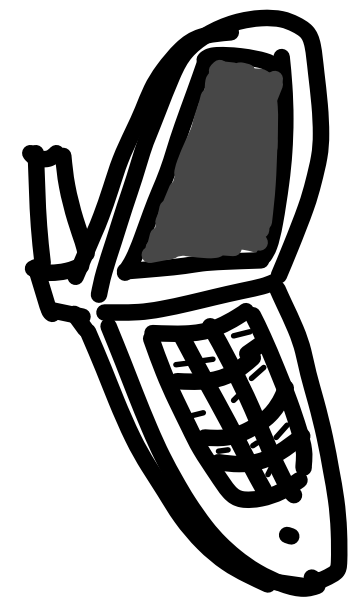
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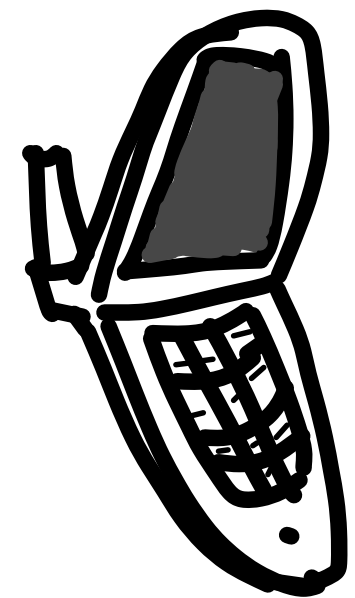
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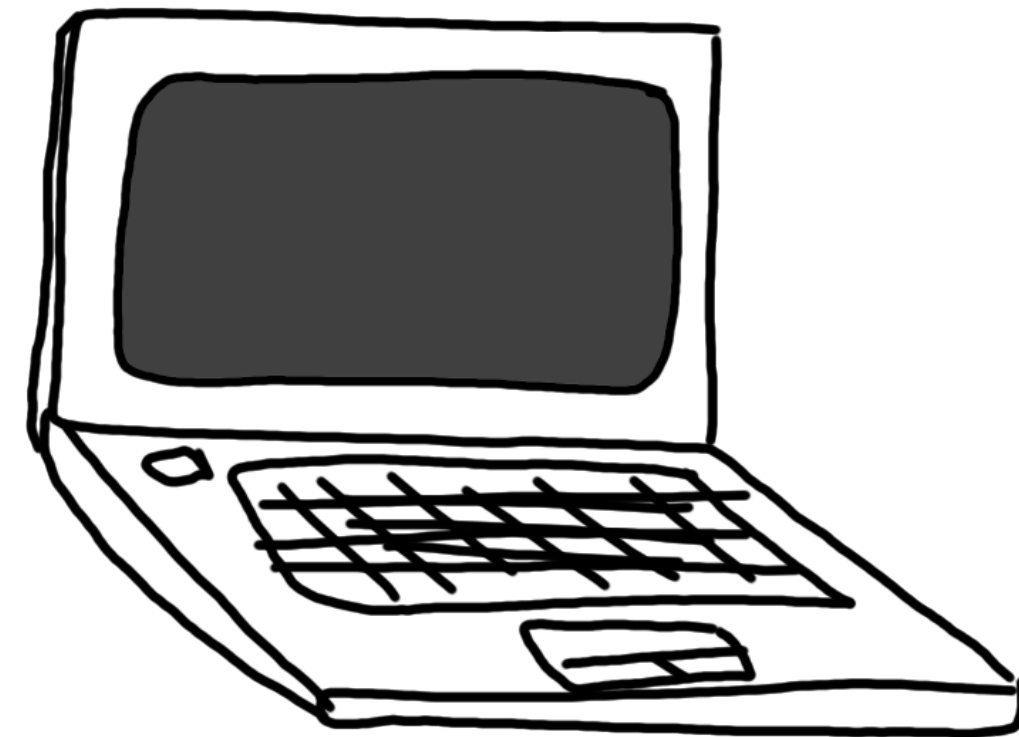
$R$



# Threshold ECDSA/Schnorr



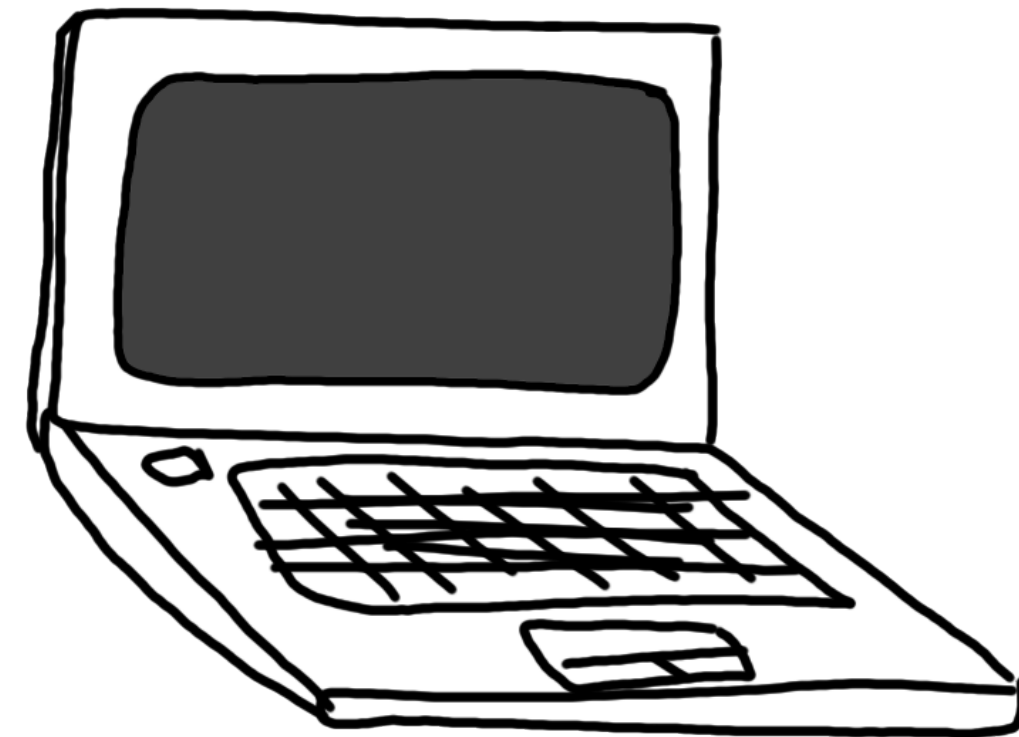
$R$



# Threshold ECDSA/Schnorr



$R$



# Threshold ECDSA/Schnorr



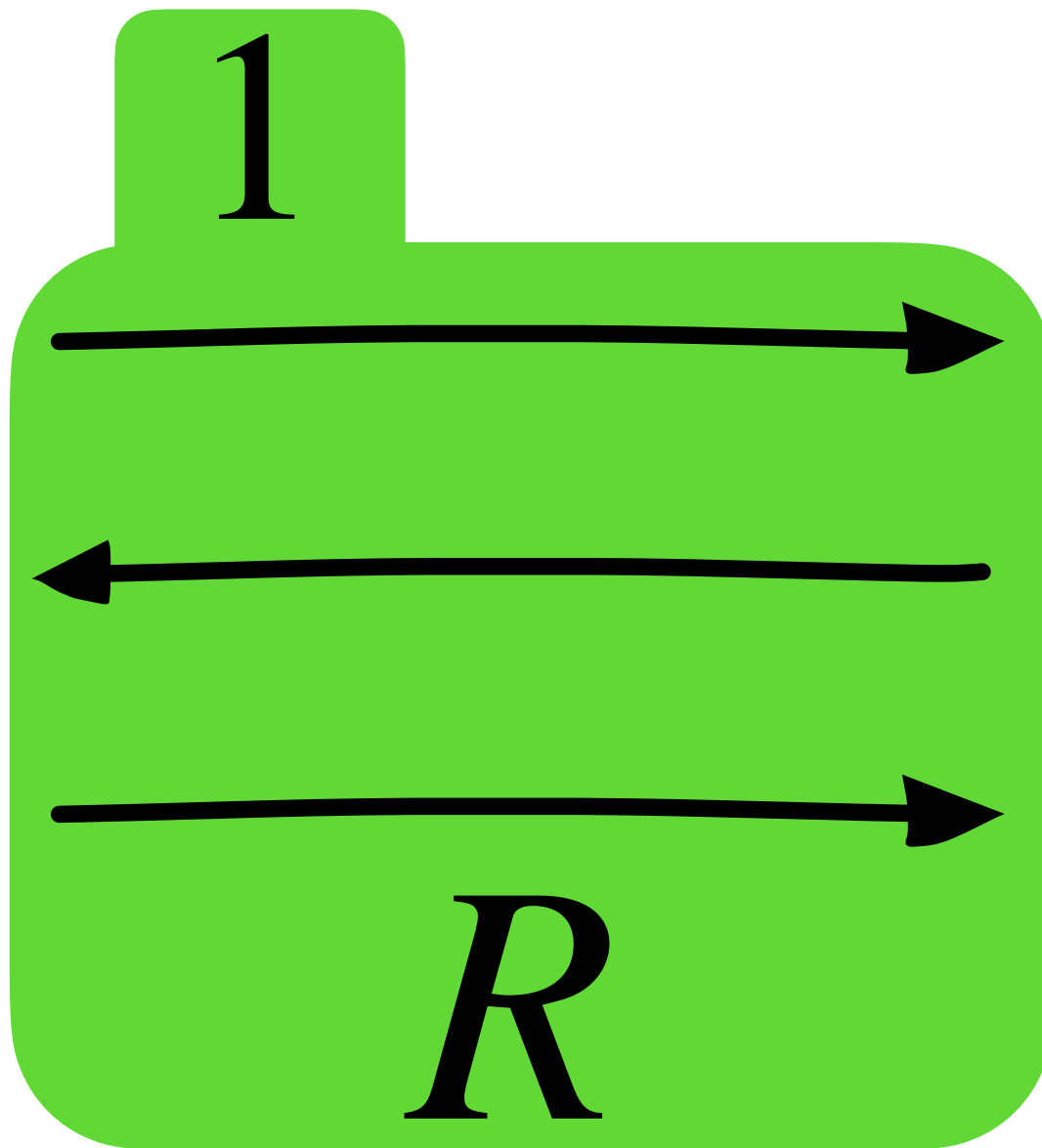
$R$



$\sigma$

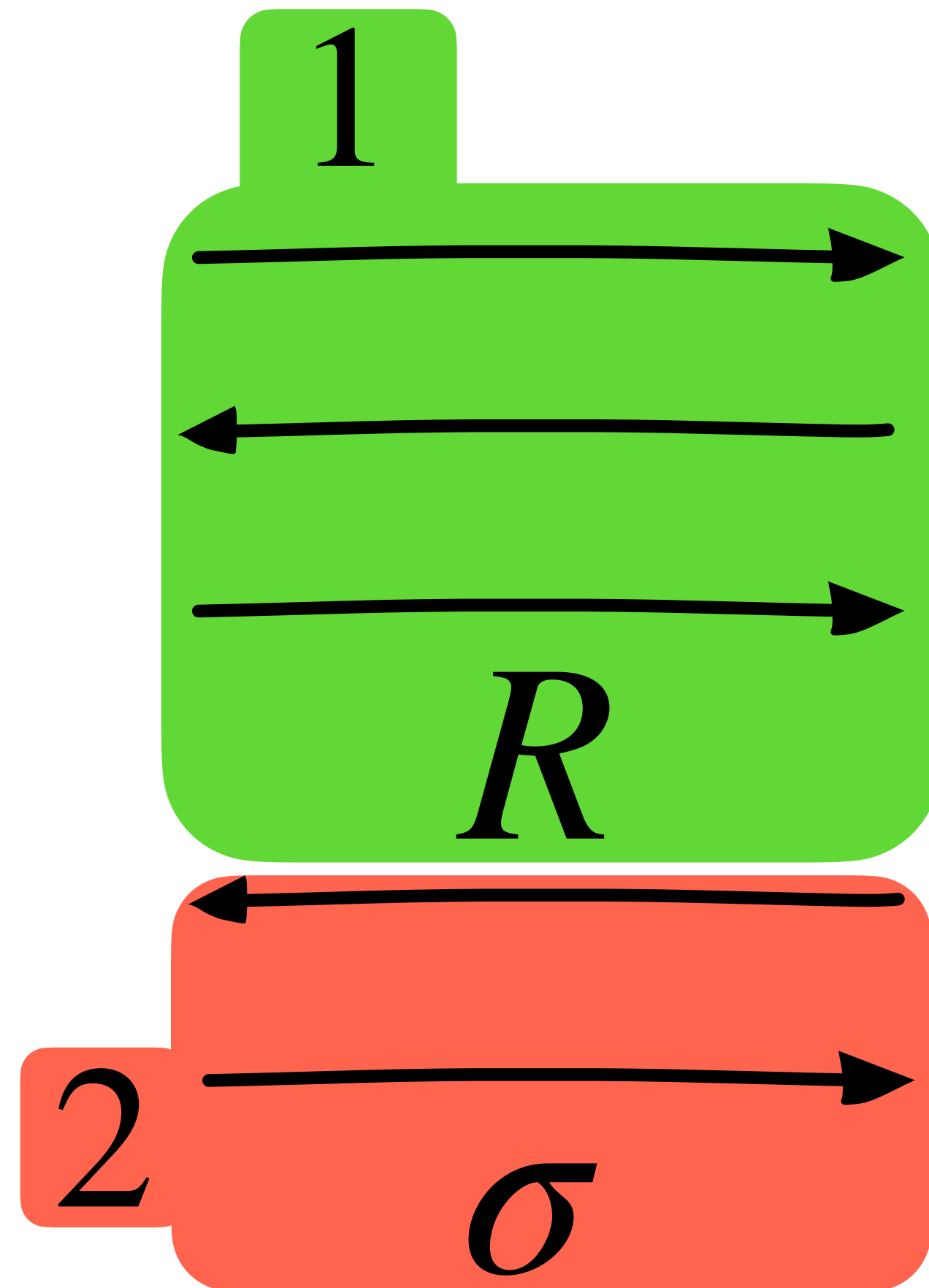
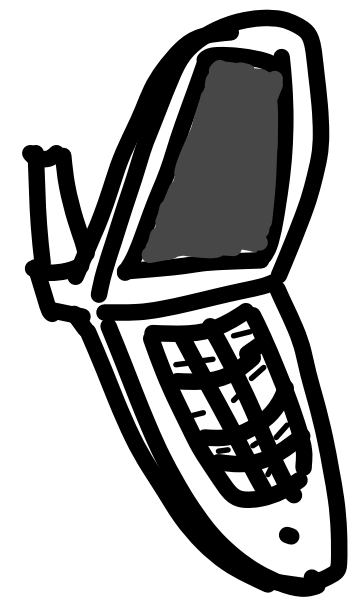


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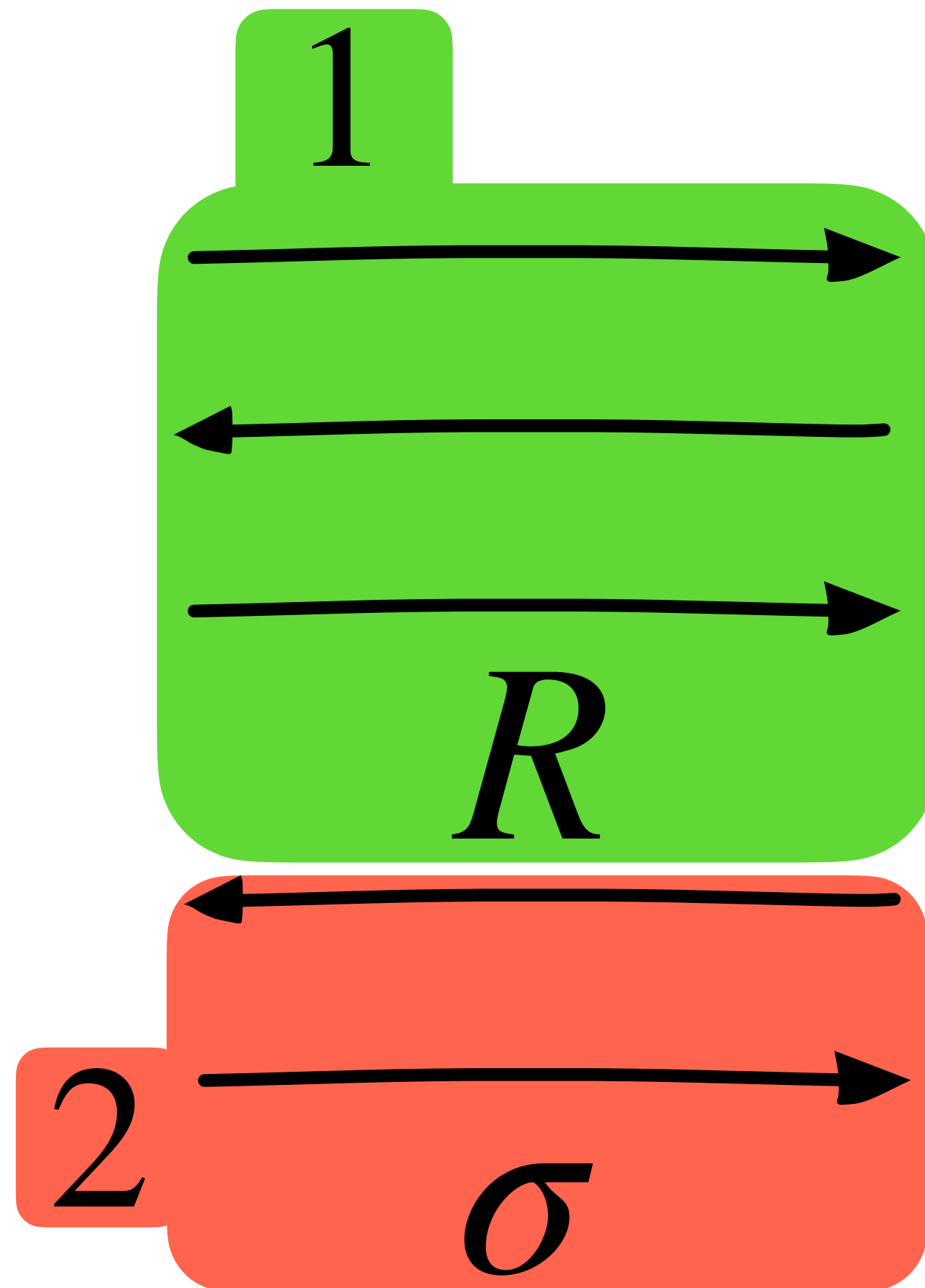
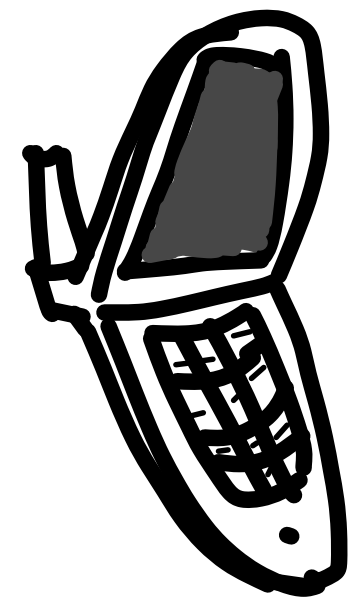


$\sigma$

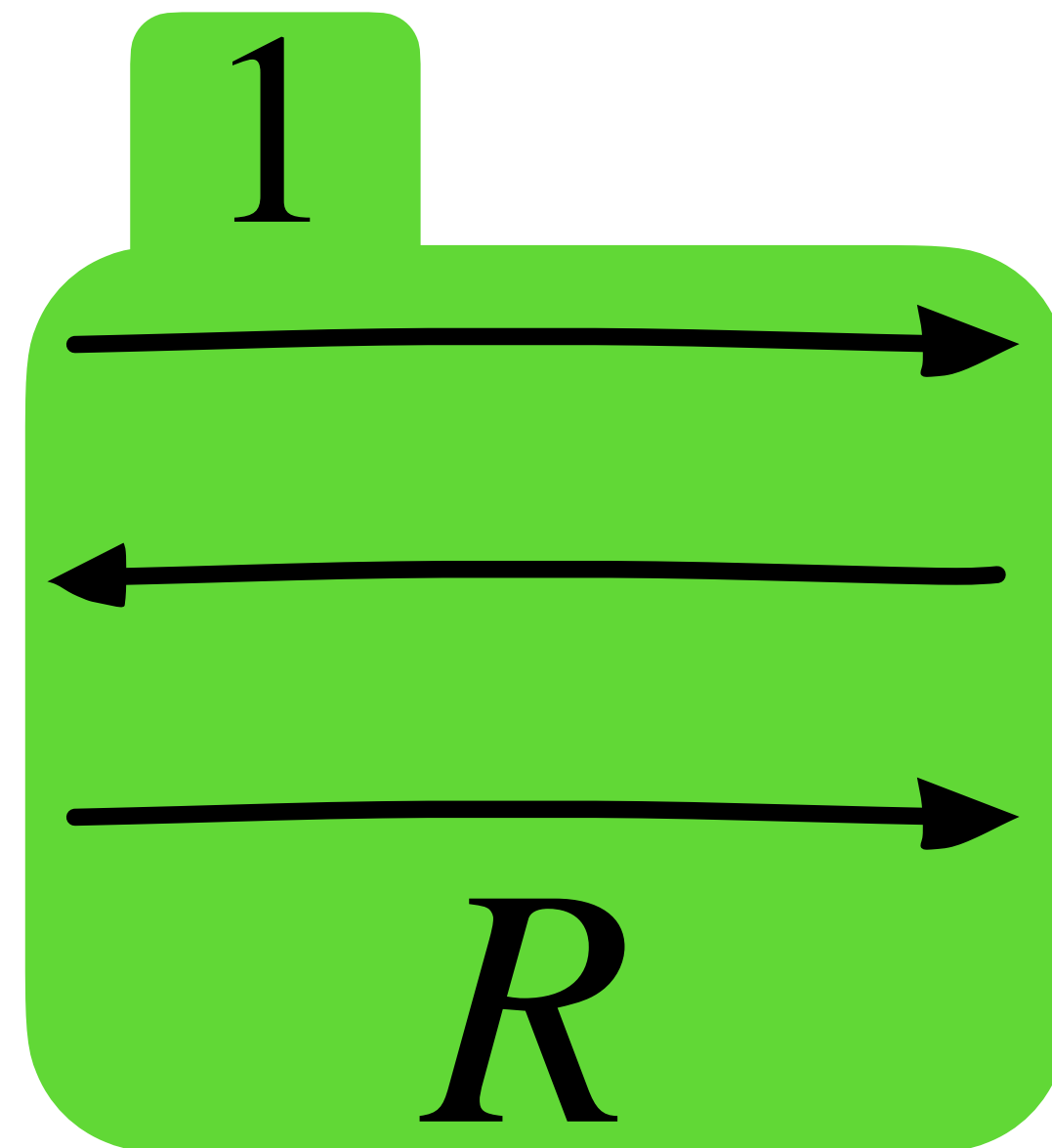
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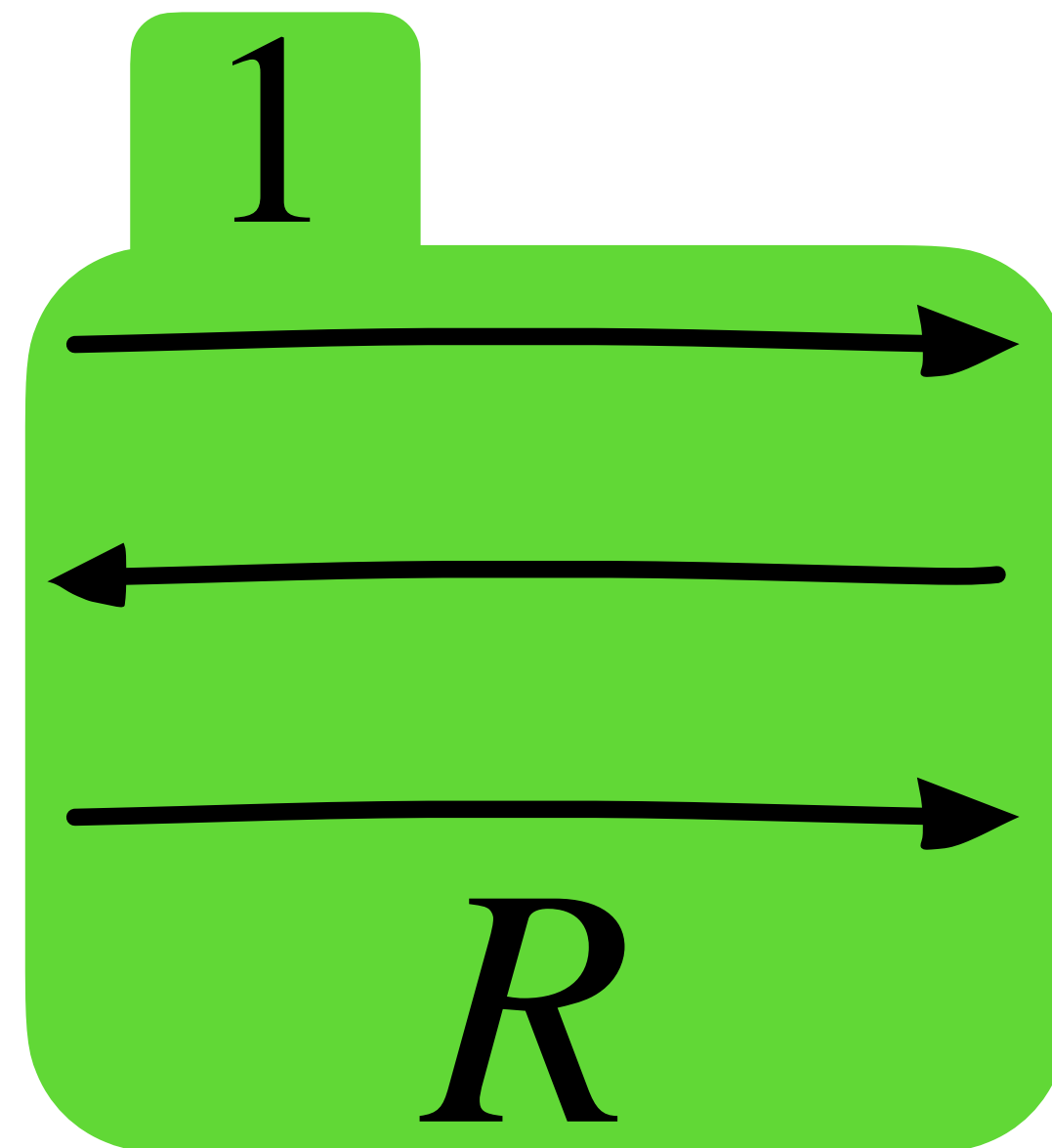
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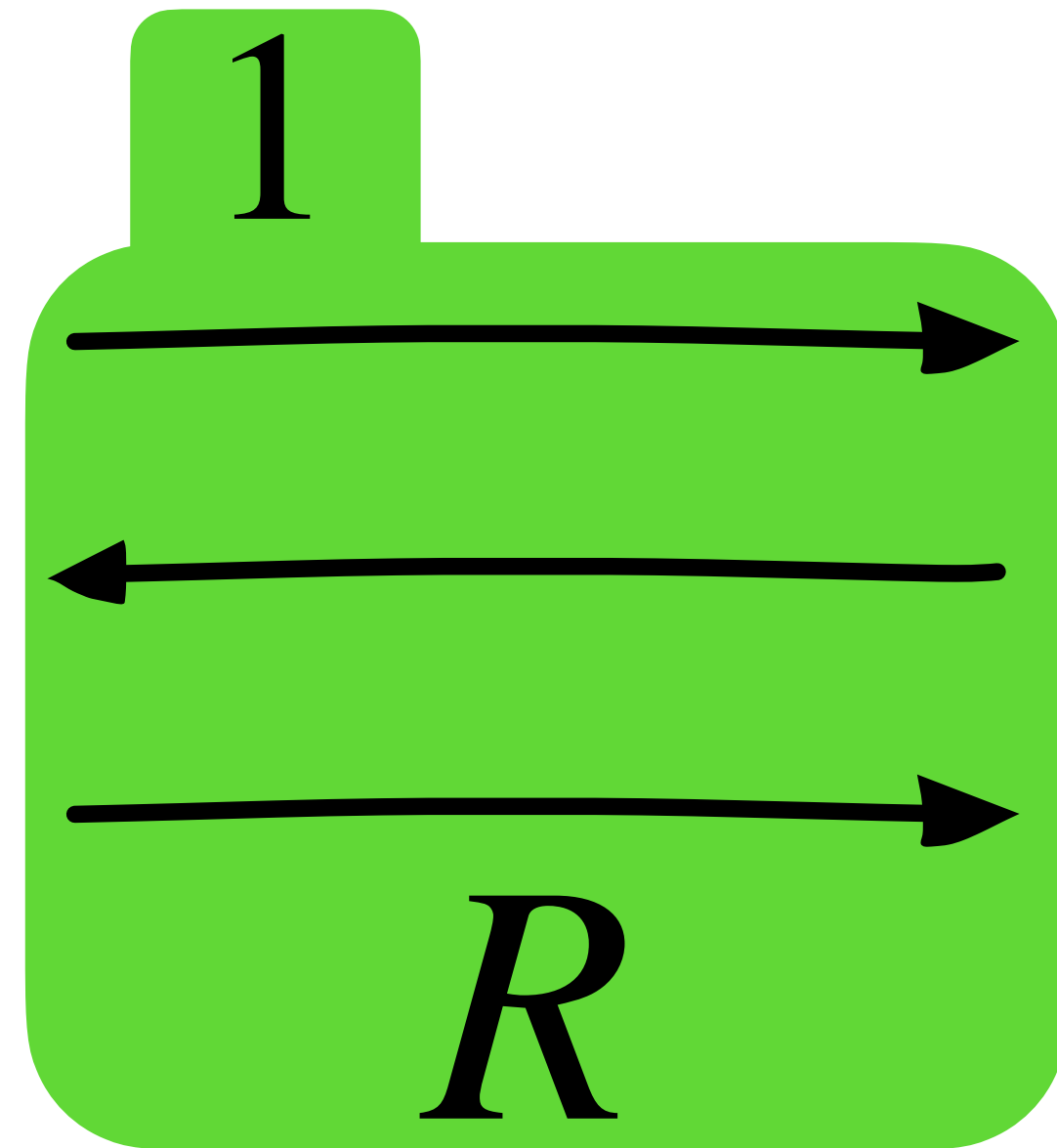
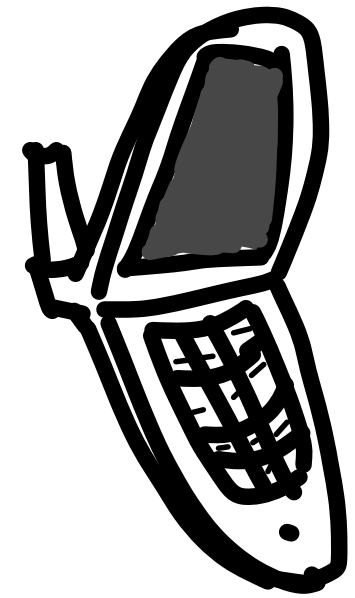
# Threshold ECDSA/Schnorr



FAIL



# Threshold ECDSA/Schnorr

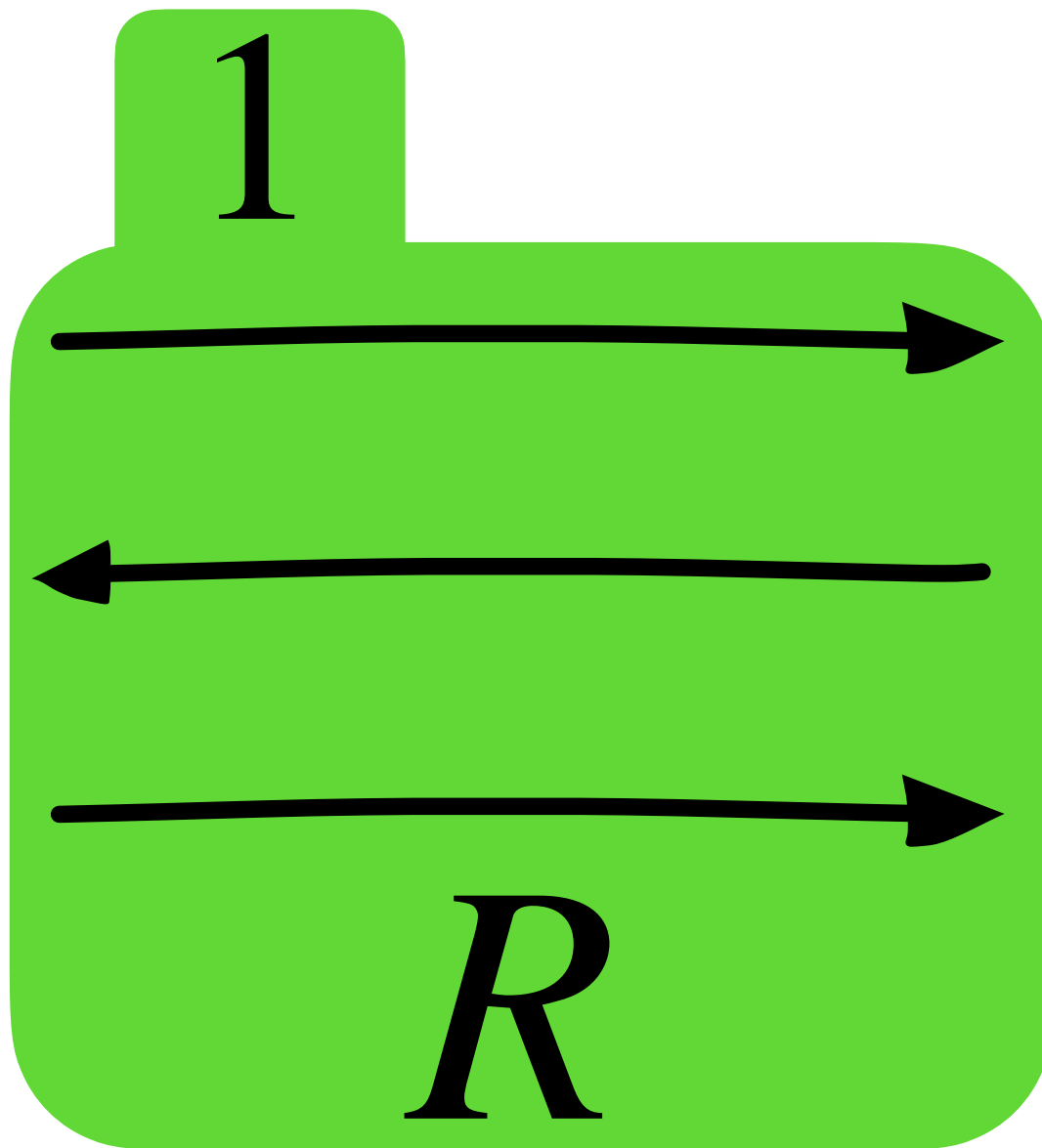


FAIL



Signatures:  $(R, \sigma)$

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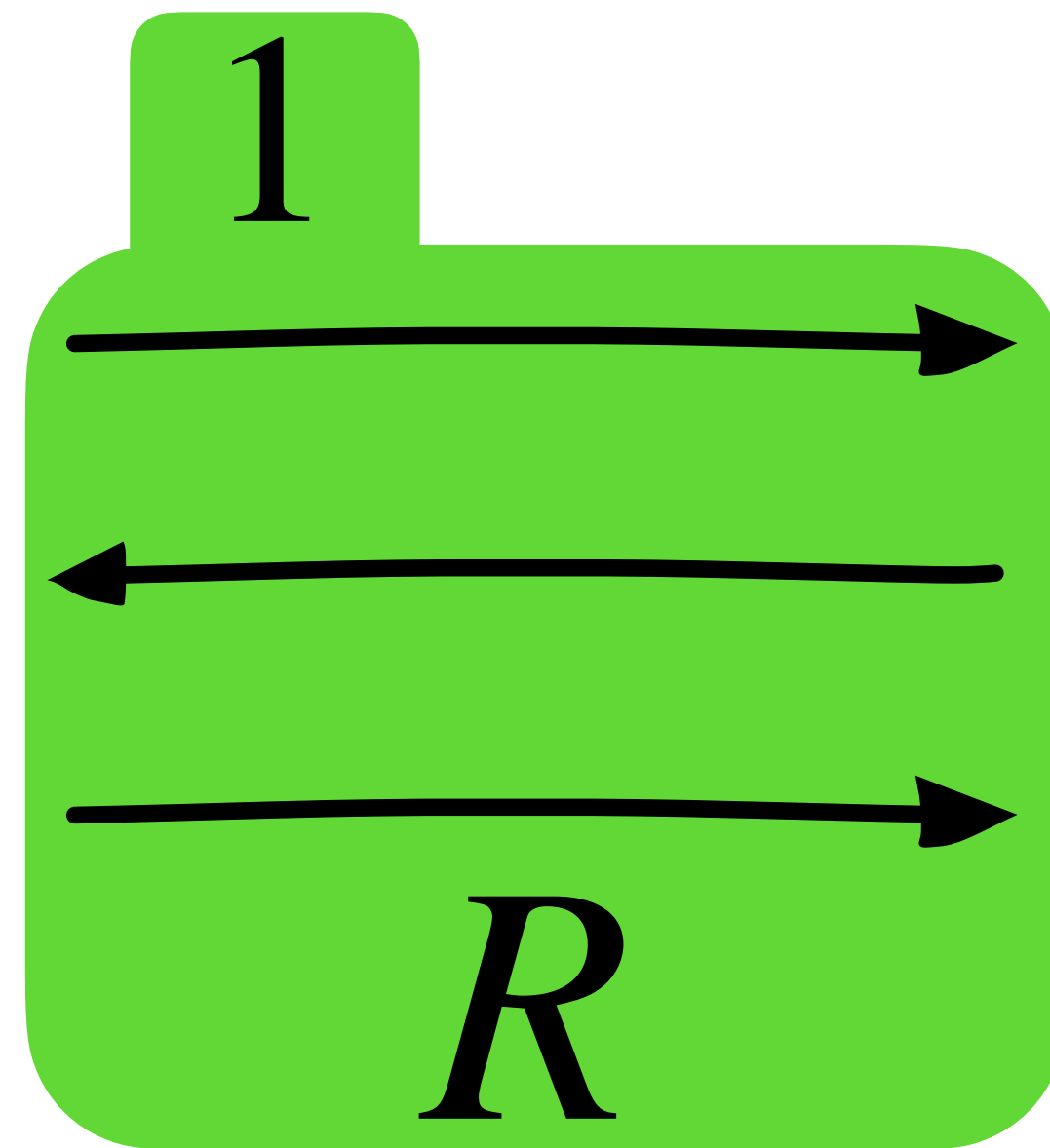


FAIL



Signatures:  $(R, \sigma)$

# Threshold ECDSA/Schnorr



**FAIL**



**No advantage in  
computing this**

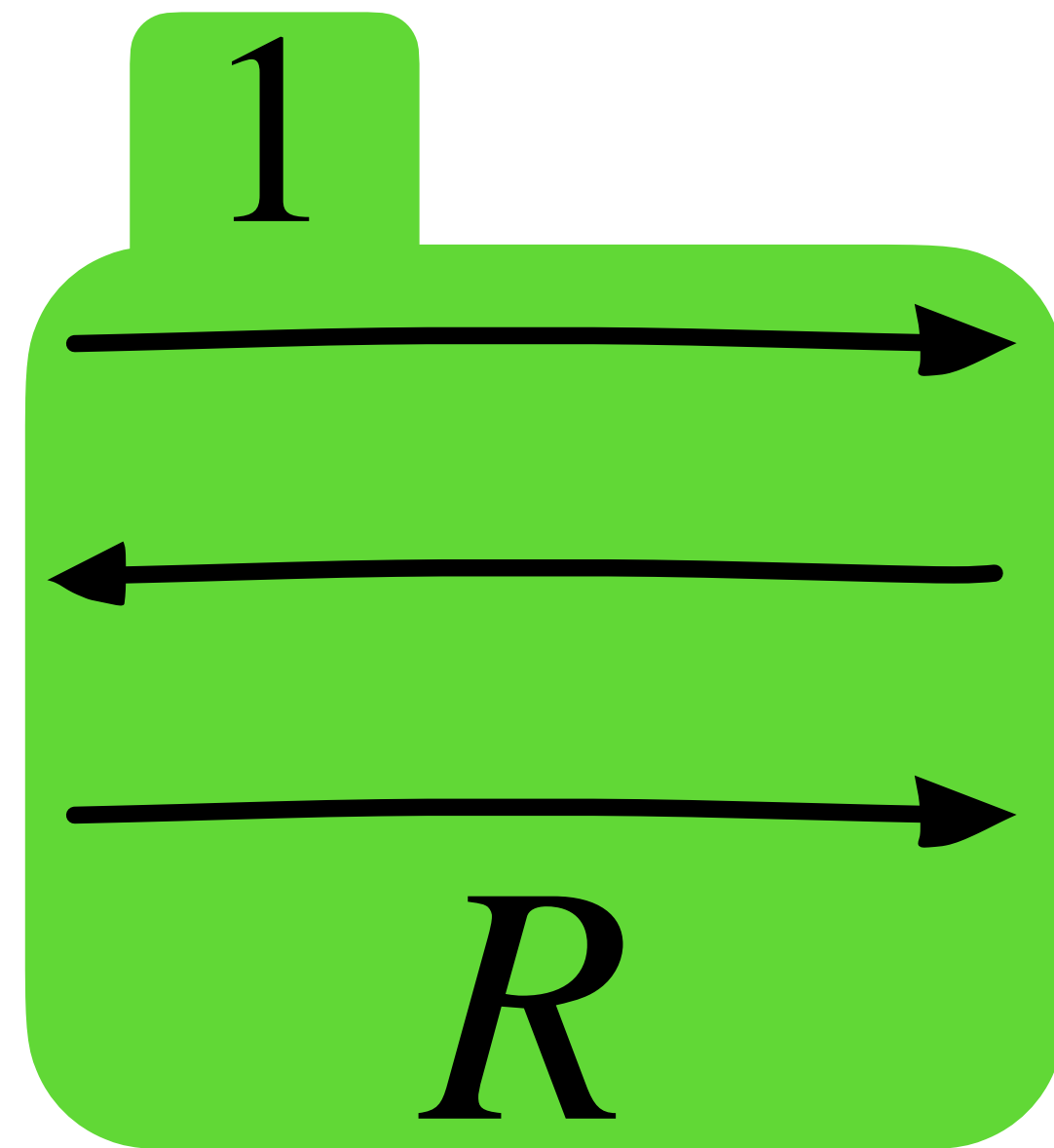
Signatures:  $(R, \sigma)$

# Threshold ECDSA/Schnorr



Achieved by most  
natural thresh Schnorr  
and ECDSA schemes

[DKLs19, GG18,  
LNR18, GJKR07]

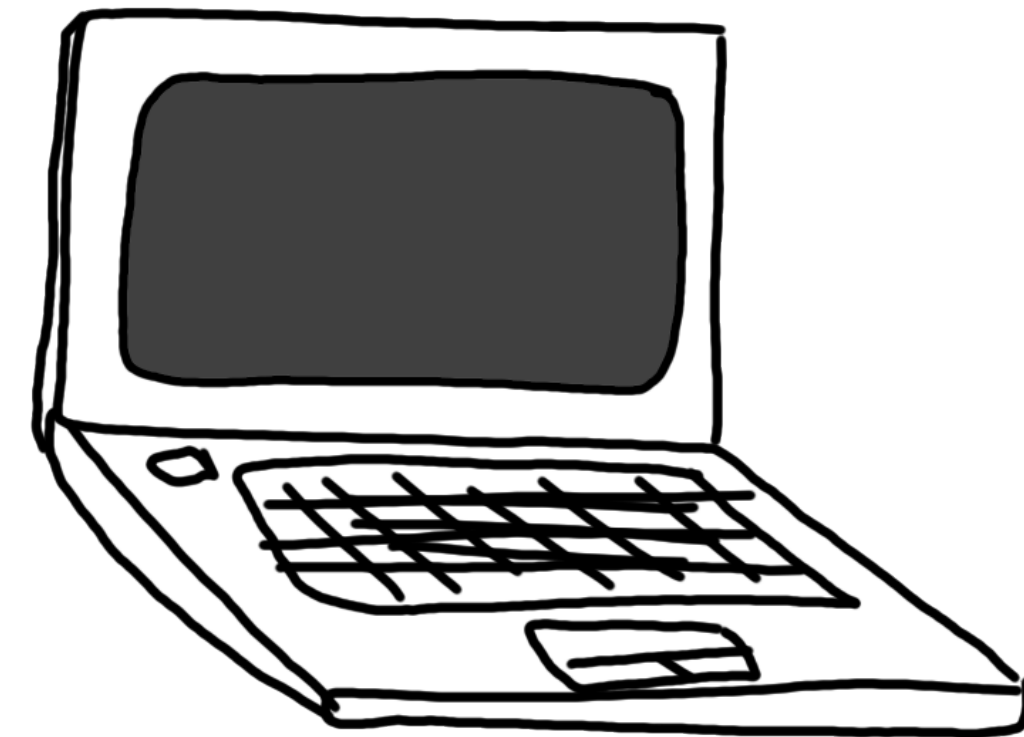
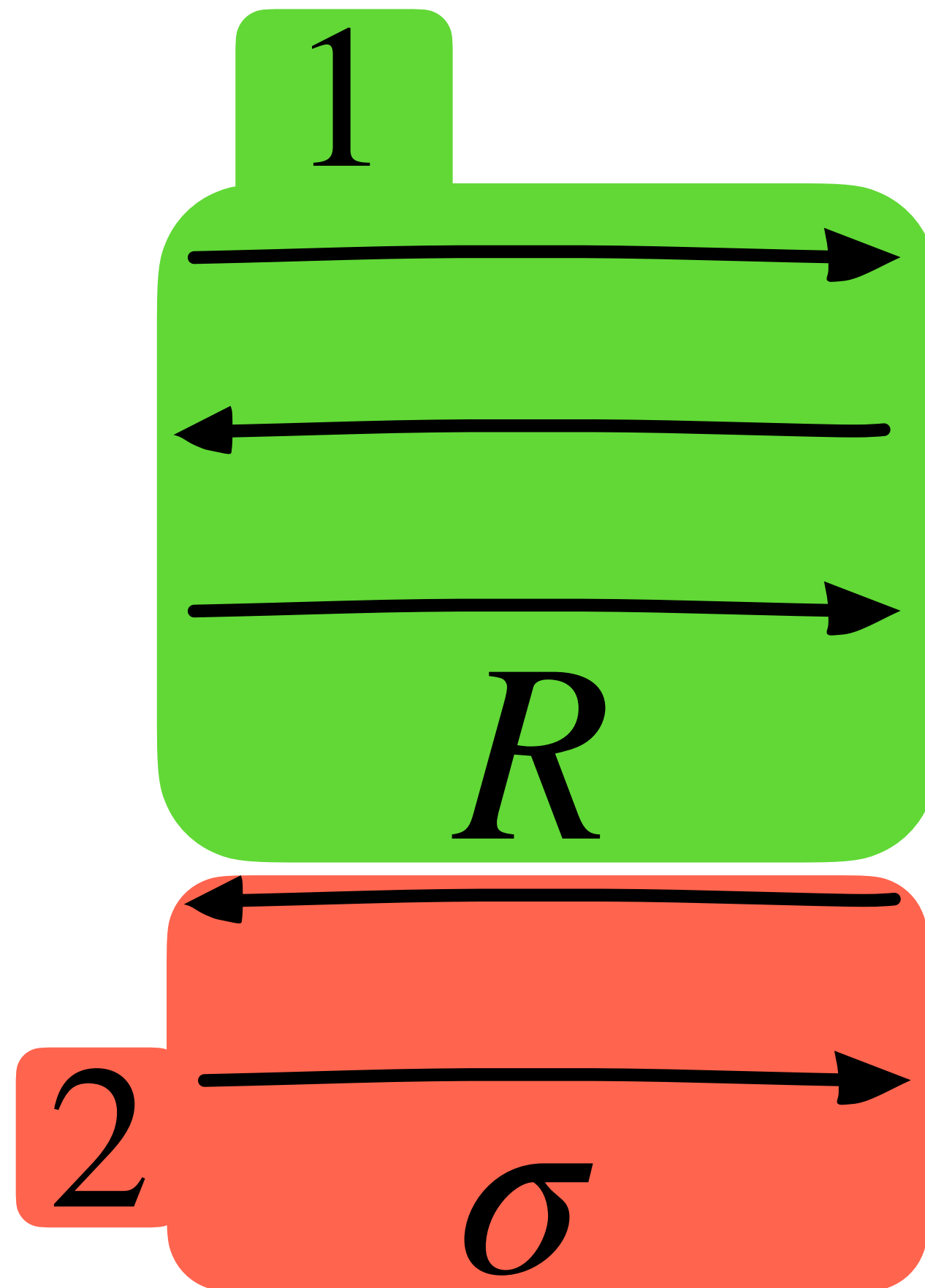
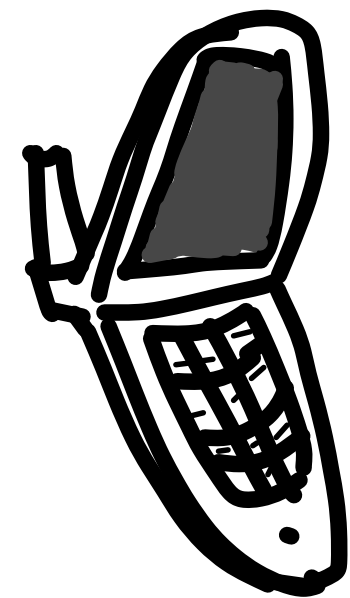


FAIL

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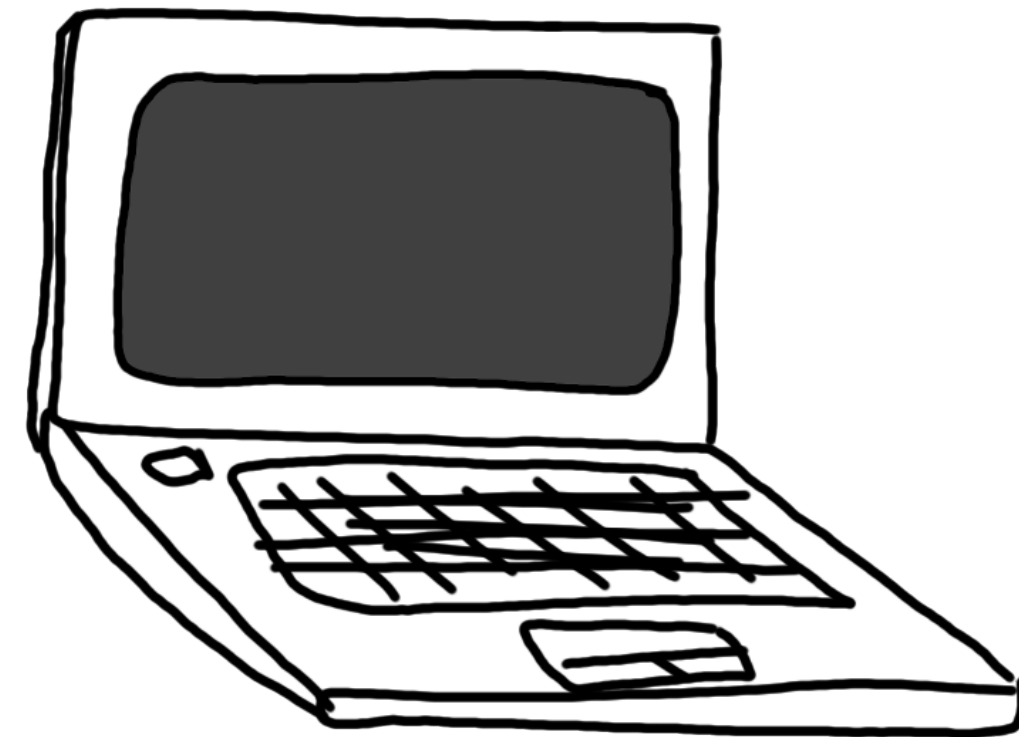
# Threshold ECDSA/Schnorr



# Interleaved Threshold Signing



1  $R$

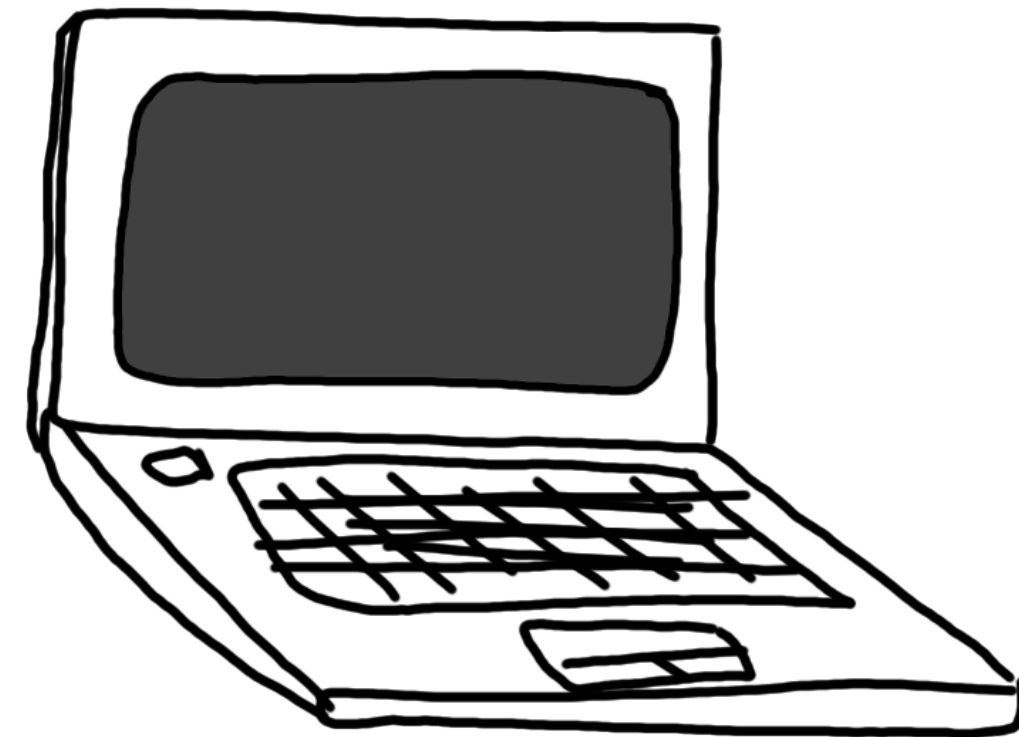


2  $\sigma$

# Interleaved Threshold Signing



1  $R$



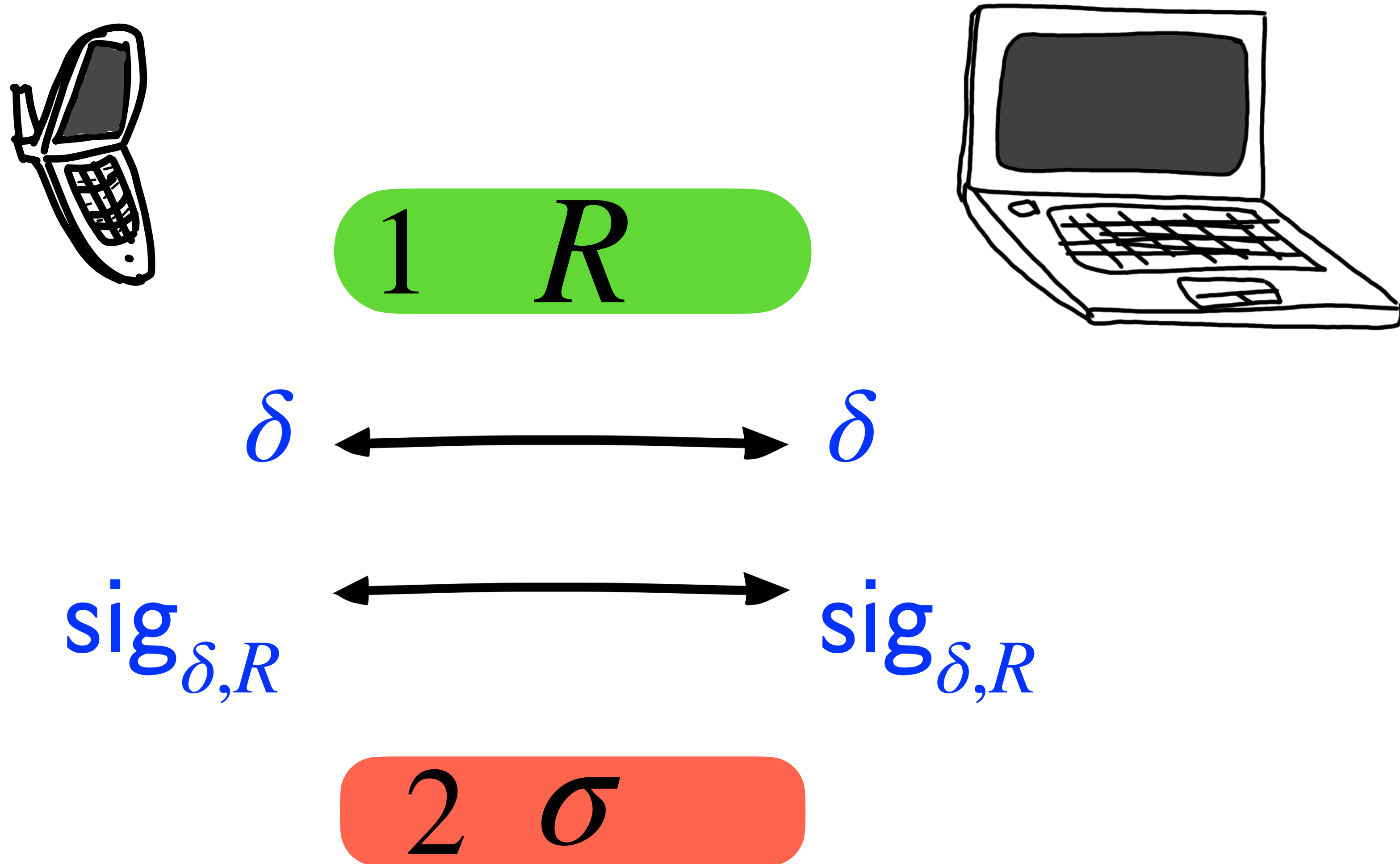
$\delta$



$\delta$

2  $\sigma$

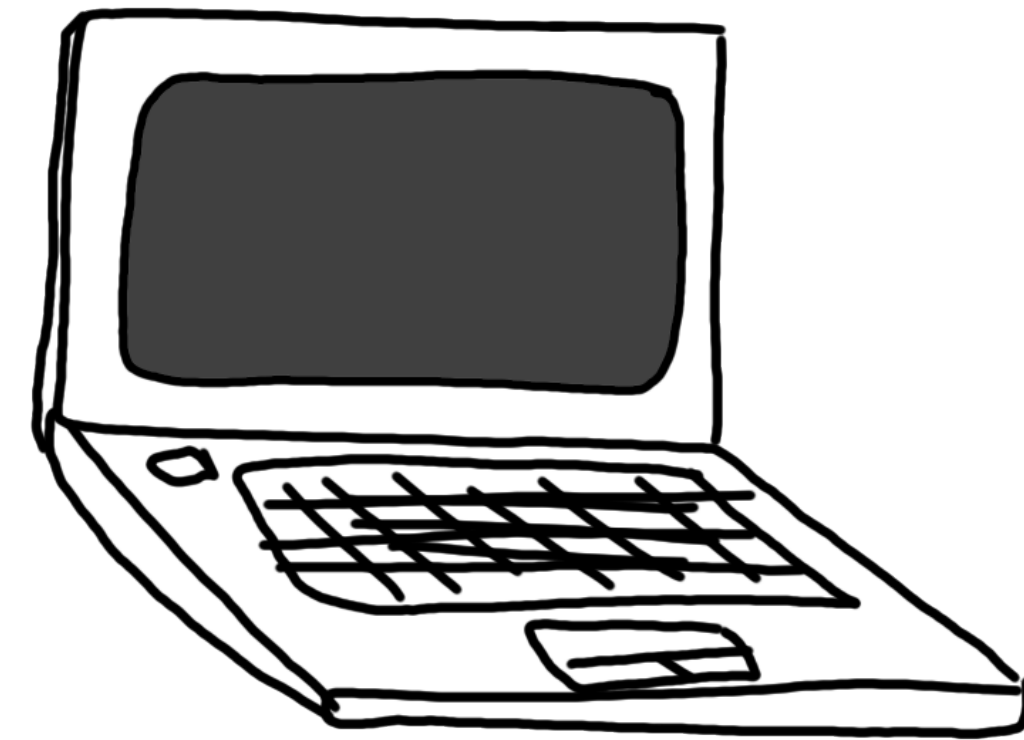
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# Interleaved Threshold Signing



1  $R$



$\delta$   $\text{sig}_{\delta, R}$

2  $\sigma$

# Interleaved Threshold Signing



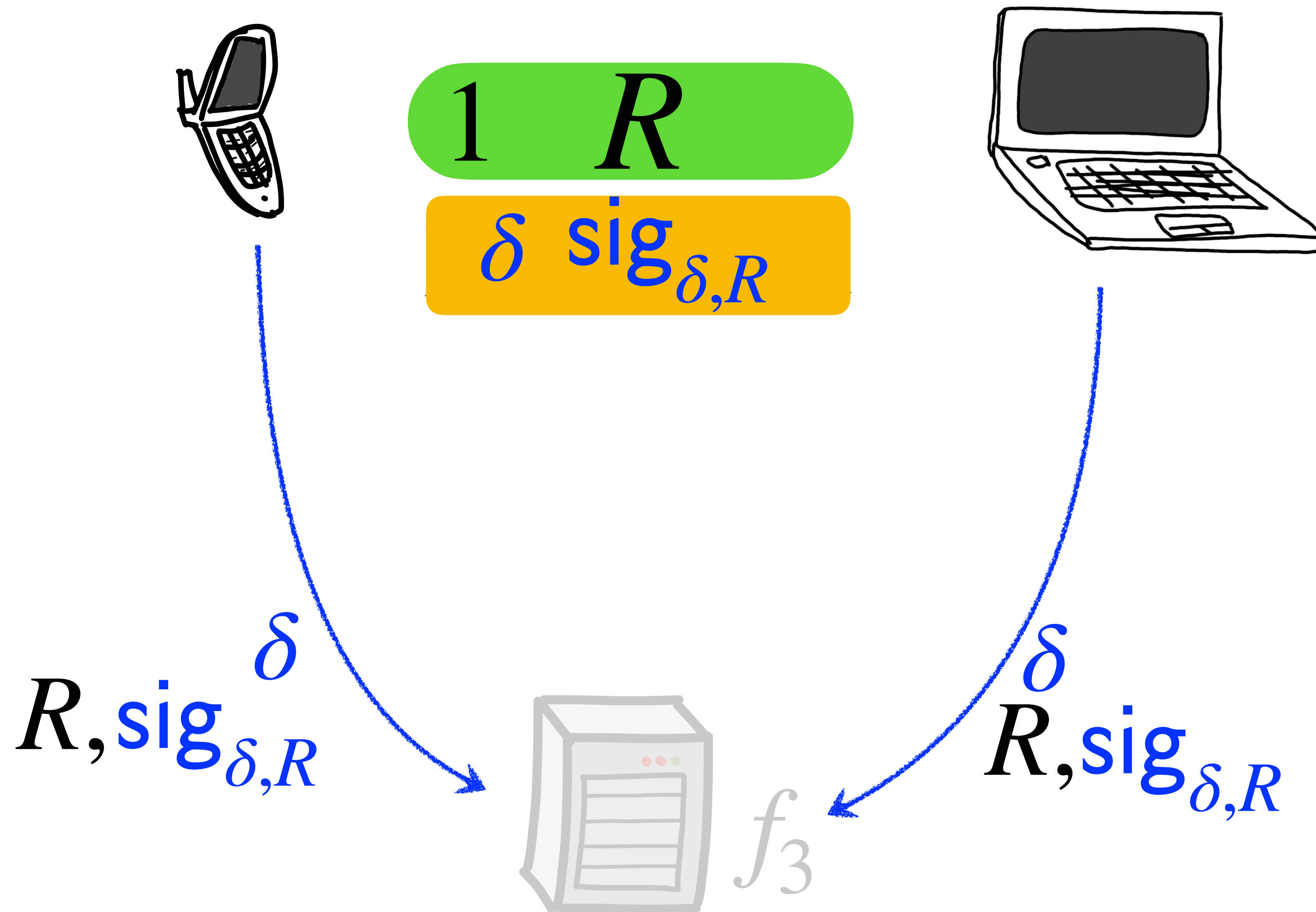
1  $R$

$\delta$   $\text{sig}_{\delta,R}$

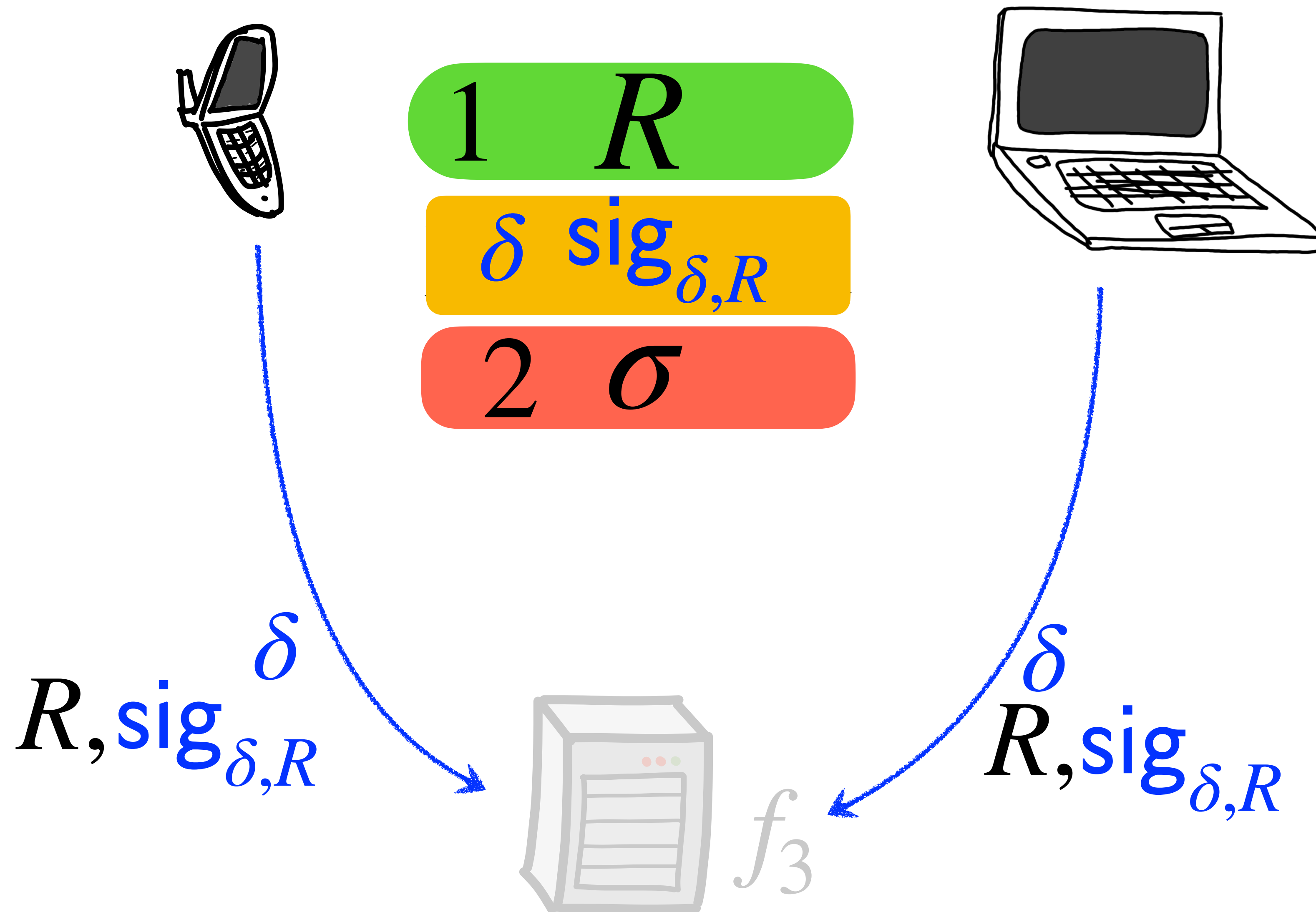


$f_3$

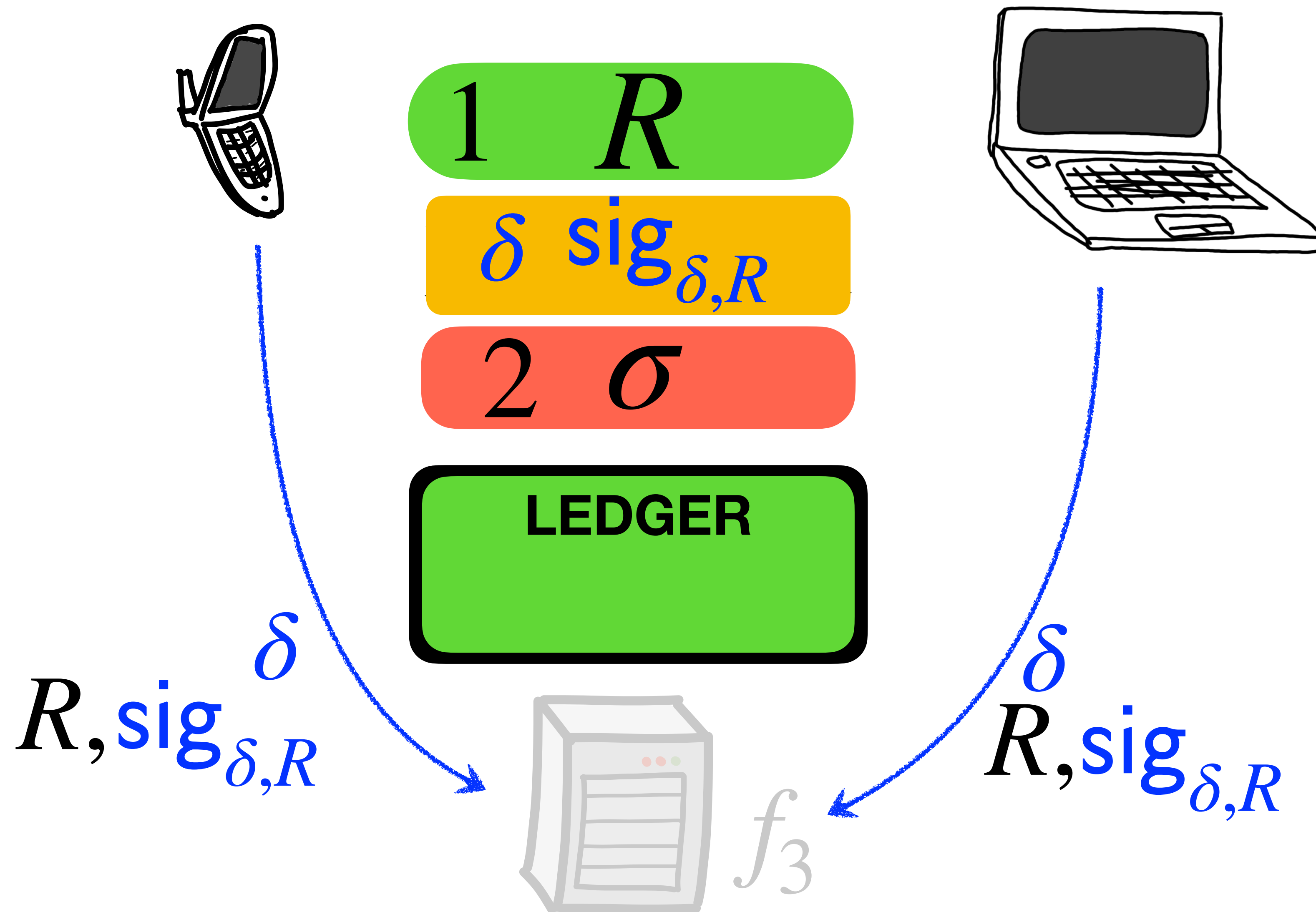
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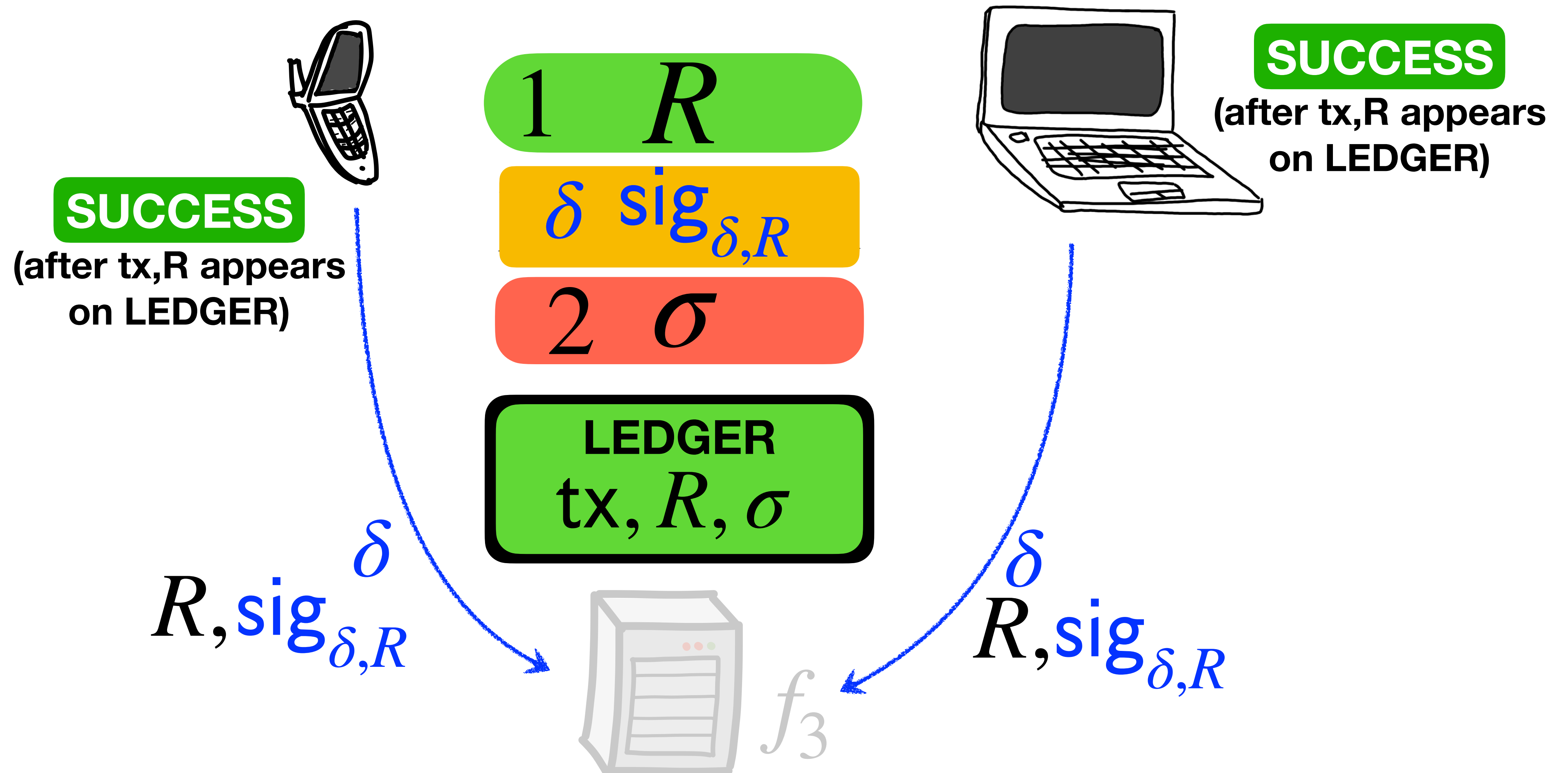
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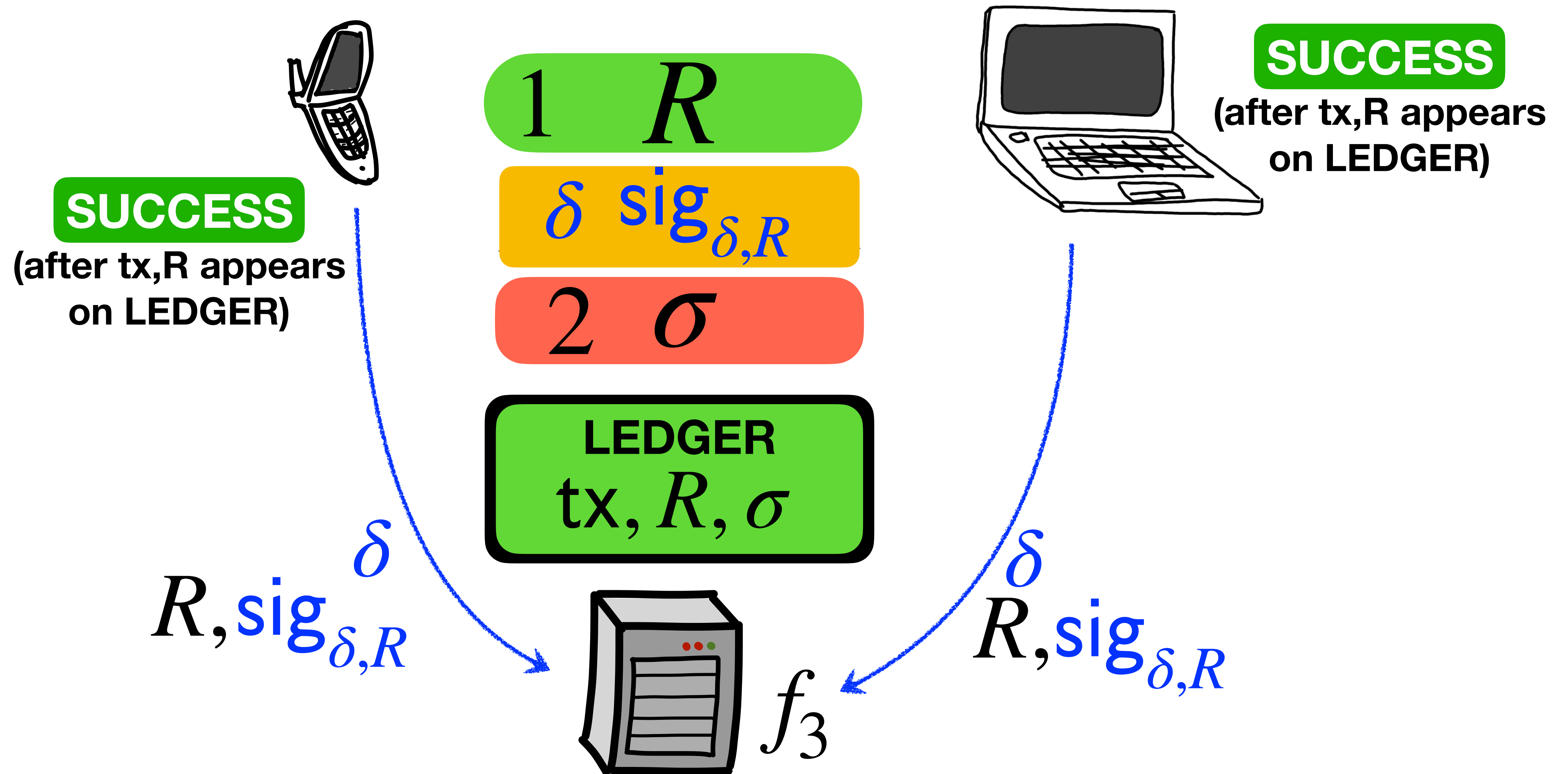
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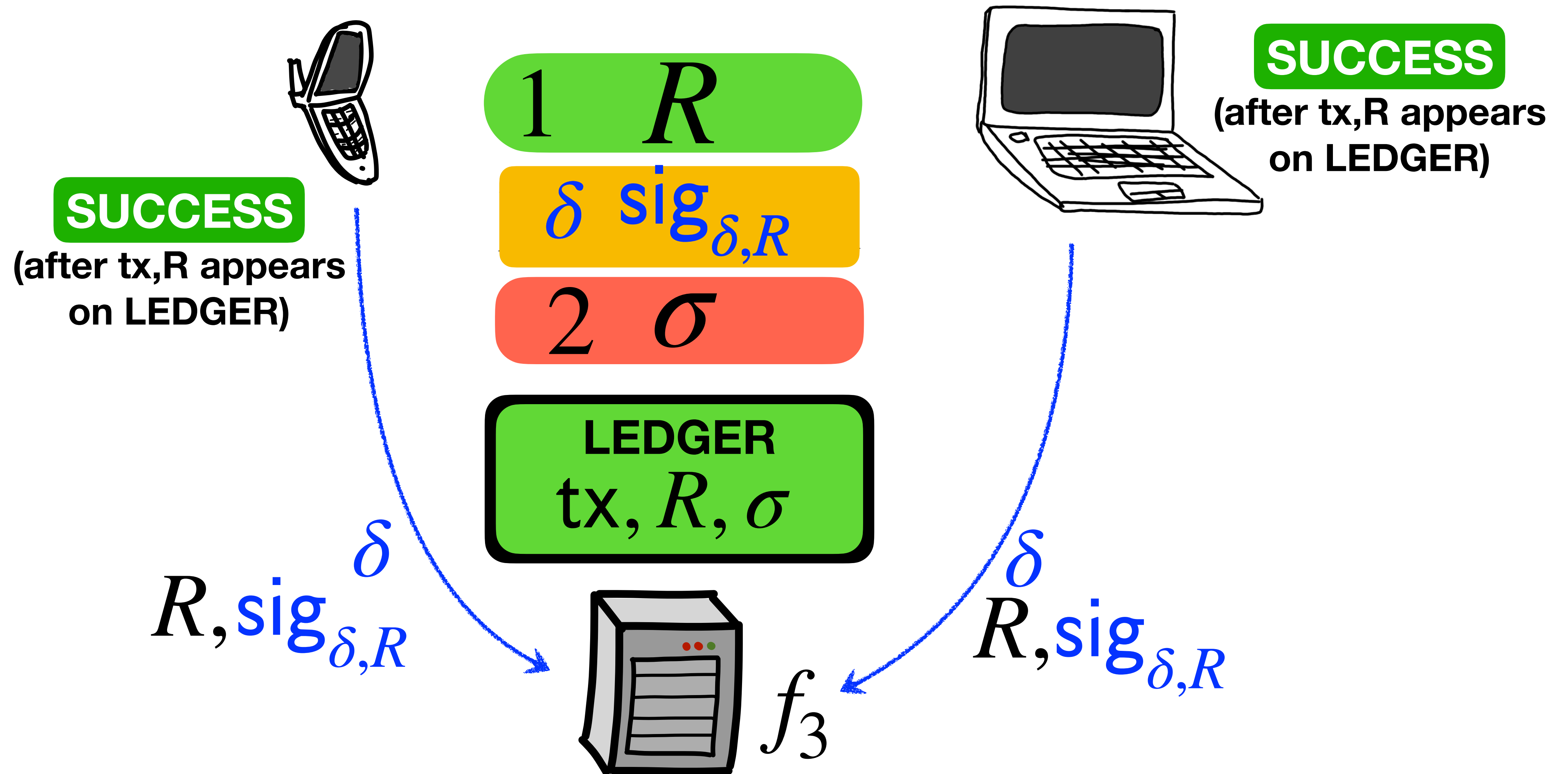
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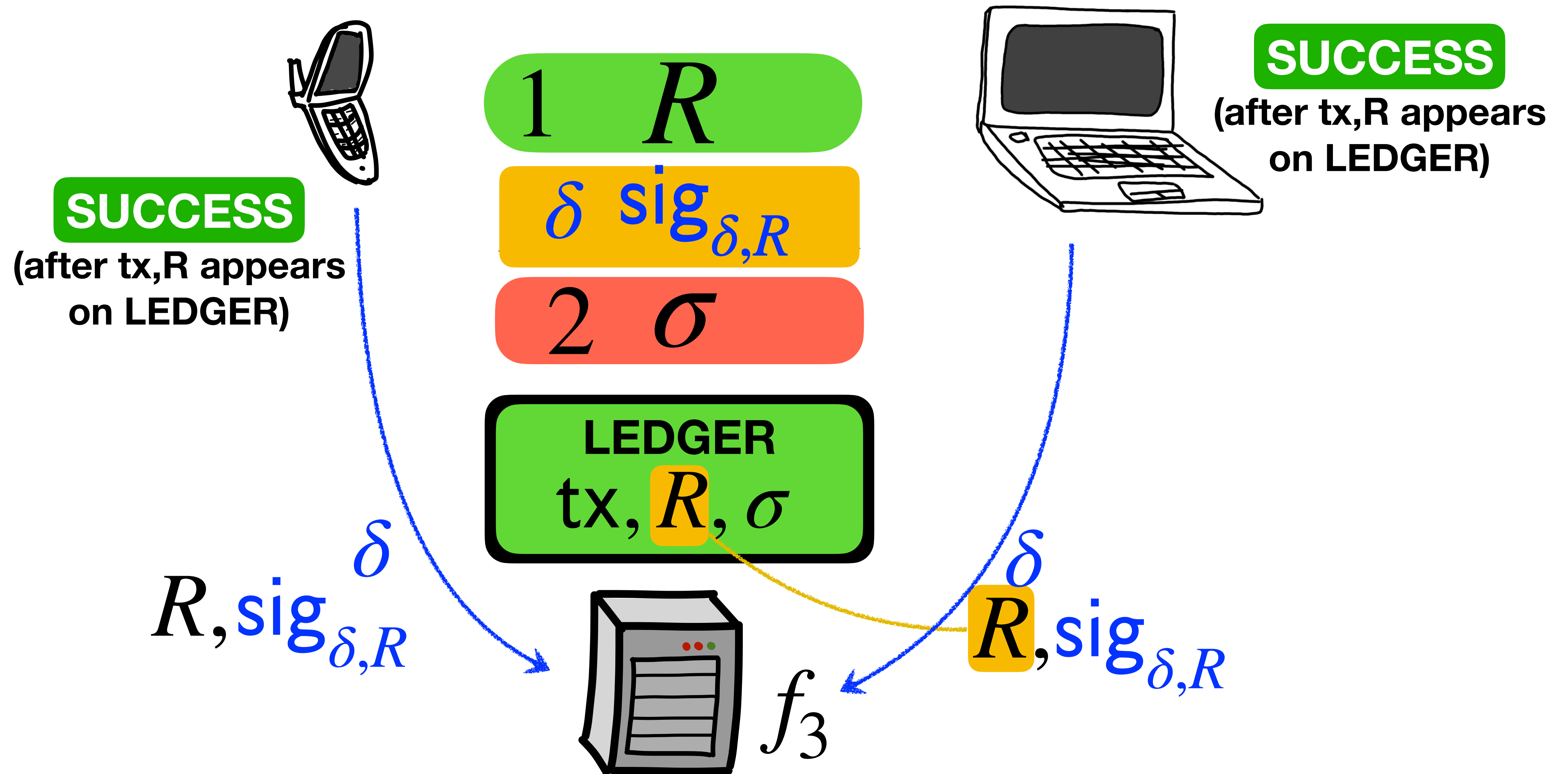
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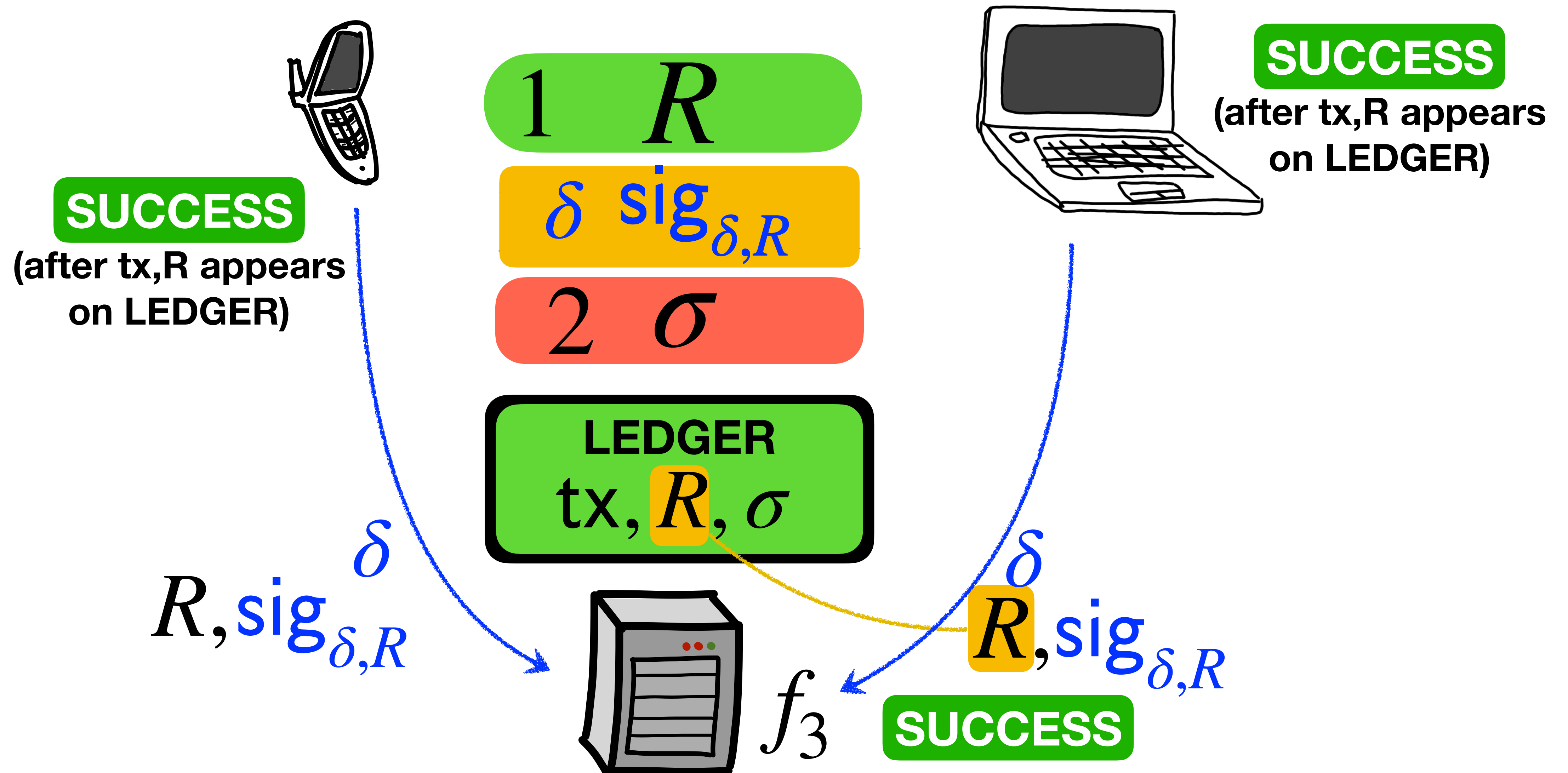
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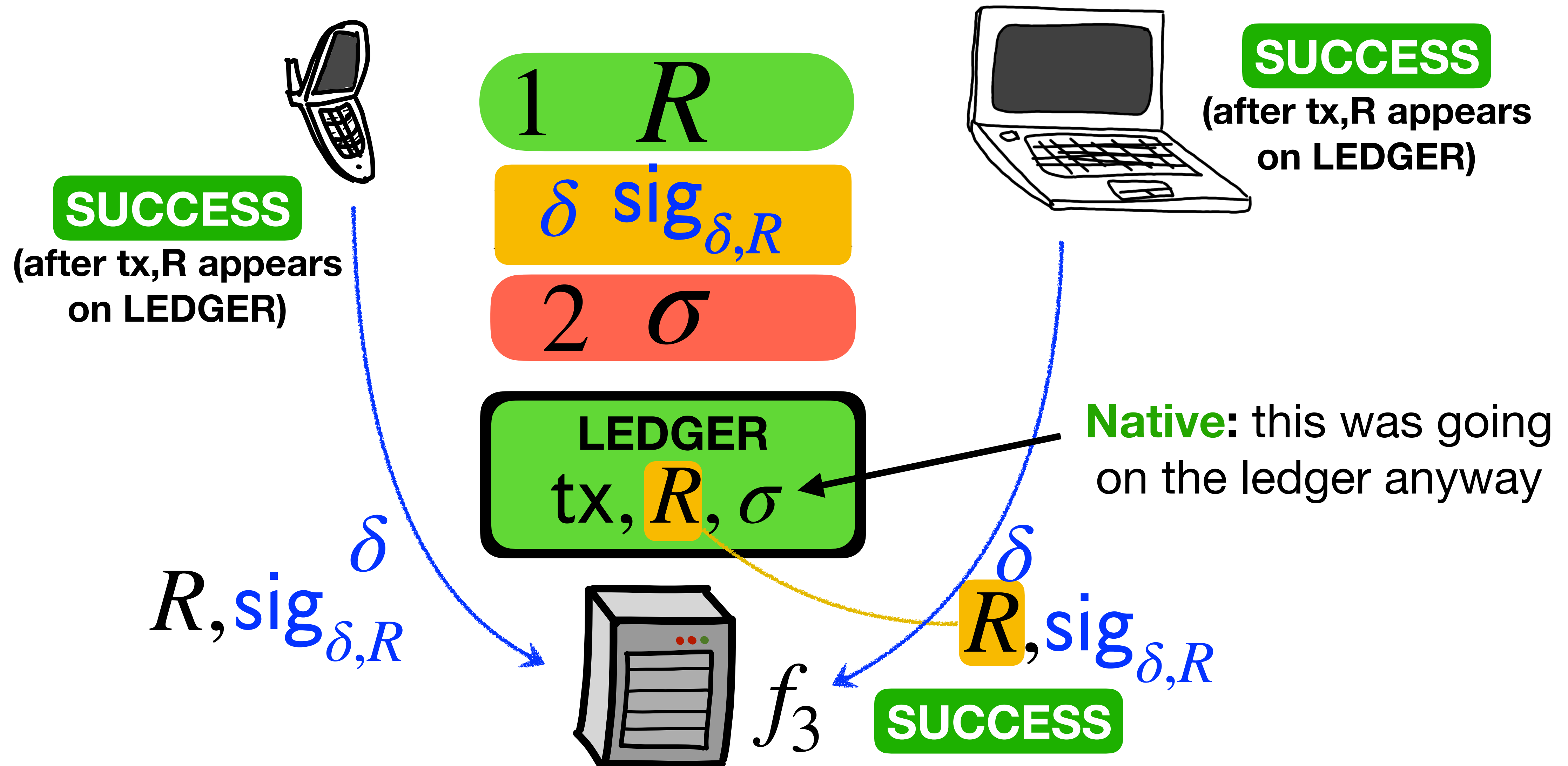
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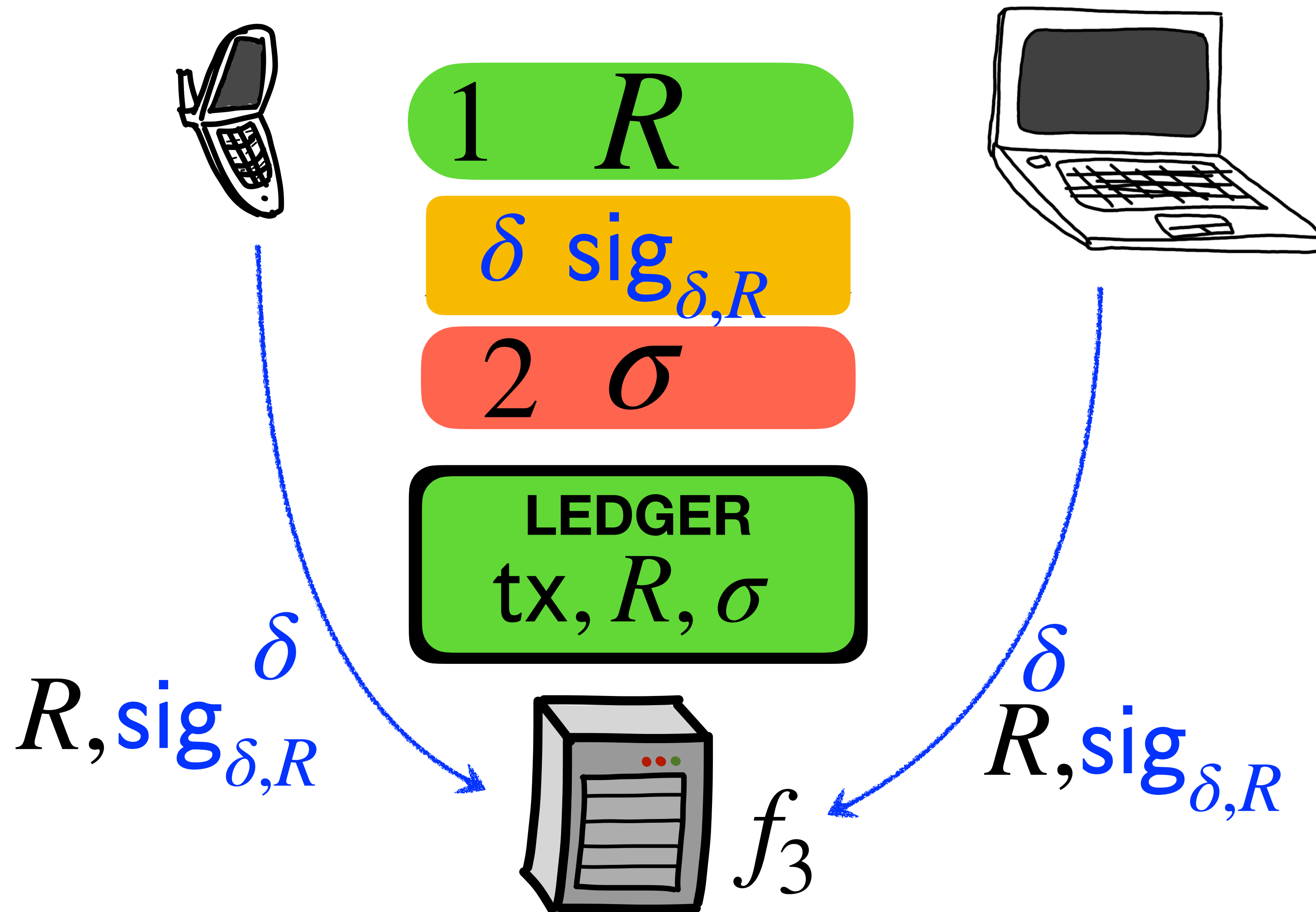
# Interleaved Threshold Signing



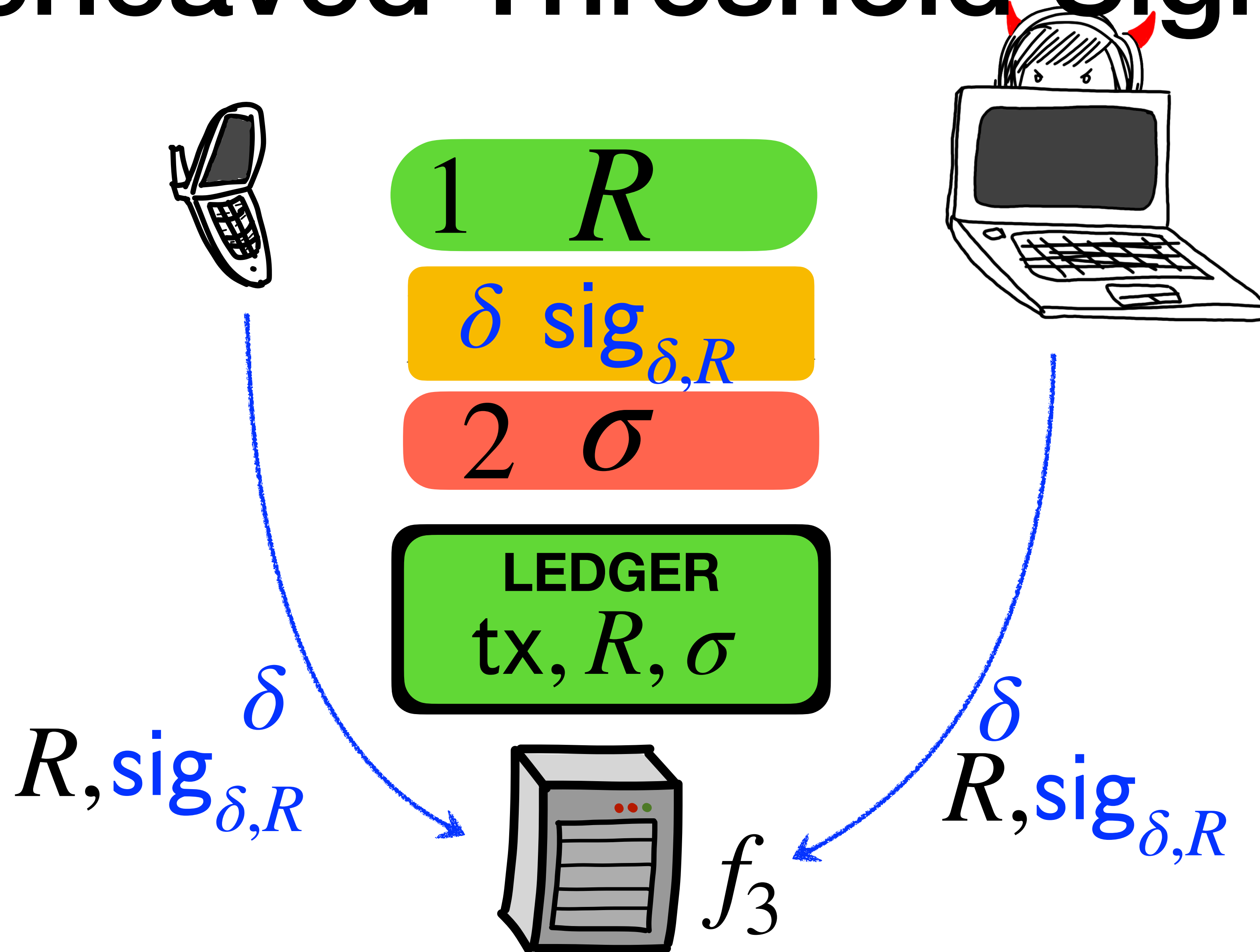
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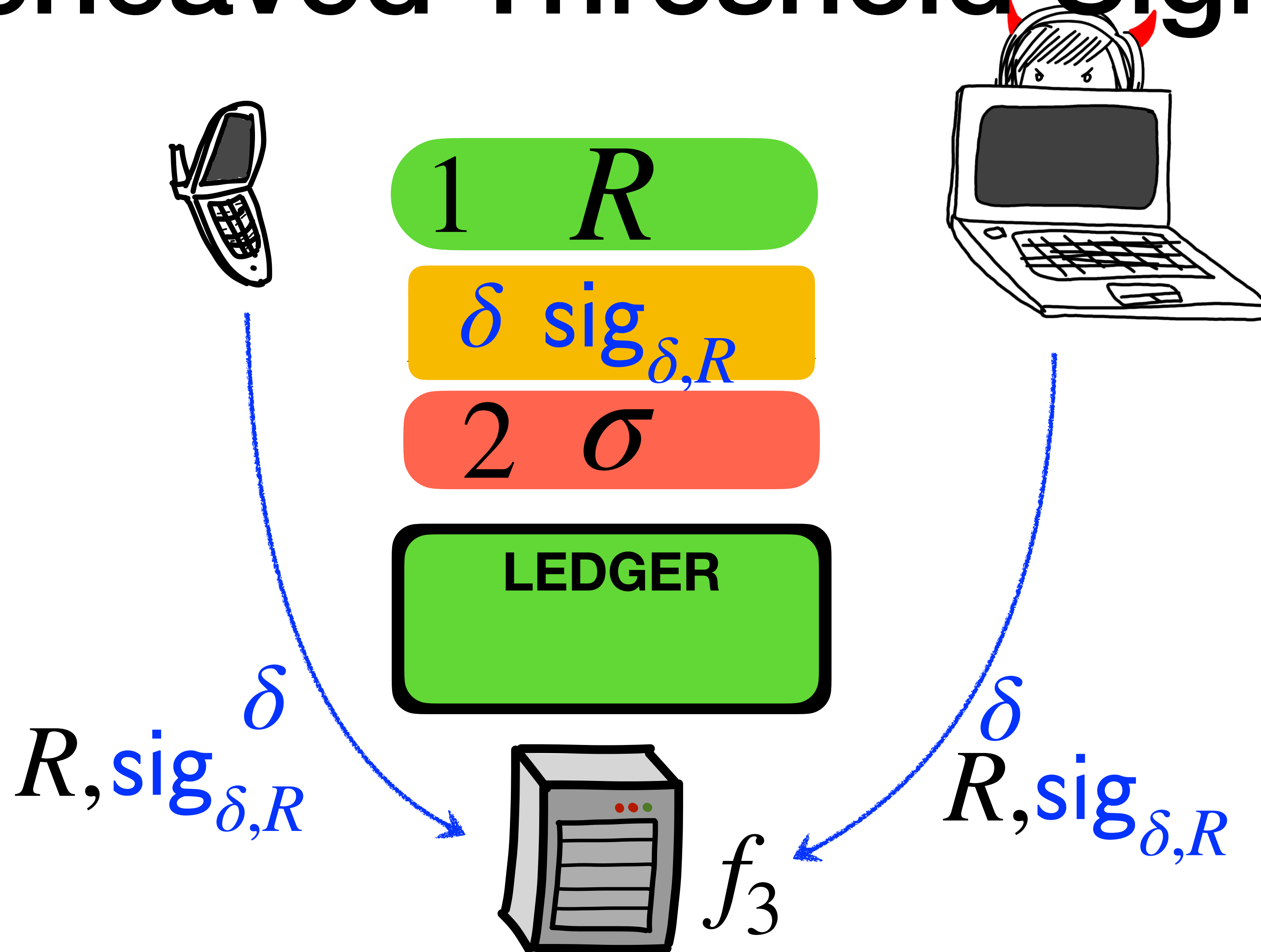
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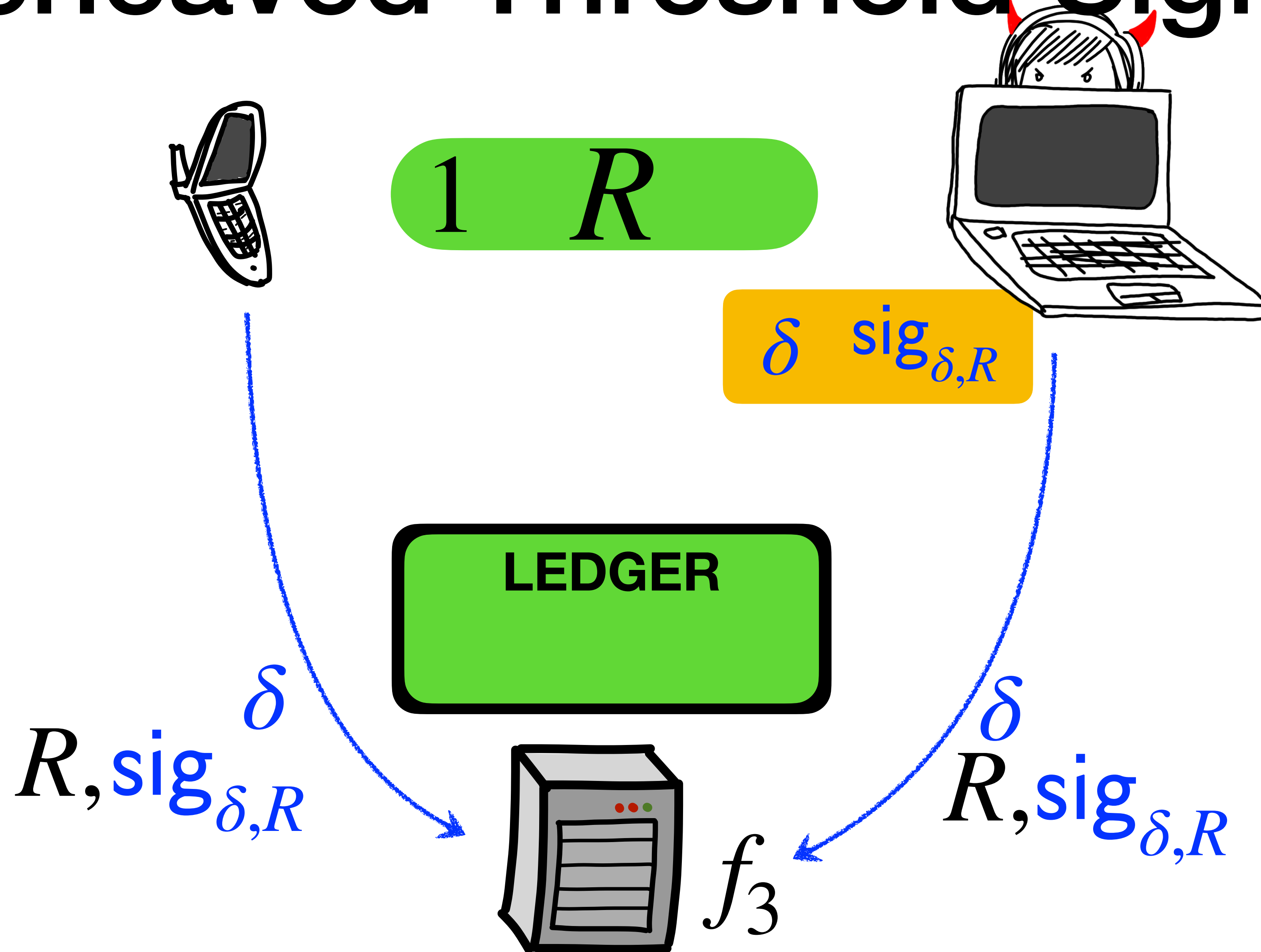
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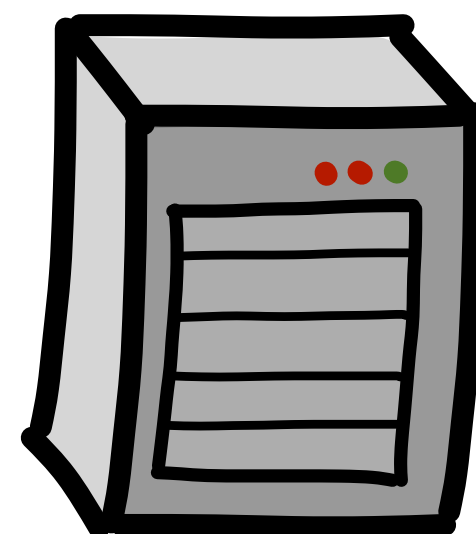


1  $R$



$\delta$   $\text{sig}_{\delta,R}$

LEDGER



$f_3$

$\delta$   
 $R, \text{sig}_{\delta,R}$

# Interleaved Threshold Signing



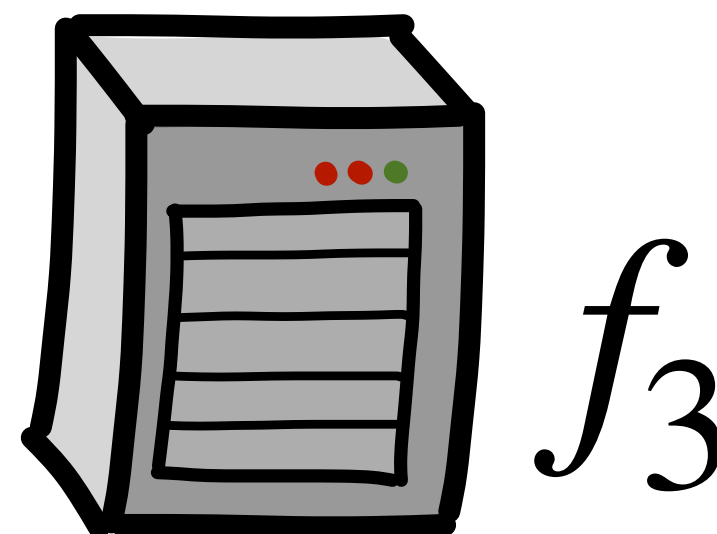
**LEDGER** will never  
receive valid  
signature under  $R$   
(Phase 2 never run)

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**LEDGER**



$f_3$

$\delta$   
 $R, \text{sig}_{\delta,R}$

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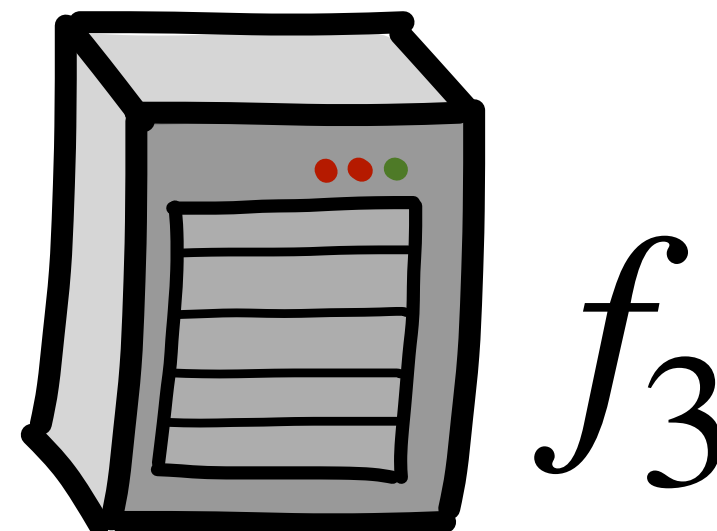


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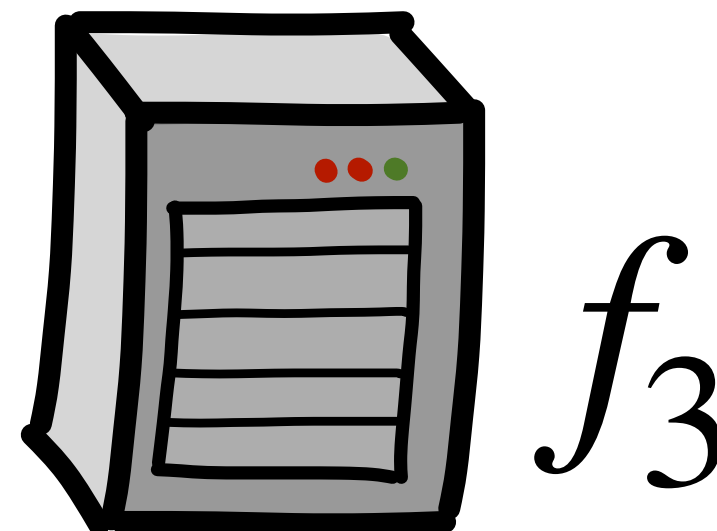
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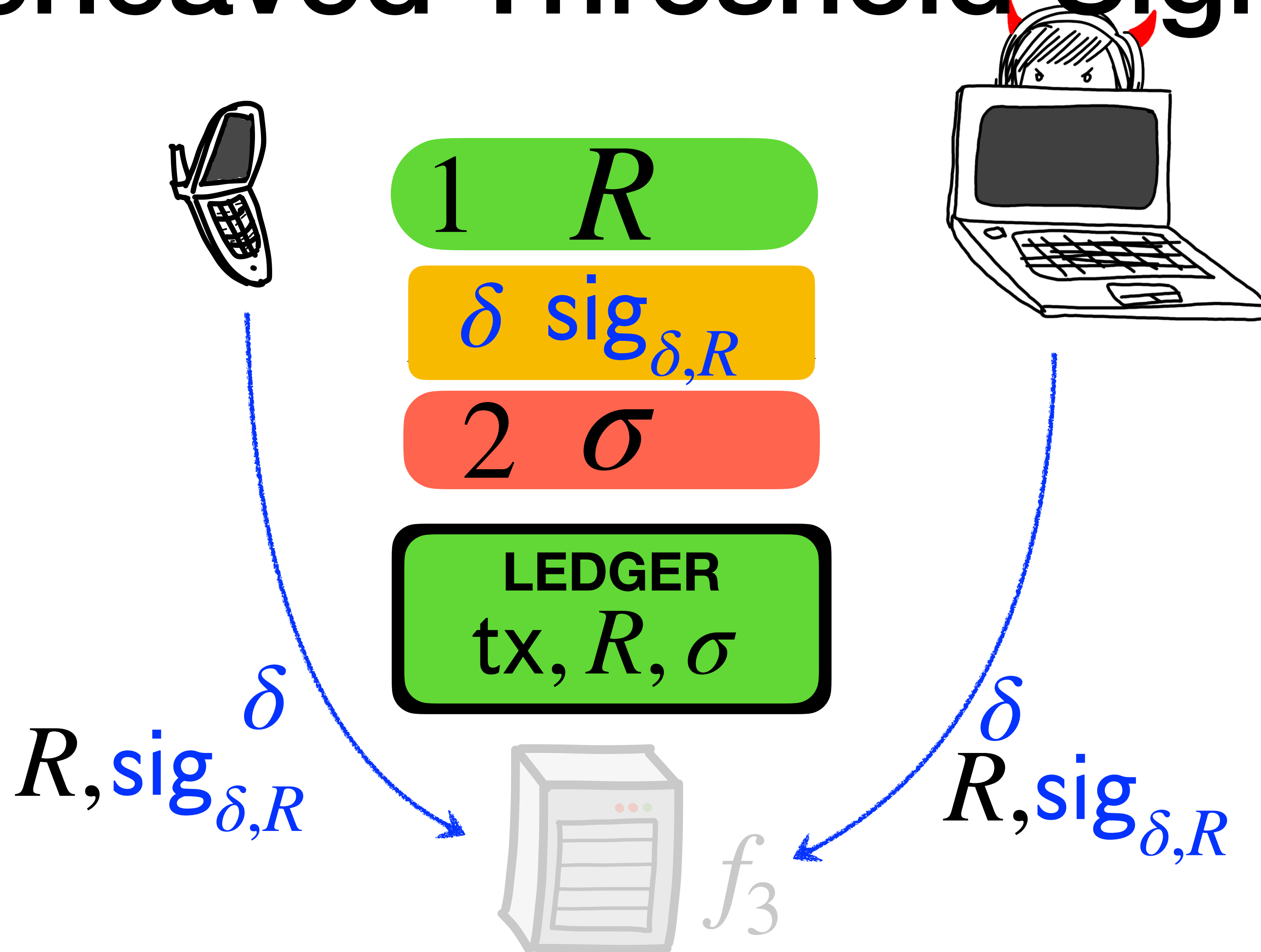
**Useless**

$\delta$   
 $R, \text{sig}_{\delta,R}$

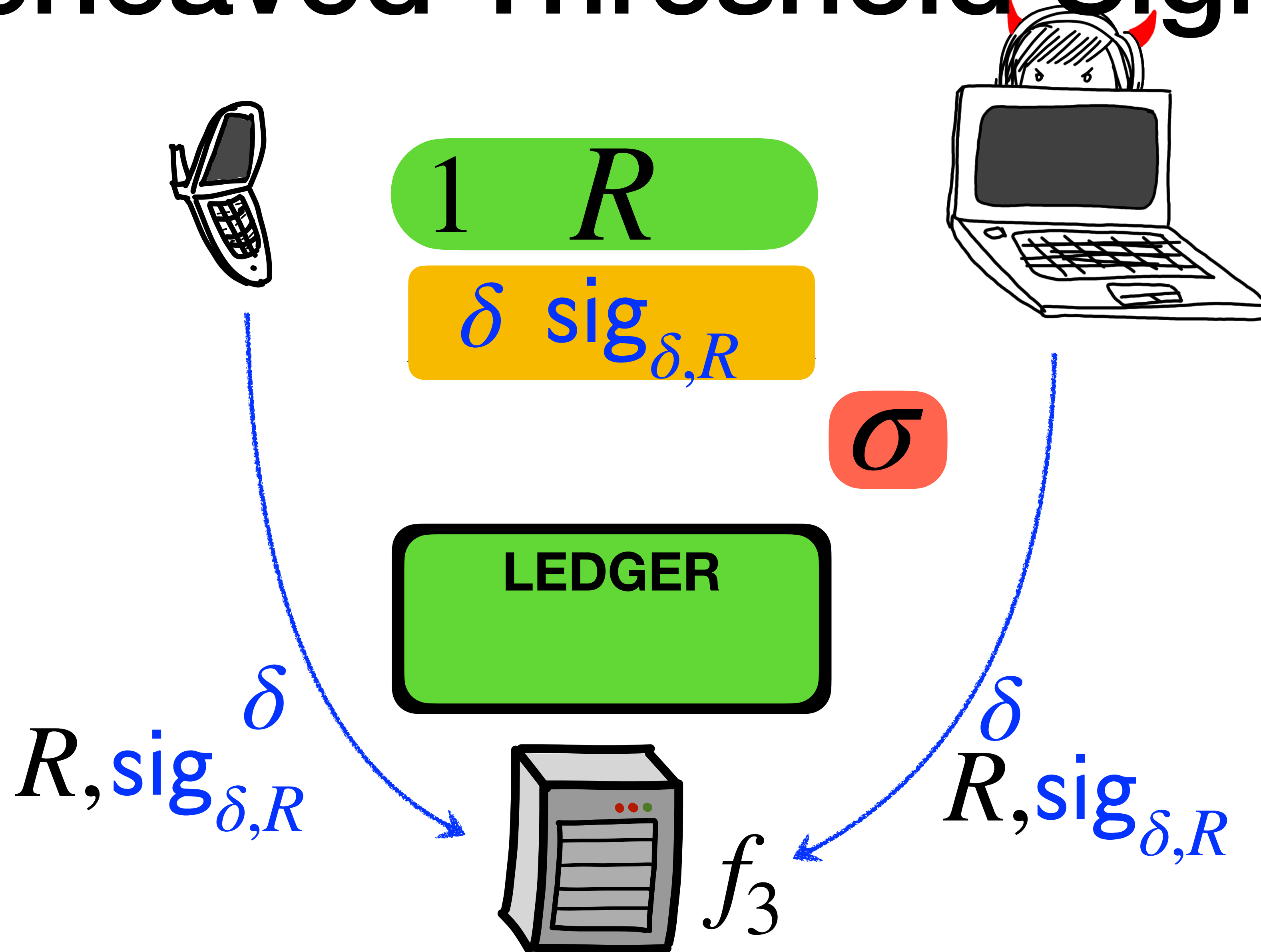


$f_3$

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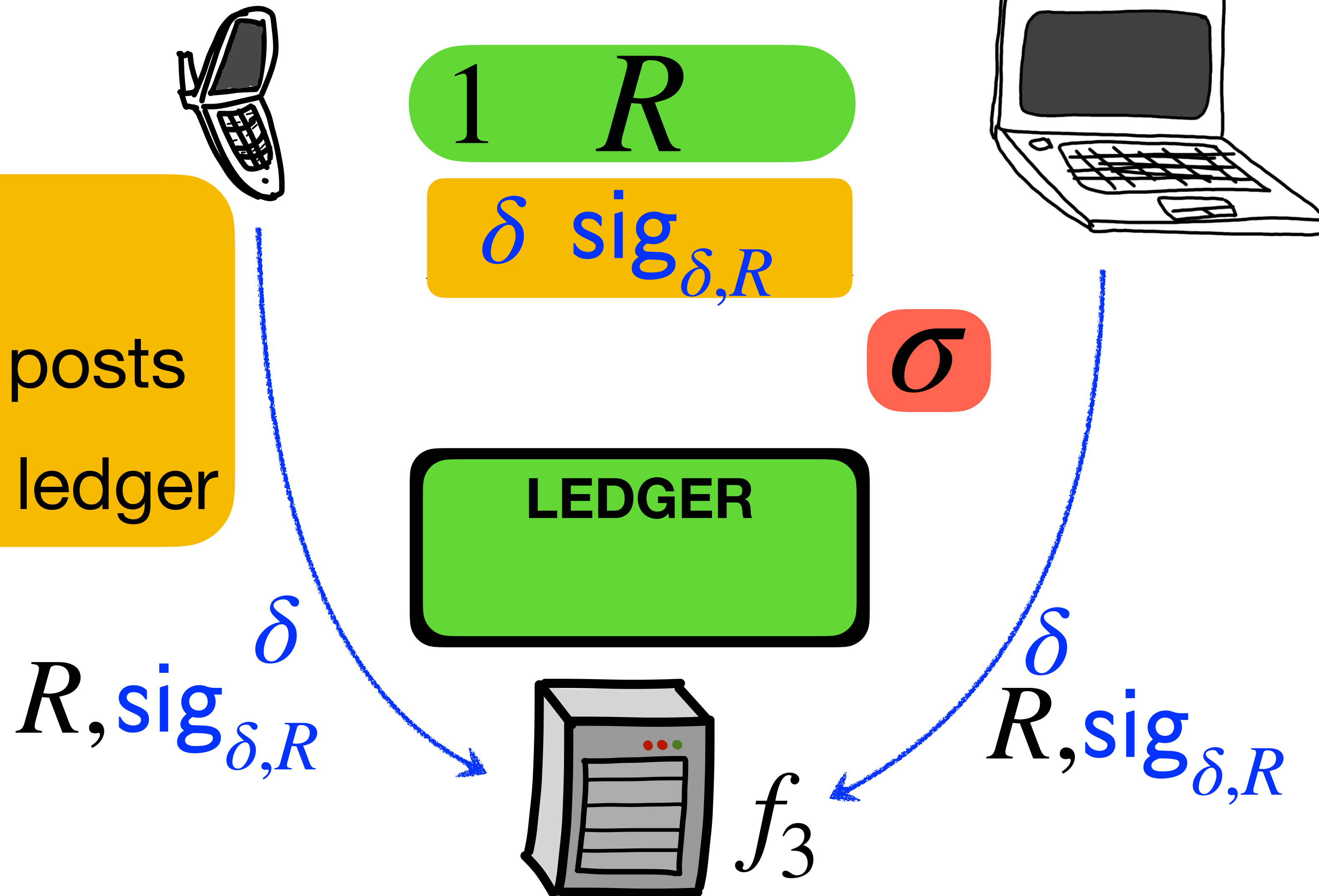
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## Case 1:

 never posts  
 $\text{tx}, R, \sigma$  to ledger



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 never posts  
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$R, \text{sig}_{\delta, R}^{\delta}$

Never used

1  $R$

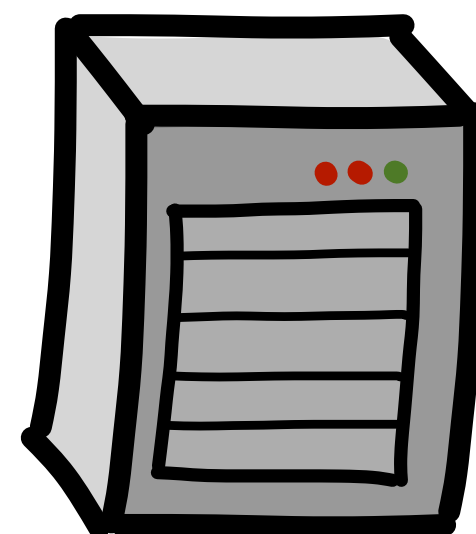
$\delta \text{ sig}_{\delta, R}$

$\sigma$

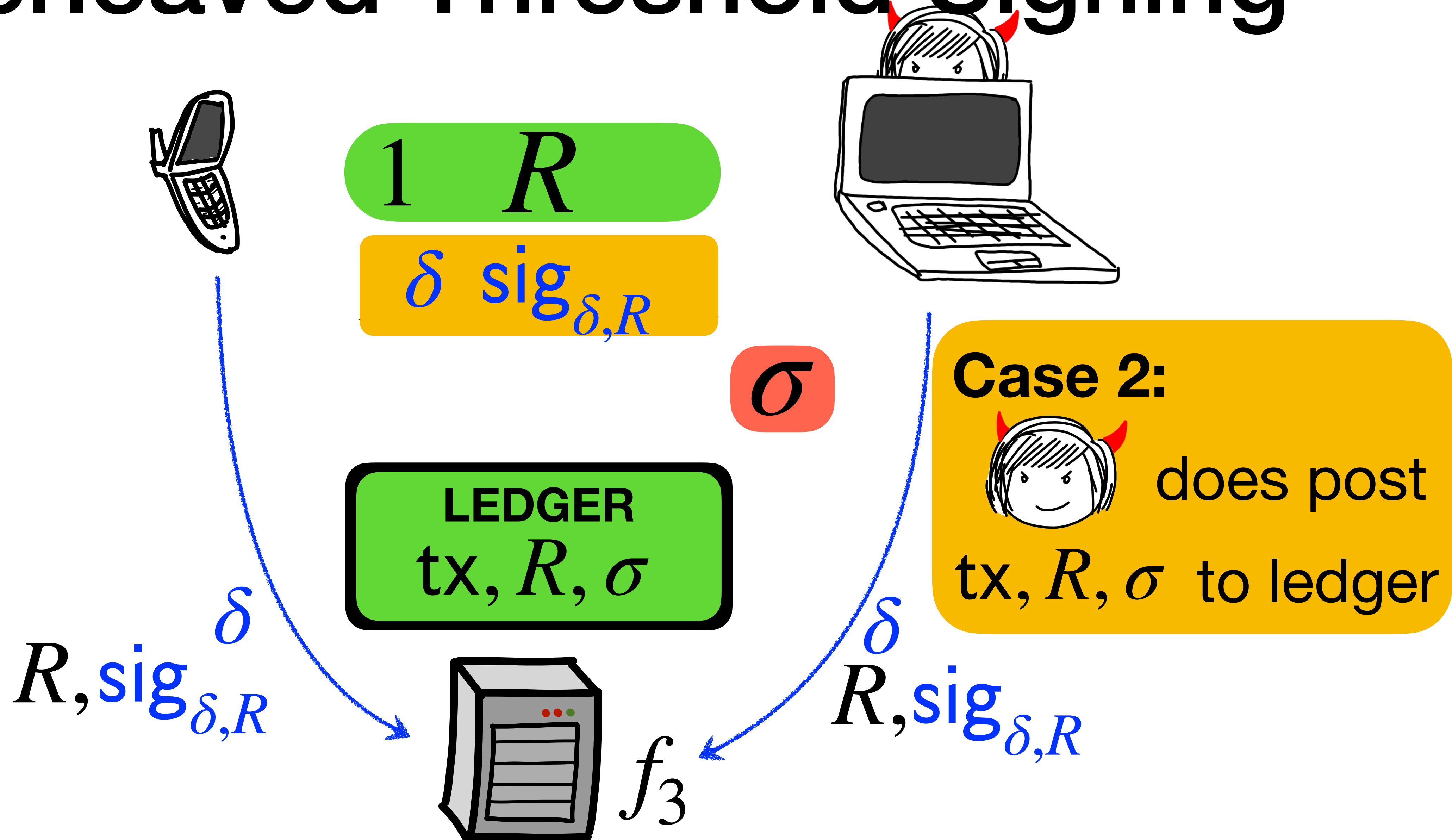
LEDGER

$\delta R, \text{sig}_{\delta, R}^{\delta}$

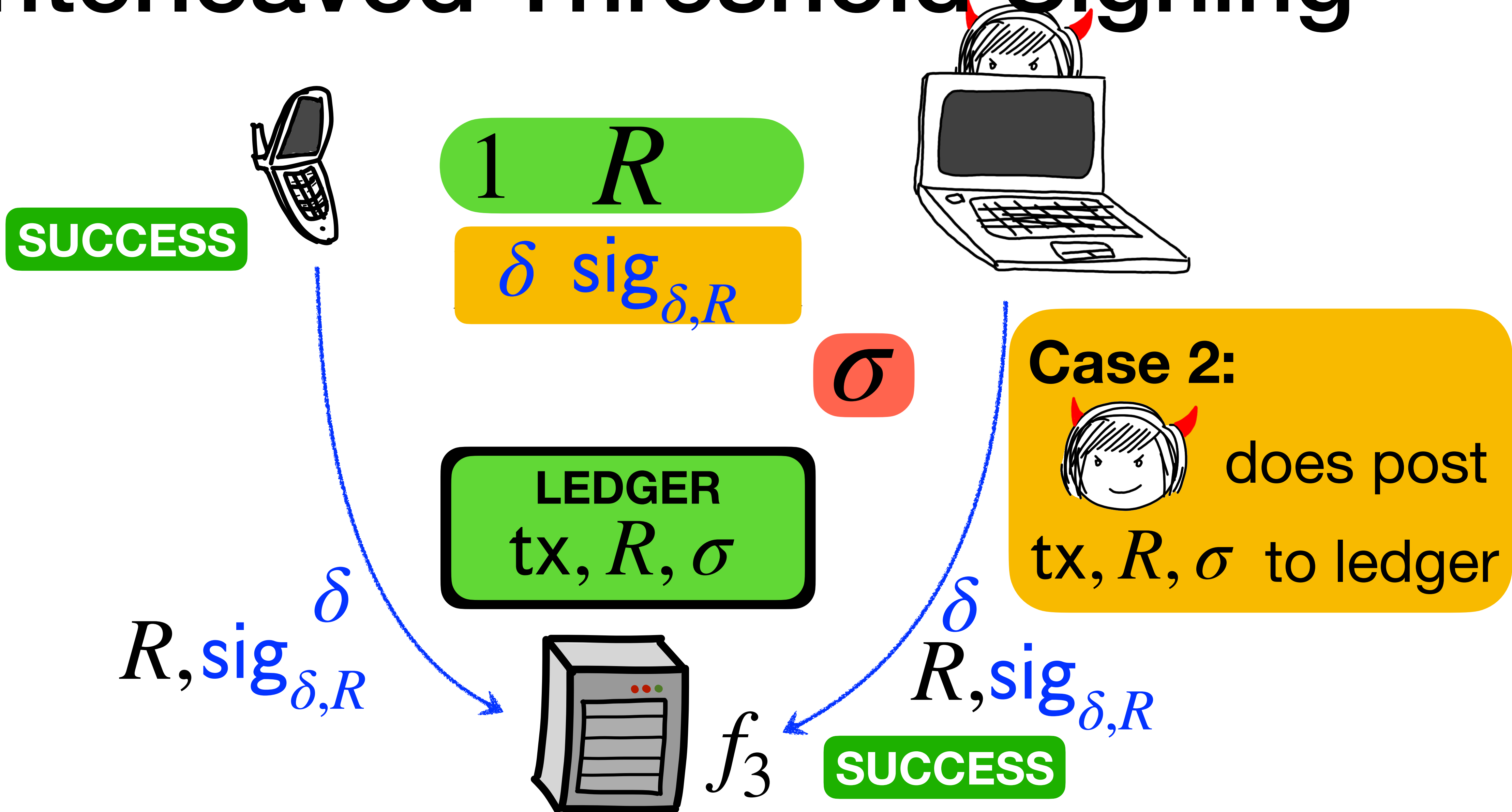
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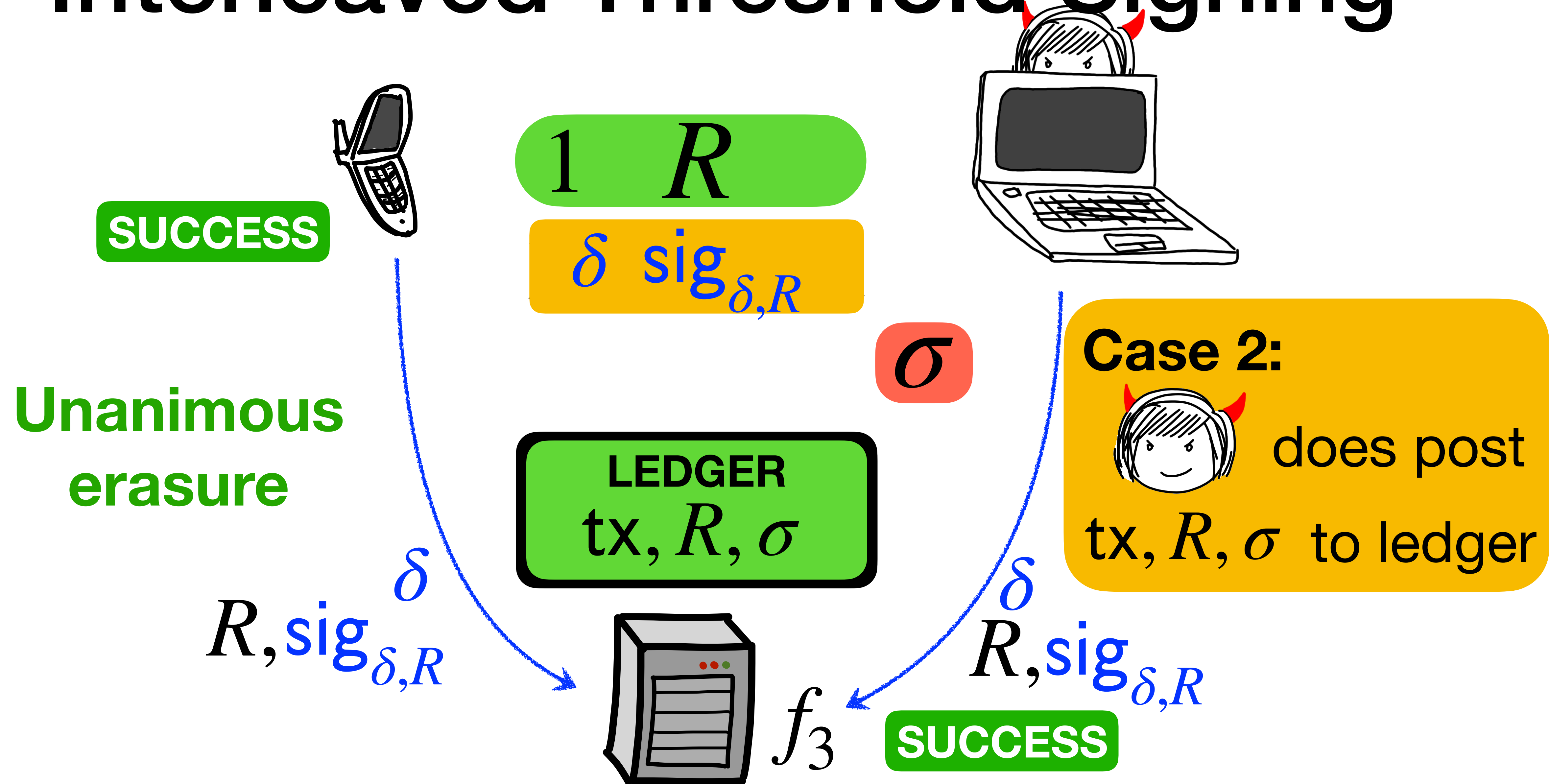
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- **Communication: 200 bytes, no extra rounds**

# This Work

- Correct definition is subtle
  - Guaranteed progress is impossible
  - We formulate **unanimous erasure**
- $(2,n)$  setting: Efficient new protocol **native** to wallets
  - New interleaved threshold sig technique
  - Offline parties can miss arbitrary number of epochs
  - Implementation shows practicality
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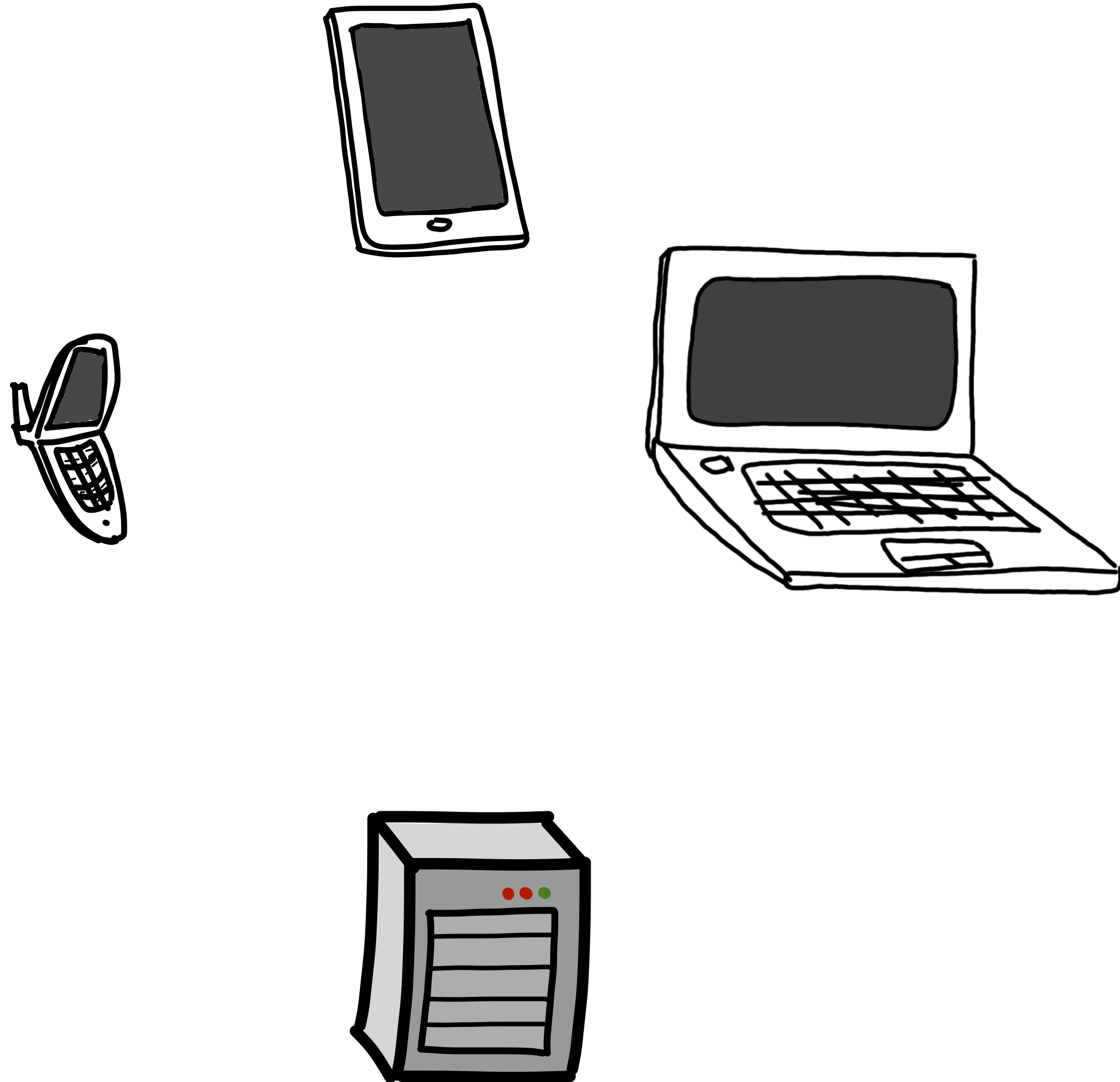
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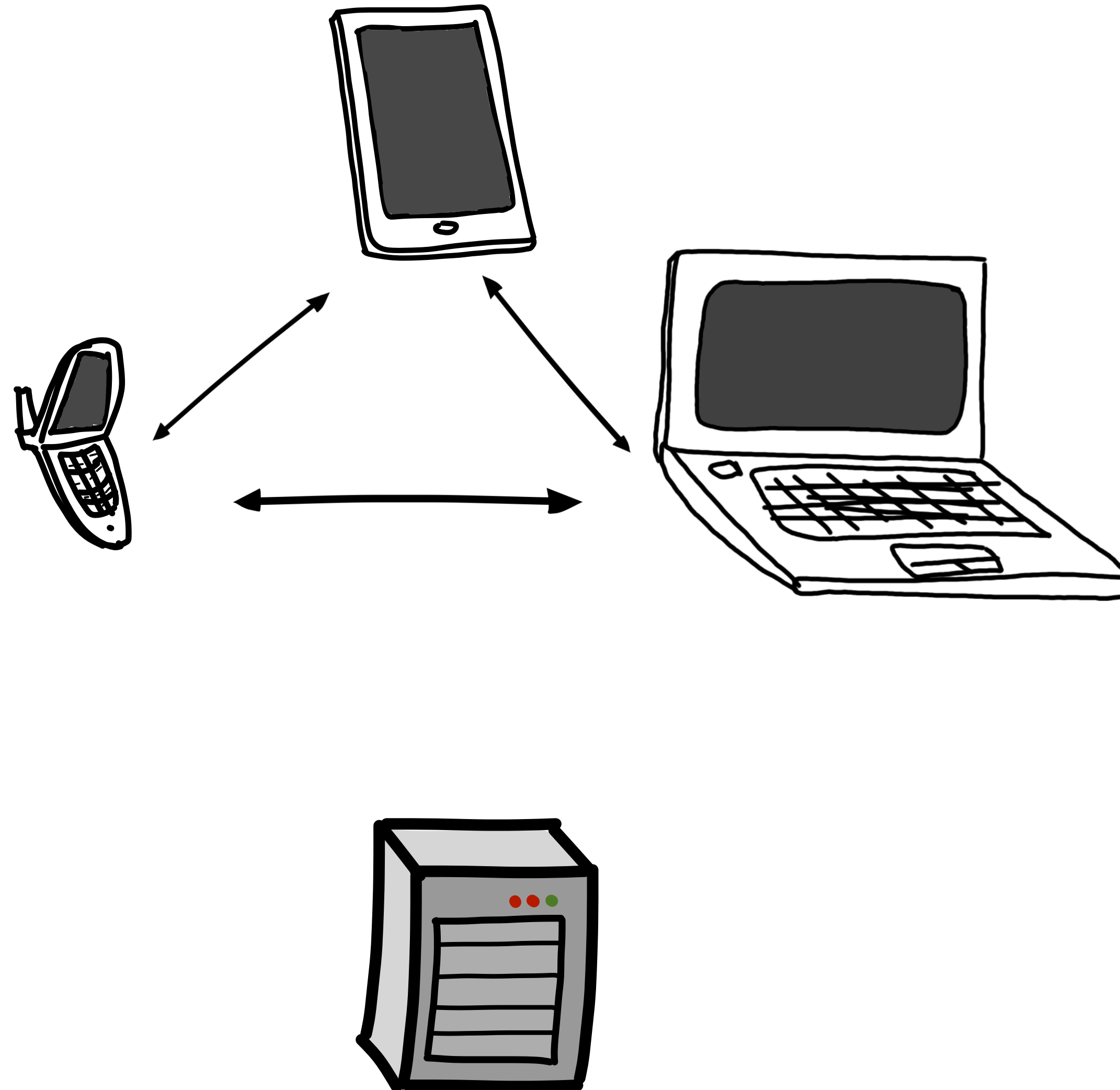
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- Intuition turns out to be wrong!

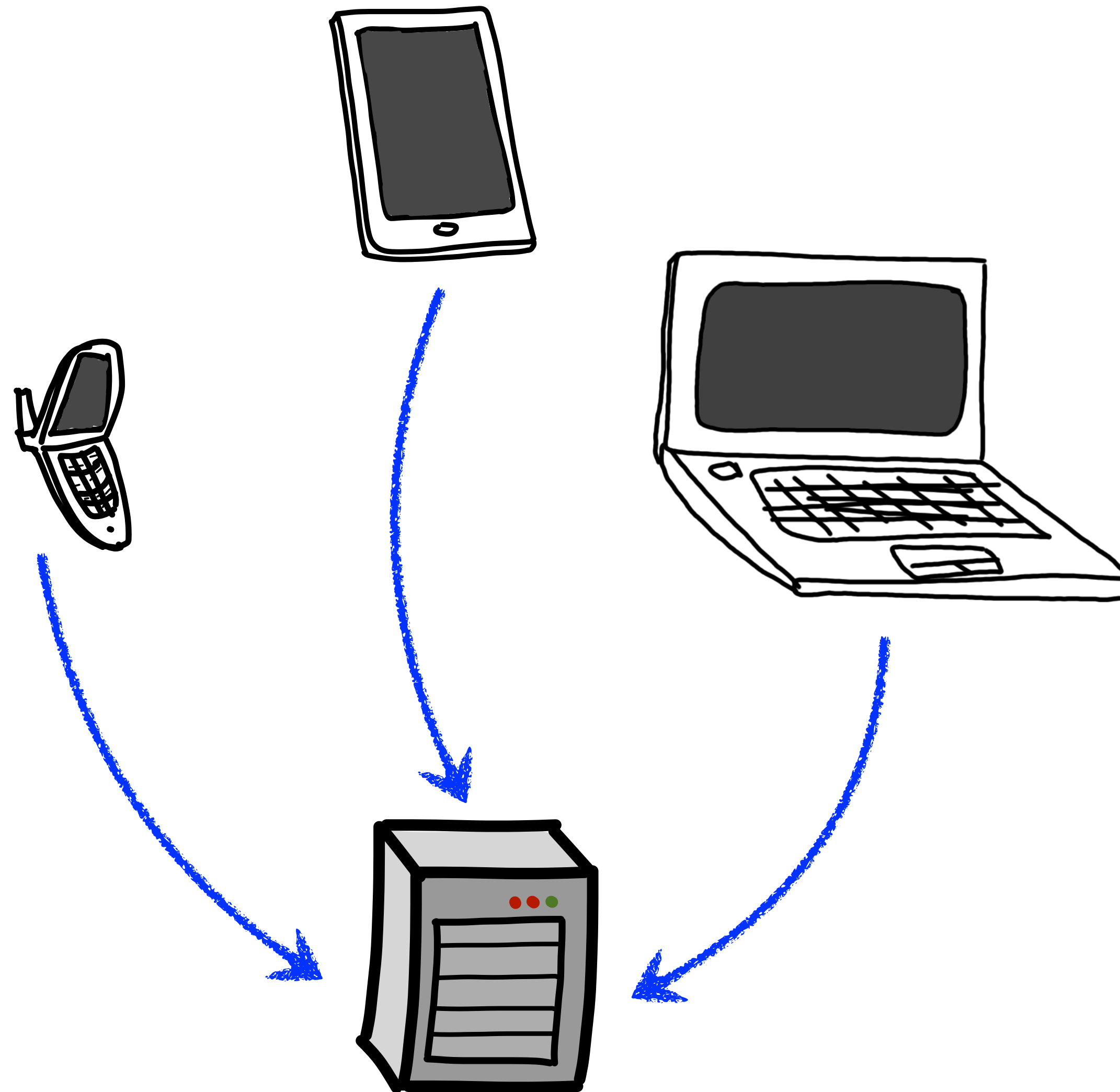
# Intuition: (3,4) case



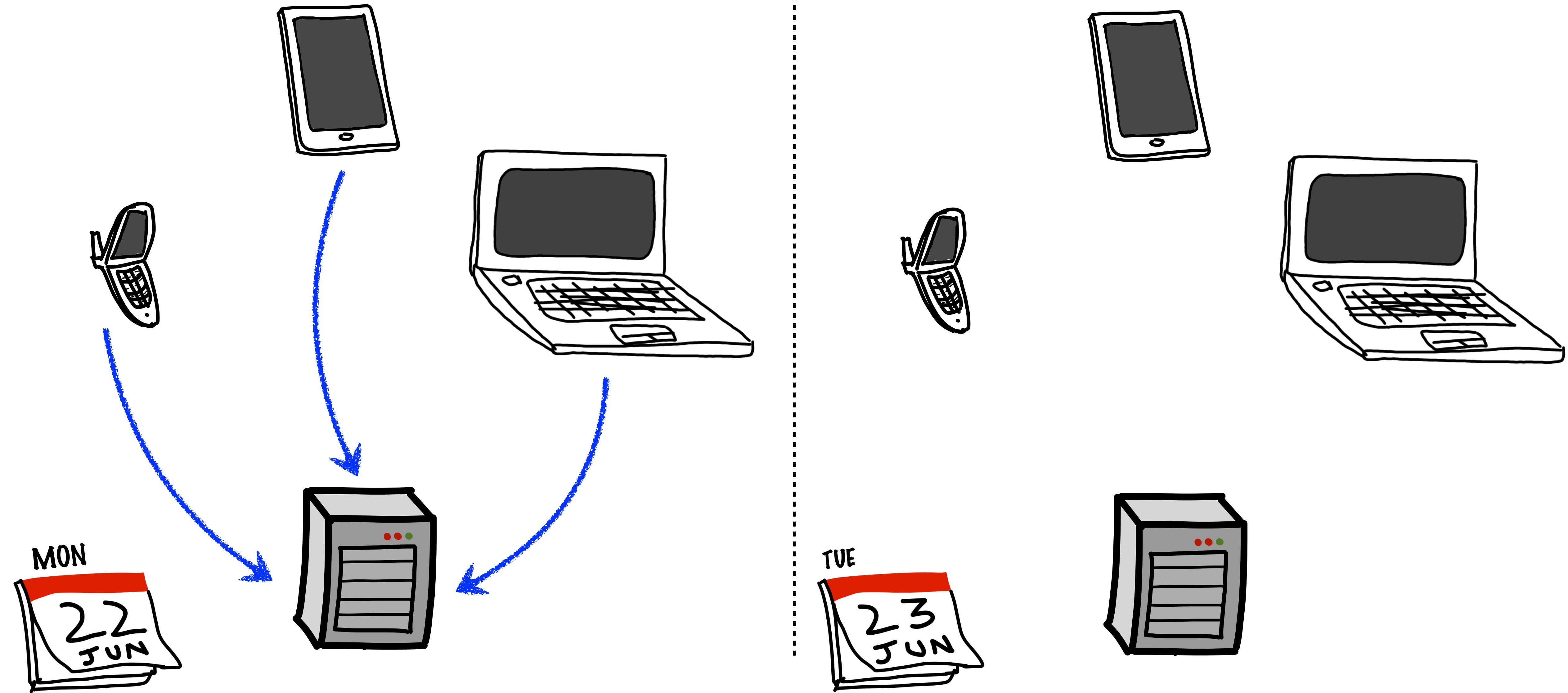
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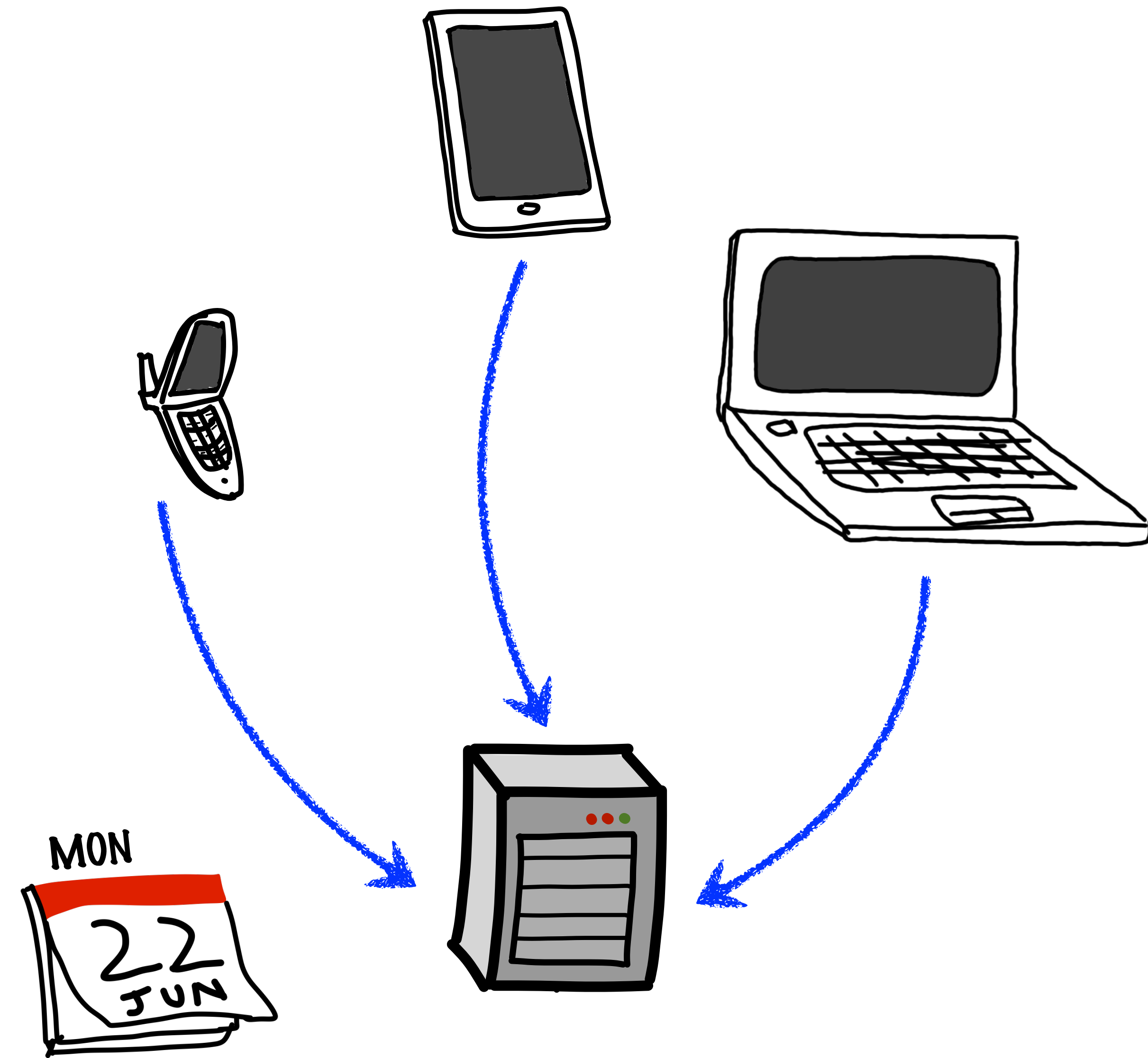
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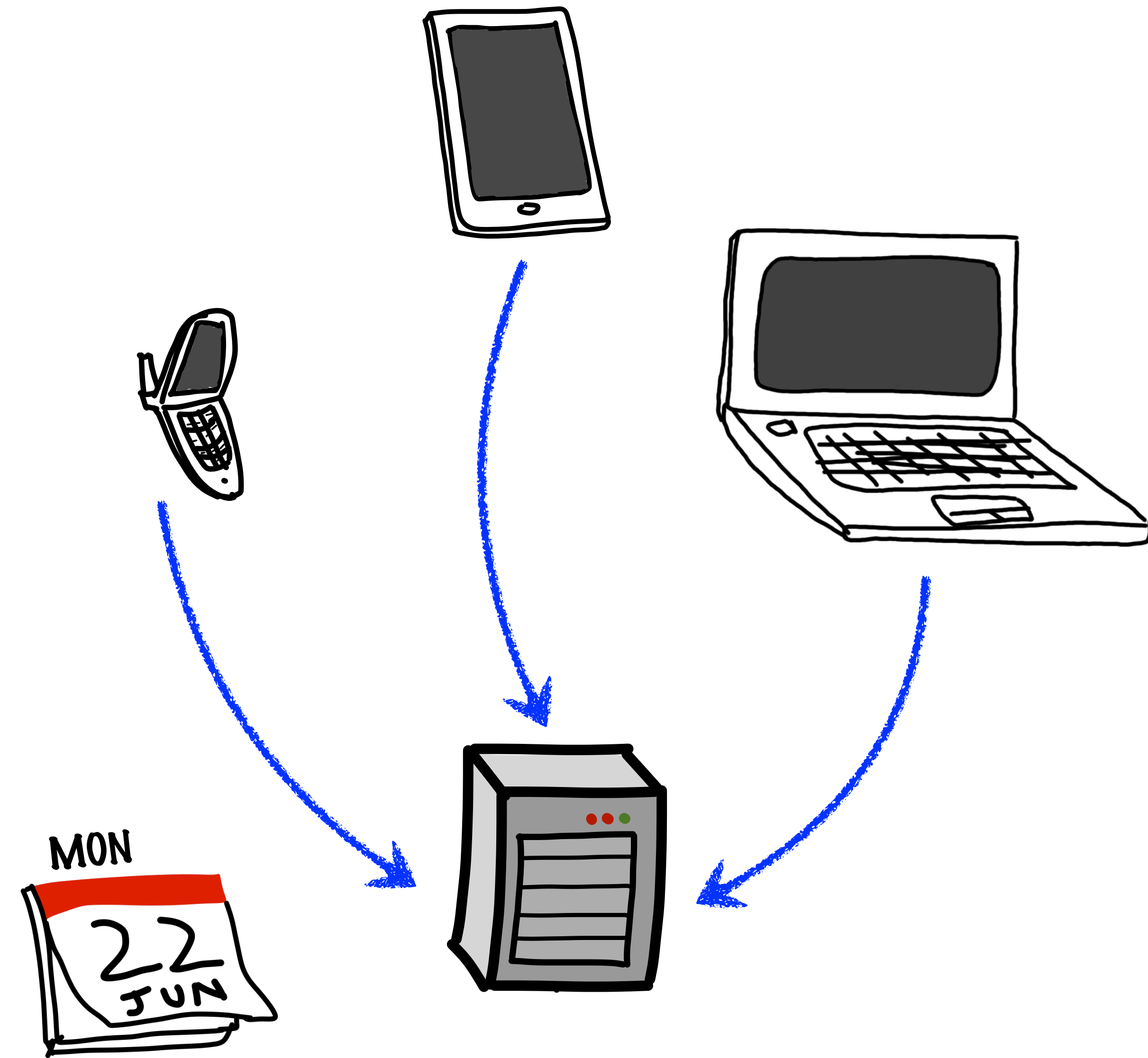
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secure against corruption  
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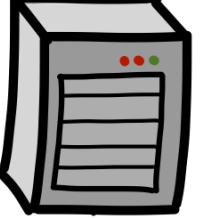


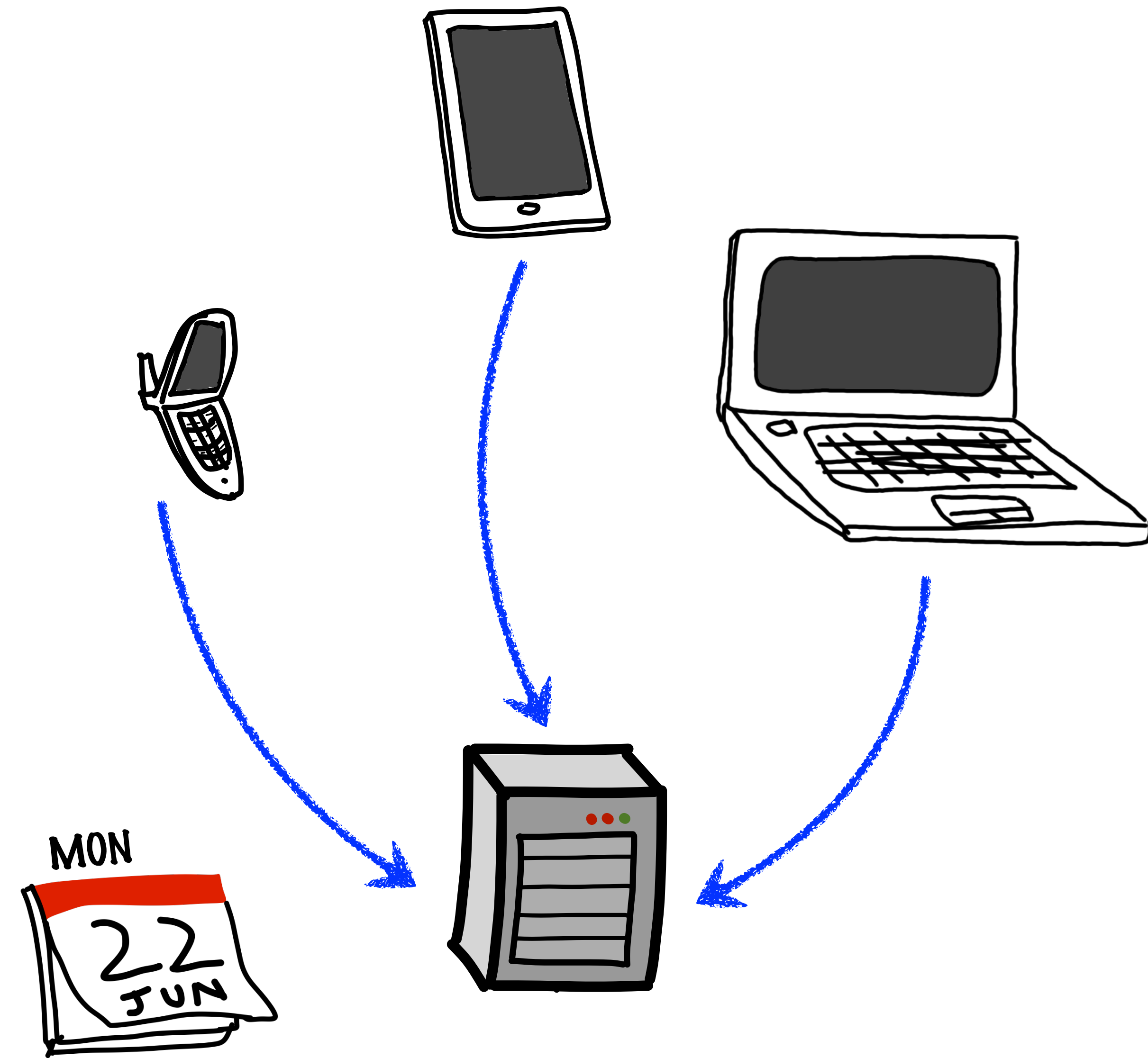
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View of  has enough info  
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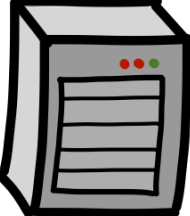


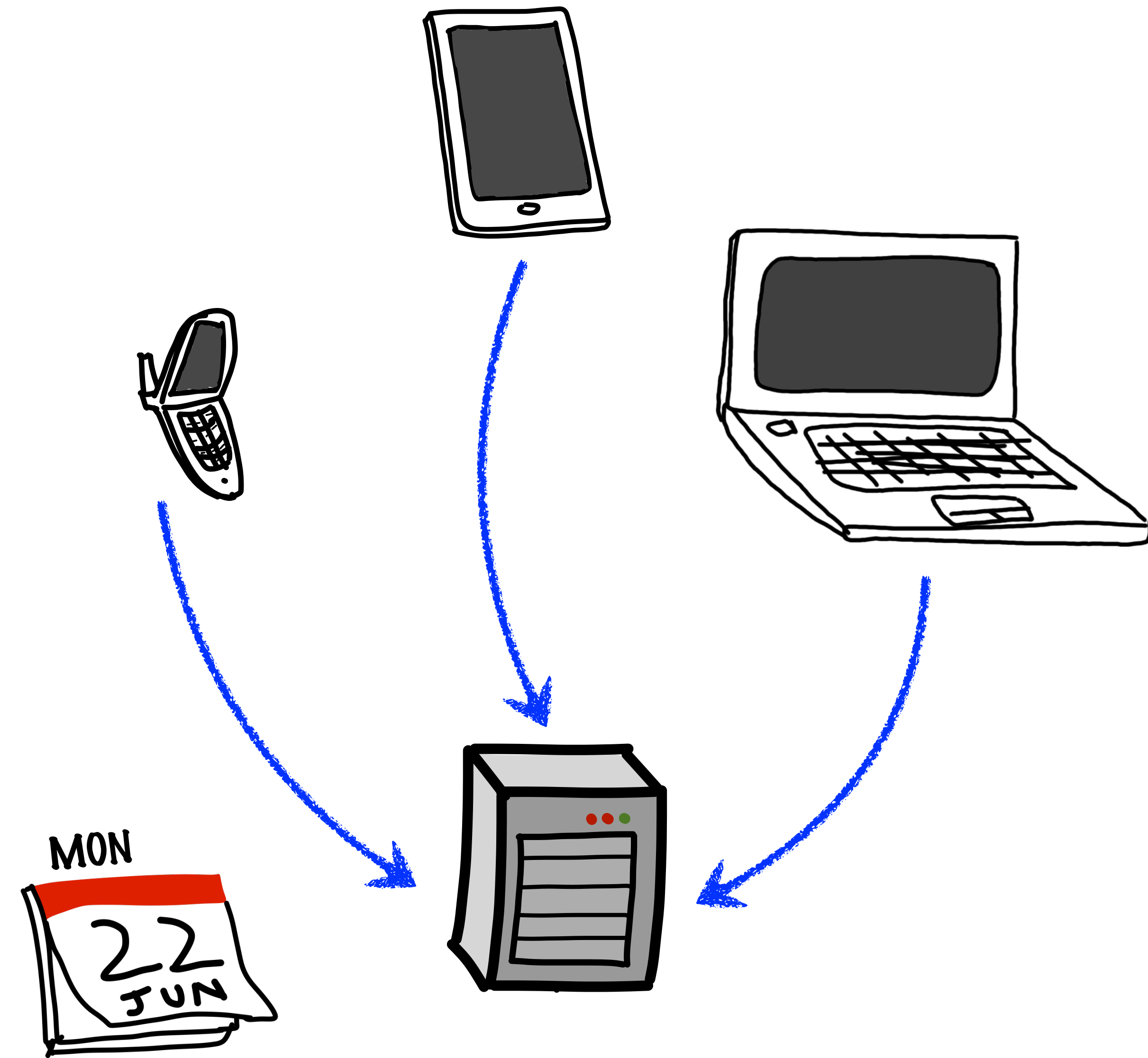
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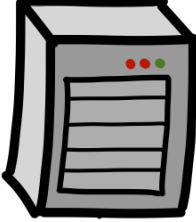


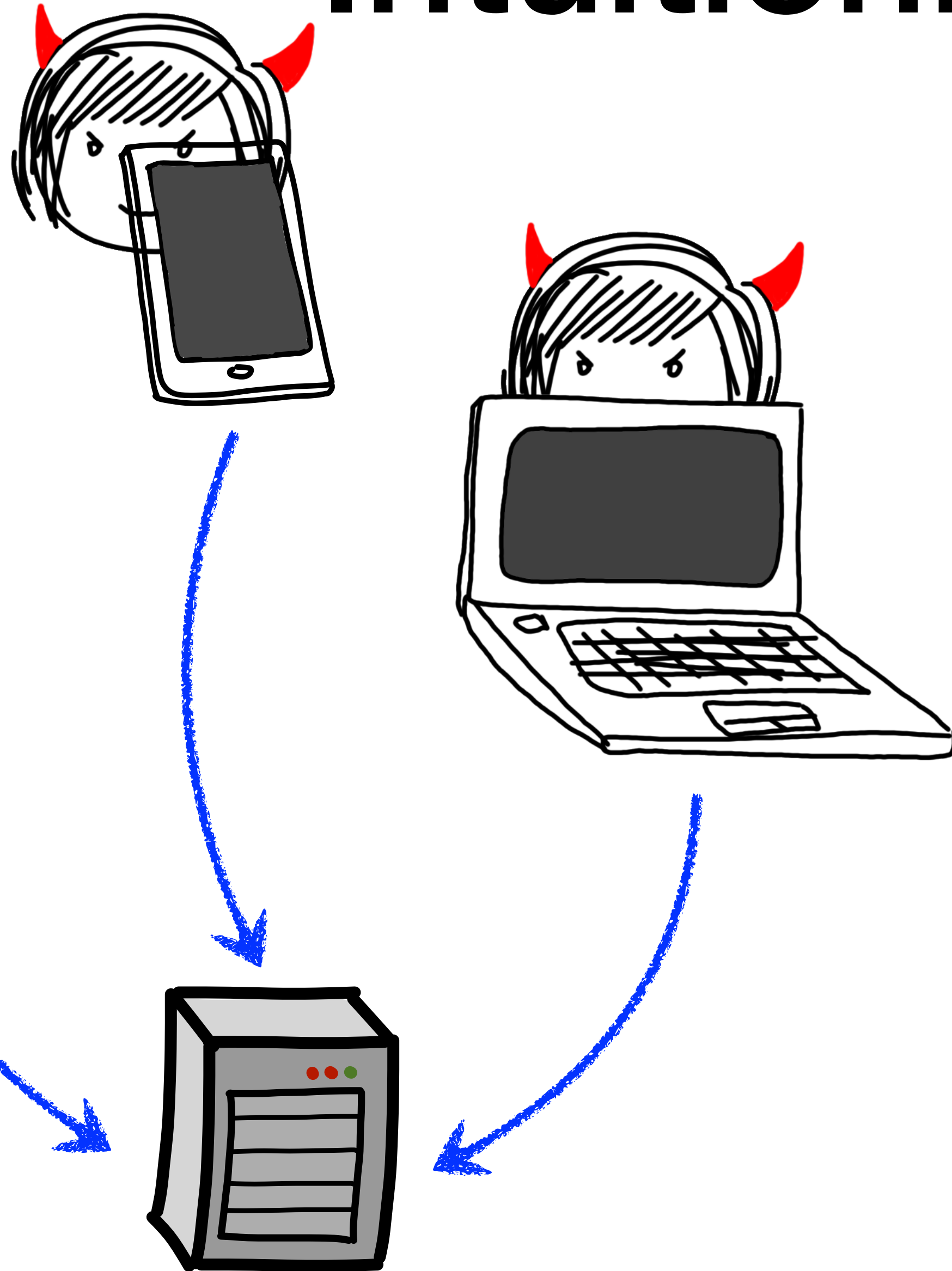
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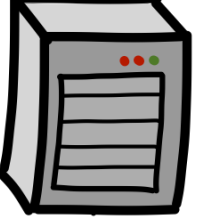
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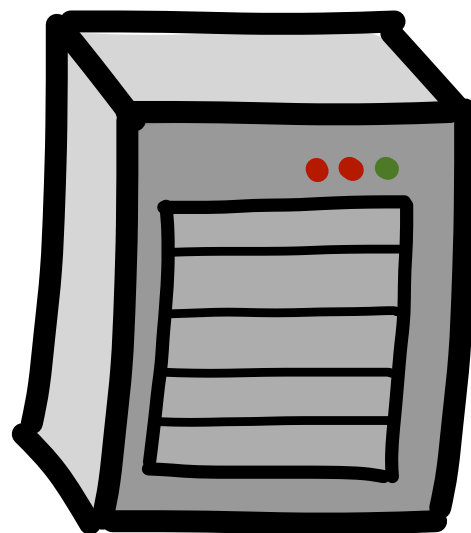
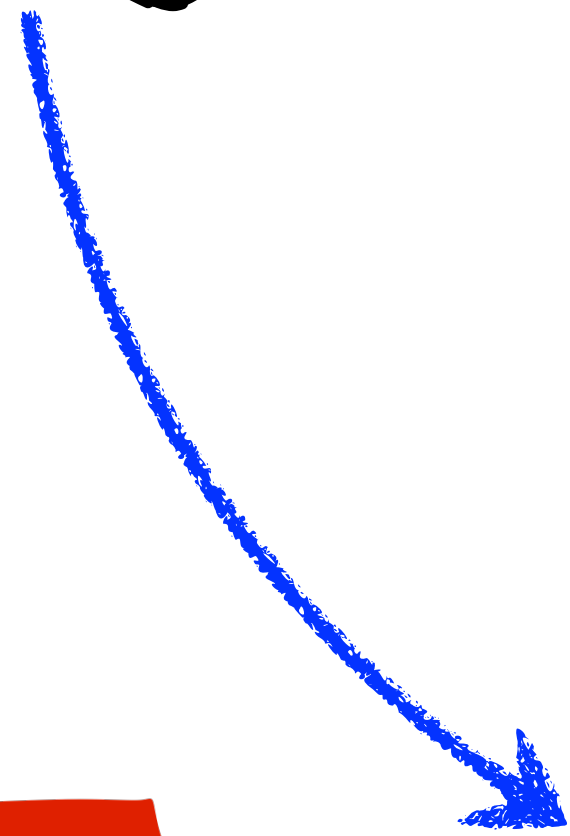


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MON


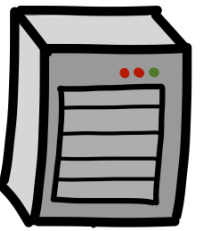
22  
JUN

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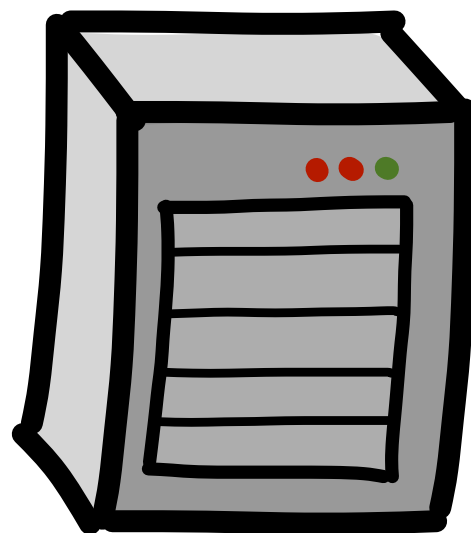
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View  
**indistinguishable**  
from honest case



MON

22  
JUN


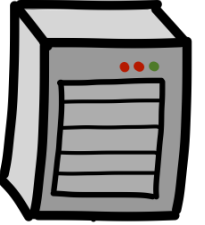
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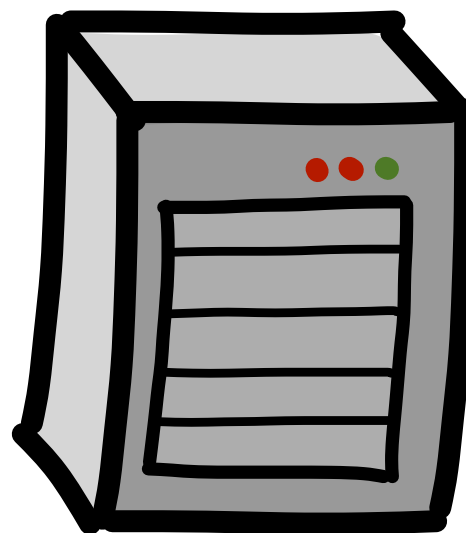
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View  
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from honest case

**SUCCESS**



MON


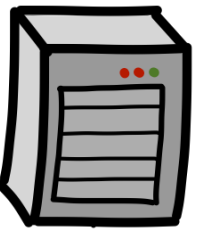
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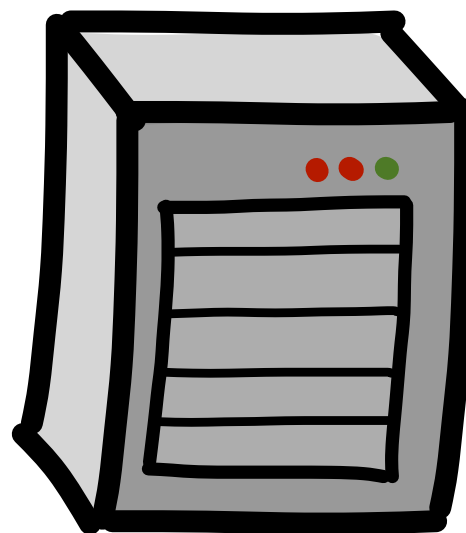
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**SUCCESS**



**SUCCESS**

By unanimous  
erasure

MON


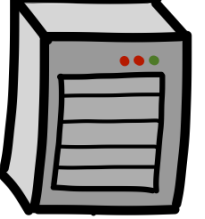
22  
JUN

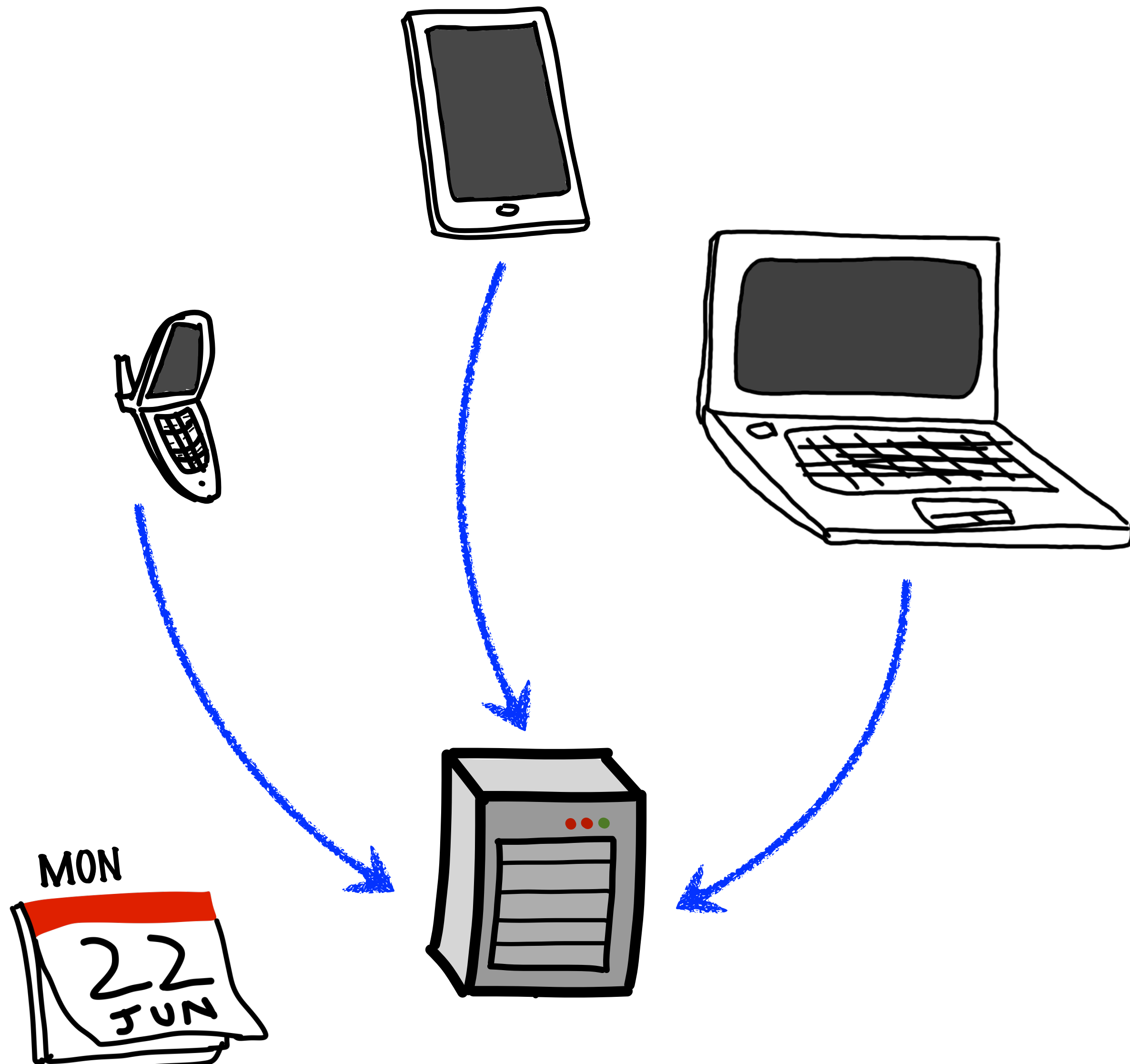
# Intuition: (3,4) case

**Assumption:**

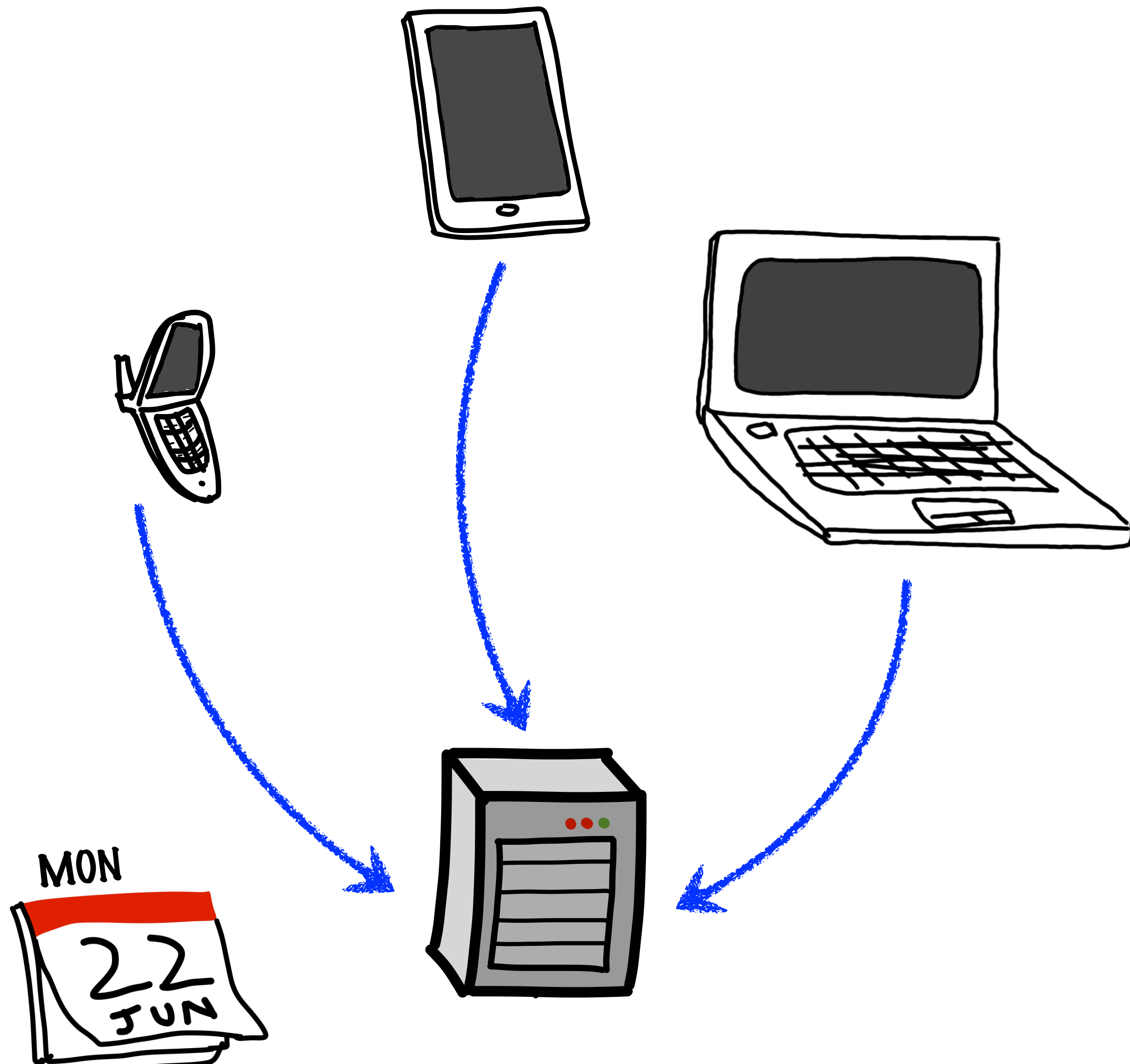
secure against corruption  
of two parties

**Claim:**

View of  has enough info  
for  to refresh




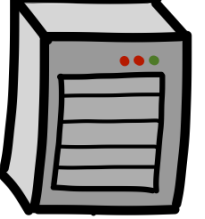
# Intuition: (3,4) case



## Assumption:

secure against corruption of two parties

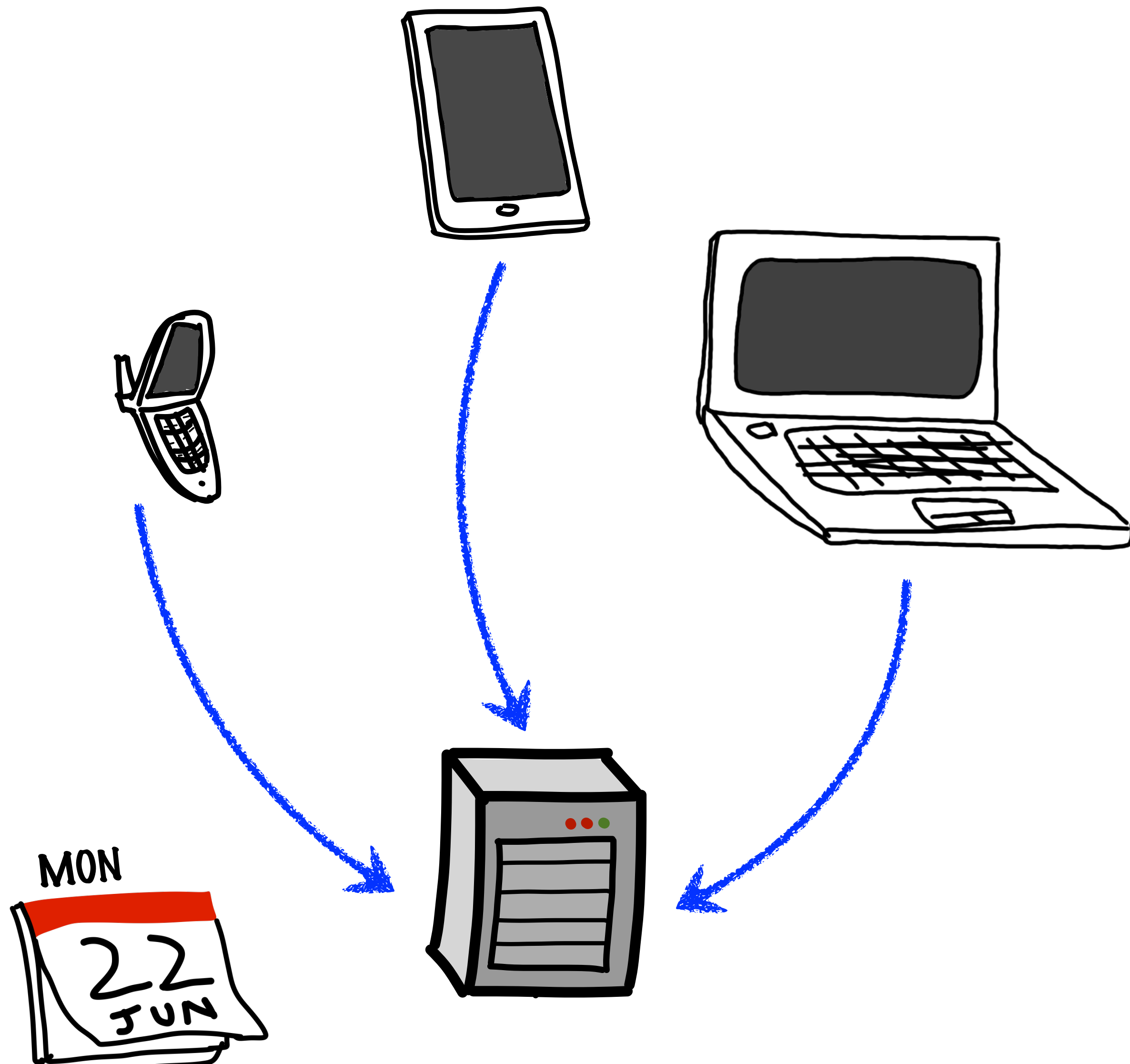
## Claim:

View of  has enough info for  to refresh

## Corollary:

Corrupting   on   
Gives secrets of  on 


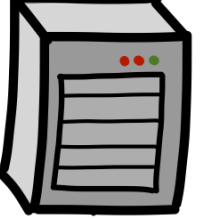
# Intuition: (3,4) case



## Assumption:

secure against corruption of two parties

## Claim:

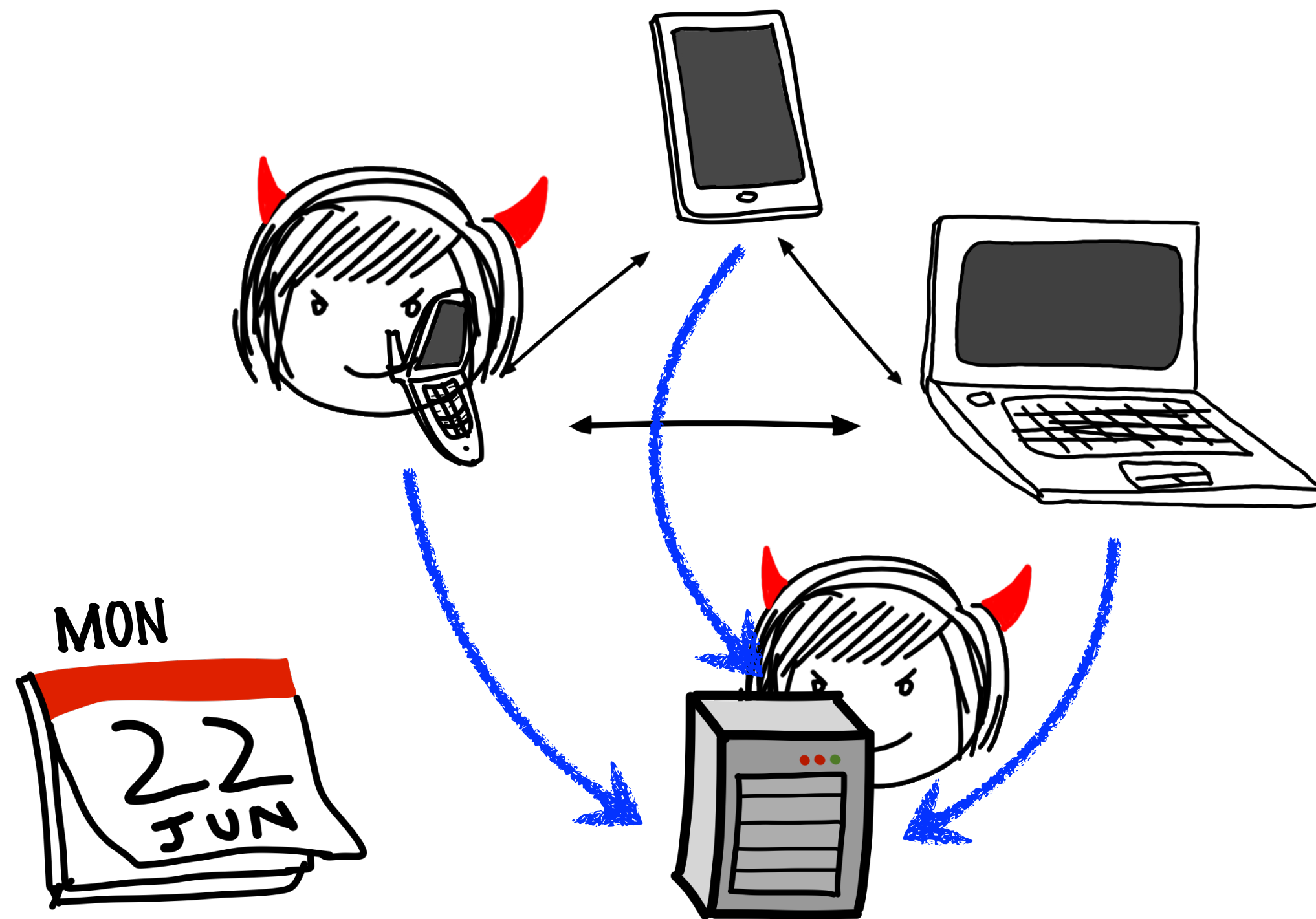
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## Corollary:

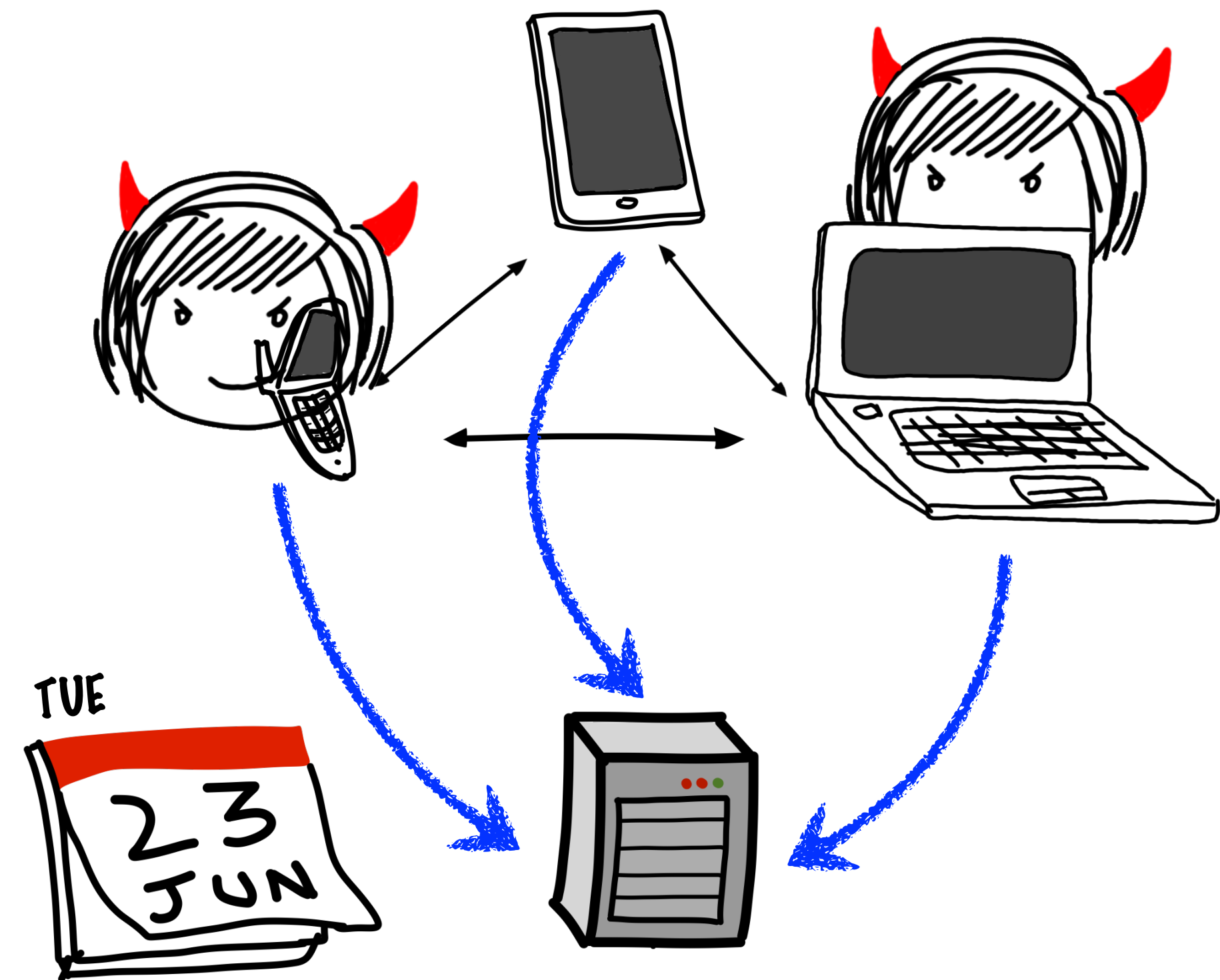
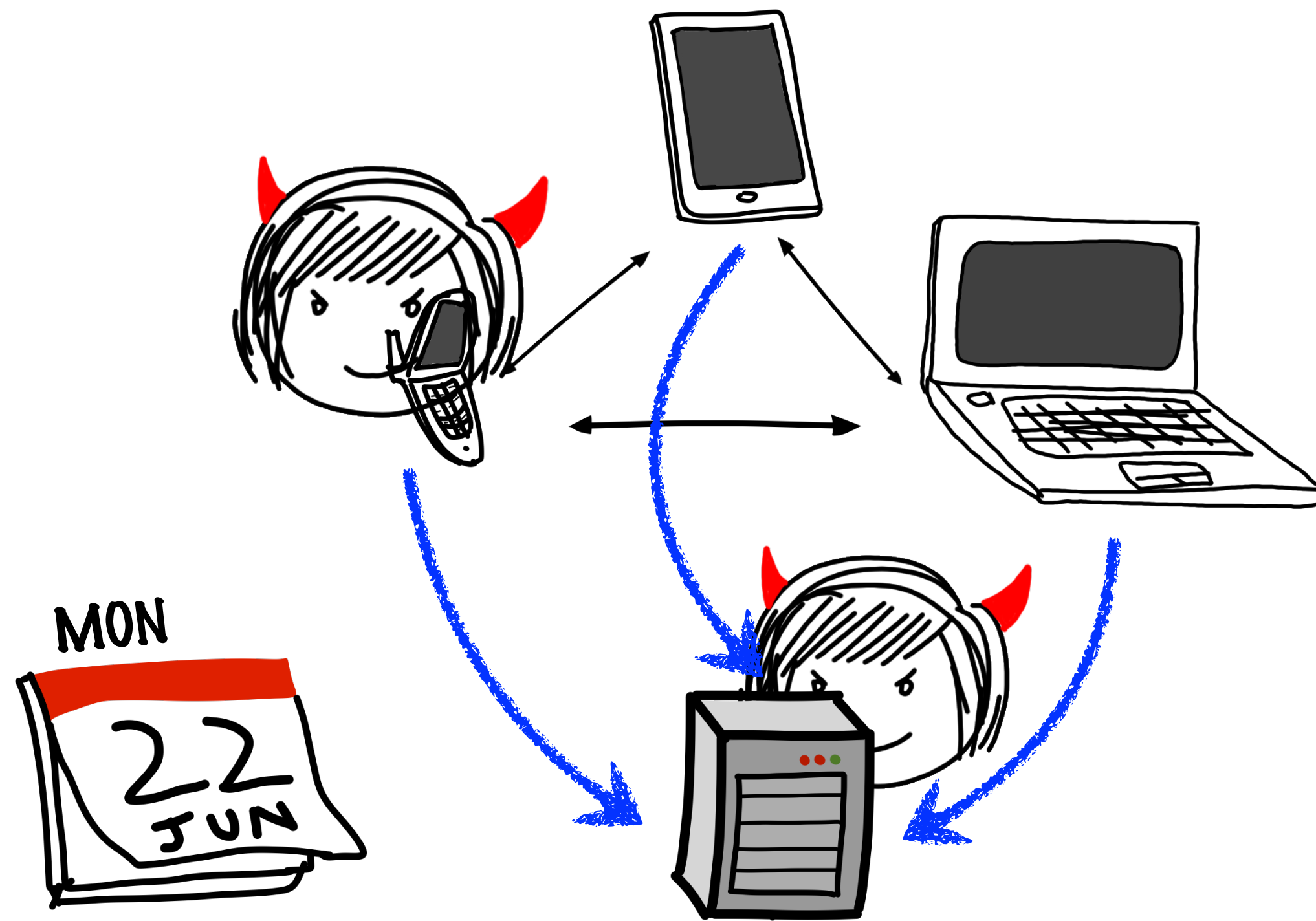
Even after uncorruption

Corrupting   on   
Gives secrets of  on 

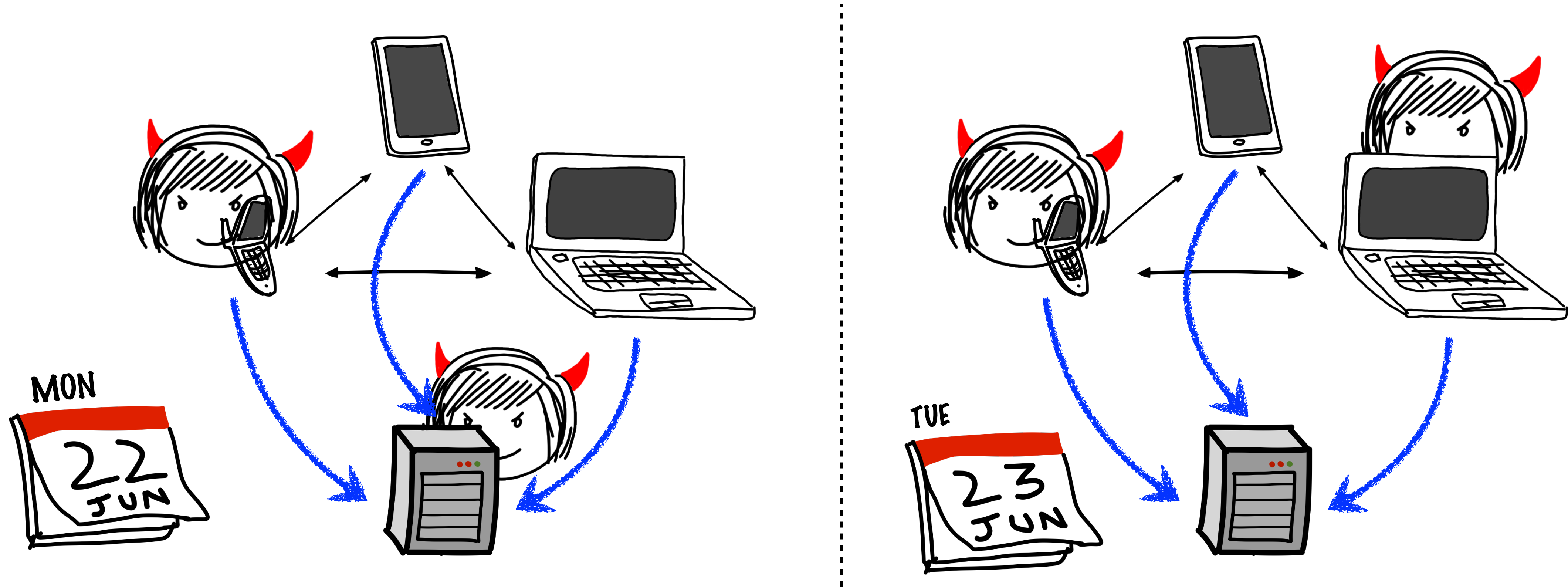
# General Attack Strategy



# General Attack Strategy

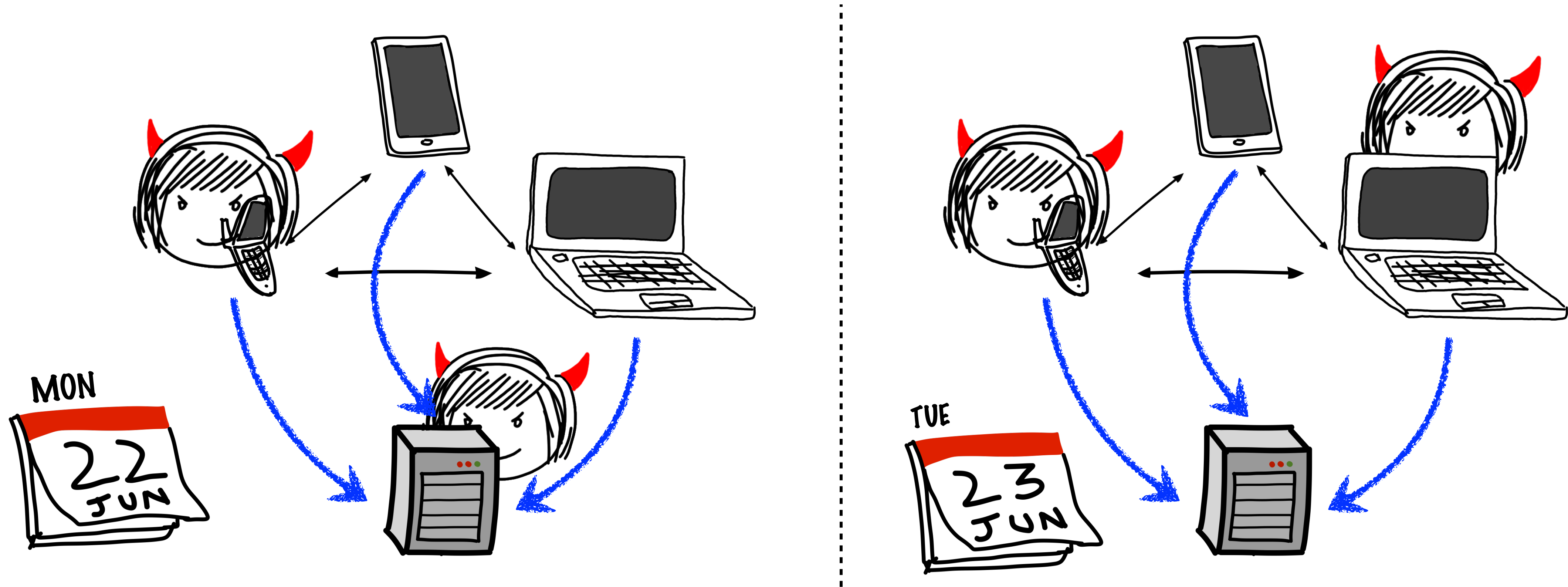


# General Attack Strategy



Can derive state of  on TUE even *after* refresh

# General Attack Strategy



Can derive state of  on TUE even ***after*** refresh

Two corrupt parties + 1 derived state = (3,4) broken

**See the paper for...**

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# See the paper for...

- Refreshing Multiplier/OT Extension state for ECDSA signing (hint: Beaver's OT correlation trick)
- Benchmarks of overhead added by  $(2,n)$  refresh to existing ECDSA implementation [Thanks Jack Doerner!](#)
- Discussions of definition, full proofs

# Thanks!

[eprint.iacr.org/2019/1328](https://eprint.iacr.org/2019/1328)

Thanks **Eysa Lee** for

